Example uses of ttr.sty for Record Types, Records, Functions, Operations and Relations

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• Simple record types:

$$R_{1}: \begin{bmatrix} l_{1} : T_{1} \\ l_{2} : T_{2} \\ l_{3} : T_{3}(l_{1}) \end{bmatrix}$$

$$R_{2}: \begin{bmatrix} l_{1} : T_{1} \\ l_{2} : T_{2'} \end{bmatrix}$$

$$R_{3}: []$$

 $\bullet \ \, \mbox{Simple records:}$

$$S_{1} = \begin{bmatrix} l_{1} = a \\ l_{2} = b \\ l_{3} = c \end{bmatrix}$$

$$S_{2} = \begin{bmatrix} l_{1} = a \\ l_{2} = b' \end{bmatrix}$$

$$S_{3} = \begin{bmatrix} \end{bmatrix}$$

• Complex record types (with manifest fields, embedded RTs and paths):

$$\begin{bmatrix} r & \vdots & \begin{bmatrix} x & \vdots & e \\ p_{=doctor(x)} & \vdots & t \\ p1_{=Chorlton(x)} & \vdots & t \end{bmatrix} \\ x_{=witness(r.x)} & \vdots & e \\ x1_{=spkr} & \vdots & e \\ ev_{=examine} & \vdots & es \\ p_{=subj(ev,x)} & \vdots & t \\ p1_{=obj(ev,x1)} & \vdots & t \end{bmatrix}$$

Complex records:

• Complex records:
$$\begin{bmatrix} x & = e \\ p_{=doctor(x)} & = t \\ p1_{=Chorlton(x)} & = t \end{bmatrix}$$

$$x_{=witness(r.x)} = e$$

$$x1_{=spkr} = e$$

$$ev_{=examine} = es$$

$$p_{=subj(ev,x)} = t$$

$$p1_{=obj(ev,x1)} = t$$

• RT functions:
$$\lambda r : \begin{bmatrix} l_1 : a \\ l_2 : b \end{bmatrix} . \begin{bmatrix} l_3 : a \end{bmatrix}$$

• Merge, min common super type and asymmetric merge functions:

$$x \wedge (y \vee z) = (x \wedge y) \vee (x \wedge z)$$
$$x \wedge y$$

• Subtype and supertype relations:

$$\begin{array}{c}
x \sqsubseteq y \\
x \sqsubseteq y
\end{array}$$

• Small inline versions:

You can put small record types inline as $[l_1 : a]$, records as $[l_1 = a]$ and functions as $\lambda r : [l_1 : a] . [l_2 : a]$.