

1. Problem

Tables are broken!

Tables are unable to provide reusable calculations.

Problem: Calculate profit margin of orders

prodName	custName	orderDate	revenue	cost
Нарру	Alice	2023/11/28	6	4
Acme	Bob	2023/11/27	5	2
Нарру	Alice	2024/11/28	7	4
Whizz	Celia	2023/11/25	3	1
Нарру	Bob	2022/11/27	4	1

Attempted solution: Create a view

prodName	custName	orderDate	revenue	cost
Нарру	Alice	2023/11/28	6	4
Acme	Bob	2023/11/27	5	2
Нарру	Alice	2024/11/28	7	4
Whizz	Celia	2023/11/25	3	1
Нарру	Bob	2022/11/27	4	1

2. Theory

Extend the relational model with measures

1. Allow tables to have measures

2. Operators for evaluating measures

3. Syntax to define measures in a query

```
SELECT *,
  (SUM(revenue) - SUM(cost)) / SUM(revenue)
  AS MEASURE profitMargin
FROM Orders
GROUP BY prodName;
```

Definitions

A **context-sensitive expression** (CSE) is an expression whose value is determined by an evaluation context.

An **evaluation context** is a predicate whose terms are one or more columns from the same table.

 This set of columns is the dimensionality of the CSE.

A **measure** is a special kind of column that becomes a CSE when used in a query.

- A measure's dimensionality is the set of non-measure columns in its table.
- The data type of a measure that returns a value of type *t* is *t* MEASURE, e.g. **INTEGER MEASURE**.

```
profitMargin is a
                             measure (and a
                             CSE)
SELECT prodName,
    profitMargin
FROM EnhancedOrders
                             Dimensionality is
GROUP BY prodName;
                             prodName, custName,
                             orderDate, revenue,
prodName profitMargin
                             cost
Acme
                  0.60
Happy
                  0.50
                             Evaluation context
Whizz
                  0.67
                             for this cell is
                             prodName = 'Acme'
SELECT (SUM(revenue) - SUM(
 / SUM(revenue) AS profitMargin
FROM Orders
WHERE prodName = 'Acme';
profitMargin
0.60
```

AT operator

The **context transformation operator AT** modifies the evaluation context.

Syntax:

```
expression AT (contextModifier...)

contextModifier ::=
   WHERE predicate
   | ALL
   | ALL dimension
   | SET dimension = [CURRENT] expression
   | VISIBLE
```

```
SELECT prodName,
    profitMargin,
    profitMargin
      AT (SET prodName = 'Happy')
      AS happyMargin
    profitMargin
      AT (SET custName = 'Bob')
      AS bobMargin
FROM EnhancedOrders
GROUP BY prodName;
prodName profitMargin happyMargin bobMargin
                 0.60
                              0.50
                                        0.60
Acme
                                         8.75
Happy
                 0.50
                              0.50
Whizz
                              0.50
                                        NULL
                 0.67
SELECT (SUM(revenue) - SUM(cost))
     / SUM(revenue) AS m
FROM Orders
WHERE prodName = 'Wbizz'
AND custName = 'Bob';
                         Evaluation context for
                         this cell is
                          prodName = 'Whizz'
NULL
                         AND custName = 'Bob'
```

3. Consequences

Grain-locking

What is the average age of the customer who would ordered each product?

When we use an aggregate function in a join query, it will 'double count' if the join duplicates rows.

This is generally not we want for measures – except if we want a weighted average – but is difficult to avoid in SQL.

Measures are locked to the grain of the table that defined them.

prodName	custName	orderDate	revenue	cost
Нарру	Alice	2023/11/28	6	4
Acme	Bob	2023/11/27	5	2
Нарру	Alice	2024/11/28	7	4
Whizz	Celia	2023/11/25	3	1
Нарру	Bob	2022/11/27	4	1

custName	custAge
Alice	23
Bob	41
Celia	17

Acme

Happy

Whizz

```
WITH EnhancedCustomers AS (
  SELECT *.
    AVG(custAge) AS MEASURE avgAge
  FROM Customers)
SELECT o.prodName,
  AVG(c.custAge) AS weightedAvgAge,
  c.avgAge AS avgAge
FROM Orders AS o
JOIN EnhancedCustomers AS c USING (custName)
GROUP BY o.prodName;
prodName weightedAvgAge avgAge
                                      Alice (age 23)
                                      has two orders;
```

41

32

17

Bob (age 41) has

one order.

