

Problem Sets from Chapter three

In class I will do Questions: #2B, #6A, #8, #10,

For homework you will do questions: #2C, #3, #6B, #7A, #13, #14

This homework will be due beginning of class Monday Sept. 23rd at the beginning of class. It should be handwritten, you can turn it in or you can upload by scanning in your documents and putting it in the Dropbox on D2L.....before class the Dropbox will shutdown at 9am September 23rd and there will be no late assignments accepted.

1. The two mathematical models of language description are generation and recognition. Describe how each can define the syntax of a programming language.
2. Write EBNF descriptions for the following:
 - a. A Java class definition header statement
 - b. A Java method call statement
 - c. A C **switch** statement
 - d. A C **union** definition
 - e. C **float** literals
3. Rewrite the BNF of **Example 3.4 (Given below)** to give `+` precedence over `*` and force `+` to be right associative.

Example 3.4 An Unambiguous Grammar for Expressions

```
<assign> → <id> = <expr>
<id> → A | B | C
<expr> → <expr> + <term>
        | <term>
<term> → <term> * <factor>
        | <factor>
<factor> → ( <expr> )
          | <id>
```

4. Rewrite the BNF of **Example 3.4** (Given in Question #3) to add the `++` and `--` unary operators of Java.

5. Write a BNF description of the Boolean expressions of Java, including the three operators `&&`, `||`, and `!` and the relational expressions.
6. Using the grammar in **Example 3.2 (Given Below)**, show a parse tree and a leftmost derivation for each of the following statements:
- `A = A * (B + (C * A))`
 - `B = C * (A * C + B)`
 - `A = A * (B + (C))`

Example 3.2 A Grammar for Simple Assignment Statements

$\langle \text{assign} \rangle \rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle$

$\langle \text{id} \rangle \rightarrow A \mid B \mid C$

$\langle \text{expr} \rangle \rightarrow \langle \text{id} \rangle + \langle \text{expr} \rangle$

$\quad \mid \langle \text{id} \rangle * \langle \text{expr} \rangle$

$\quad \mid (\langle \text{expr} \rangle)$

$\quad \mid \langle \text{id} \rangle$

7. Using the grammar in **Example 3.4 (Given in Question 3)**, show a parse tree and a leftmost derivation for each of the following statements:
- `A = (A + B) * C`
 - `A = B + C + A`
 - `A = A * (B + C)`
 - `A = B * (C * (A + B))`

Example 3.4 An Unambiguous Grammar for Expressions

$\langle \text{assign} \rangle \rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle$

$\langle \text{id} \rangle \rightarrow A \mid B \mid C$

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle$

$\quad \mid \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle$

$\quad \mid \langle \text{factor} \rangle$

$$\begin{aligned} \langle \text{factor} \rangle &\rightarrow (\langle \text{expr} \rangle) \\ &\quad | \langle \text{id} \rangle \end{aligned}$$

8. Prove that the following grammar is ambiguous:

$$\begin{aligned} \langle S \rangle &\rightarrow \langle A \rangle \\ \langle A \rangle &\rightarrow \langle A \rangle + \langle A \rangle \quad | \quad \langle \text{id} \rangle \\ \langle \text{id} \rangle &\rightarrow a \quad | \quad b \quad | \quad c \end{aligned}$$

9. Modify the grammar of **Example 3.4 (Given in Question 3 or 7)** to add a unary minus operator that has higher precedence than either `+` or `*`.

10. Describe, in English, the language defined by the following grammar:

- $\langle S \rangle \rightarrow \langle A \rangle \langle B \rangle \langle C \rangle$
- $\langle A \rangle \rightarrow a \langle A \rangle \quad | \quad a$
- $\langle B \rangle \rightarrow b \langle B \rangle \quad | \quad b$
- $\langle C \rangle \rightarrow c \langle C \rangle \quad | \quad c$

11. Consider the following grammar:

- $\langle S \rangle \rightarrow \langle A \rangle a \langle B \rangle b$
- $\langle A \rangle \rightarrow \langle A \rangle b \quad | \quad b$
- $\langle B \rangle \rightarrow a \langle B \rangle \quad | \quad a$

Which of the following sentences are in the language generated by this grammar?

- c. baab
- d. bbbab
- e. bbaaaaa **S**
- f. bbaab

12. Consider the following grammar:

- $\langle S \rangle \rightarrow a \langle S \rangle c \langle B \rangle \mid \langle A \rangle \mid b$
- $\langle A \rangle \rightarrow c \langle A \rangle \mid c$
- $\langle B \rangle \rightarrow d \mid \langle A \rangle$

Which of the following sentences are in the language generated by this grammar?

- c. abcd
- d. acccbd
- e. acccbcc
- f. acd
- g. accc

13. Write a grammar for the language consisting of strings that have n copies of the letter a followed by the same number of copies of the letter b, where $n > 0$. For example, the strings ab, aaaabbbb, and aaaaaaabbbbbbbb are in the language but a, abb, ba, and aaabb are not.

14. Draw parse trees for the sentences aabb and aaaabbbb, as derived from the grammar of [Problem_13](#).

15. Convert the BNF of [Example_3.1 \(Given Below\)](#) to EBNF.

Example 3.1 A Grammar for a Small Language

```

<program> → begin <stmt_list> end
<stmt_list> → <stmt>
                | <stmt> ; <stmt_list>
<stmt> → <var> = <expression>
<var> → A | B | C
<expression> → <var> + <var>
                | <var> - <var>
                | <var>

```

16. Convert the BNF of **Example 3.3** to EBNF.

Example 3.3 An Ambiguous Grammar for Simple Assignment Statements

$\langle \text{assign} \rangle \rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle$
 $\langle \text{id} \rangle \rightarrow A \mid B \mid C$
 $\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{expr} \rangle$
 $\quad \quad \quad \mid \langle \text{expr} \rangle * \langle \text{expr} \rangle$
 $\quad \quad \quad \mid (\langle \text{expr} \rangle)$
 $\quad \quad \quad \mid \langle \text{id} \rangle$

17. Convert the following EBNF to BNF:

- $S \rightarrow A \{bA\} S \rightarrow A \{bA\}$
- $A \rightarrow a[b]A$