SOME NICE COMPUTATIONS THE MHS SOFTWARE CAN DO

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$$\sum_{p-1\geq n>m\geq 3} \frac{\binom{p+m}{m}}{n(m-2)} \equiv -\frac{13}{4} - \frac{31}{4} + 4\zeta_p(3) \quad p \mod p^2.$$

$$\sum_{p-1\geq n\geq m\geq 3} \frac{\binom{p+m}{m}}{n(m-2)} \equiv -2 - (5 + 4\zeta_p(3))\, p - 12\zeta_p(3)p^2 \mod p^3.$$

$$\sum_{n=1}^{p-1} H_n(1,1) \sum_{m=1}^{p-4} \binom{m+p+2}{p} \frac{1}{m^3} \equiv -\frac{1}{8} - \frac{17}{16}p + \left(3 + \frac{9}{2}p\right) \zeta_p(3) - 11p\,\zeta_p(5) \mod p^2.$$

$$\sum_{n=0}^{p} \binom{p}{n}^4 \equiv 2 - 16p^5\,\zeta_p(5) - 20p^6\,\zeta_p(3)^2 - 143p^7\,\zeta_p(7) + O(p^8)$$

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