Composition & closure

Just as tables are closed under queries, so tables-with-measures are closed under queries-with-measures

Measures can reference measures

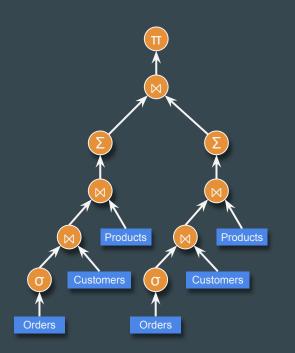
Complex analytical calculations without touching the **FROM** clause

Evaluation contexts can be nested

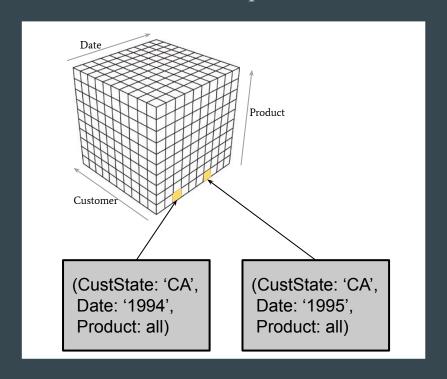
```
SELECT *,
  SUM(cost) AS MEASURE sumCost,
  SUM(revenue) AS MEASURE sumRevenue,
  (sumRevenue - sumCost) / sumRevenue
    AS MEASURE profitMargin,
  sumRevenue
    - sumRevenue AT (SET YEAR(orderDate)
        = CURRENT YEAR(orderDate) - 1)
    AS MEASURE revenueGrowthYoY,
  ARRAY_AGG(productId
    ORDER BY sumRevenue DESC LIMIT 5)
      AT (ALL productId)
      AS MEASURE top5Products,
  ARRAY_AGG(customerId
    ORDER BY sumRevenue DESC LIMIT 3)
    AT (ALL customerId
      SET productId MEMBER OF top5Products
        AT (SET YEAR(orderDate)
          = CURRENT YEAR(orderDate) - 1))
    AS MEASURE top3CustomersOfTop5Products
FROM Orders:
```

Bottom-up vs Top-down query

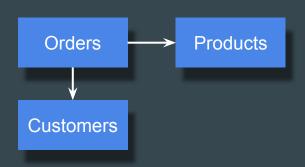
Relational algebra (bottom-up)



Multidimensional (top-down)



Represent a Business Intelligence model as a SQL view



- SQL planner handles view expansion
- Grain locking makes it safe to use a star schema
- Users can define new models simply by writing queries

```
CREATE VIEW OrdersCube AS
SELECT *
FROM (
  SELECT o.orderDate AS `order.date`,
    o.revenue AS `order.revenue`,
    SUM(o.revenue) AS MEASURE `order.sum_revenue`
  FROM Orders) AS o
LEFT JOIN (
  SELECT c.custName AS `customer.name`,
    c.state AS `customer.state`,
    c.custAge AS `customer.age`,
    AVG(c.custAge) AS MEASURE `customer.avg_age`
  FROM Customers) AS c
ON o.custName = c.custName
LEFT JOIN (
  SELECT p.prodName AS `product.name`,
    p.color AS `product.color`,
    AVG(p.weight) AS MEASURE `product.avg_weight`
  FROM Products) AS p
ON o.prodName = p.prodName;
```

```
SELECT `customer.state`, `product.avg_weight`
FROM OrdersCube
GROUP BY `customer.state`;
```

Implementing measures & CSEs as SQL rewrites

simple				
	1			

Complexity	Query	Expanded query
Simple measure can be inlined	SELECT prodName, avgRevenue FROM OrdersCube GROUP BY prodName	SELECT prodName, AVG(revenue) FROM orders GROUP BY prodName
Join requires grain-locking	SELECT prodName, avgAge FROM OrdersCube GROUP BY prodName	SELECT o.prodName, AVG(c.custAge PER c.custName) FROM orders JOIN customers GROUP BY prodName → (something with GROUPING SETS)
Period-over- period	SELECT prodName, avgAge - avgAge AT (SET year = CURRENT year - 1) FROM OrdersCube GROUP BY prodName	(something with window aggregates)
Scalar subquery can accomplish anything	SELECT prodName, prodColor avgAge AT (ALL custState SET year = CURRENT year - 1) FROM OrdersCube GROUP BY prodName, prodColor	SELECT prodName, prodColor, (SELECT FROM orders WHERE <evaluation context="">) FROM orders GROUP BY prodName, prodColor</evaluation>

Summary

Top-down evaluation makes queries concise

Measures make calculations reusable

Measures don't break SQL

