

Julia Diliberto
CST 370
Homework 4

- 1a. Sum of the squares from 1 to n
1b. Multiplication
1c. n
1d. $O(n)$

- 2a. The range of values in the array
2b. Comparison
2c. $2n-2$
2d. $O(n)$

3a. $999 = 1 + 2(n-1)$
 $999 = 1 + 2n - 2$
 $999 = 2n - 1$
 $2n = 1000$
 $n = 500$

$$S_n = \frac{500(1+999)}{2}$$

$$S_n = 250(1000) = 250000$$

3b. $1024 = 2(2)^{n-1}$
 $512 = 2^{n-1}$

$$\ln(512) = \ln(2^{n-1})$$

$$\ln 512 = (n-1)\ln 2$$

$$\ln 512 / \ln 2 = n - 1$$

$$\ln 512 / \ln 2 + 1 = n$$

$$n = 10$$

$$S_n = \frac{2(2)^{10} - 2}{1}$$

$$S_n = 2046$$

4. $f(1)=1; f(2)=2; f(3)=3; f(4)=5; f(5)=8...$

$$f(n) = f(n-1) + f(n-2), n \geq 3; f(1)=1, f(2)=2$$

fibonacci

5a. $x(n) = x(n-1) + 5$

$$x(1) = 0$$

$$x(2) = x(n-1) + 5 = 5$$

$$x(3) = x(n-1) + 5 = 10$$

$$x(4) = x(n-1) + 5 = 15$$

$$x(n) = 5(n-1)$$

$$5b. \ x(n)=3x(n-1)$$

$$x(1)=4$$

$$x(2)=3x(n-1)=3*4=12$$

$$x(3)=3 \ x(n-1)=3*3*4=36$$

$$x(4)=3 \ x(n-1)=3*3*3*4=108$$

$$x(n)=3^{(n-1)} * 4$$

$$5c. \ x(n)=x(n-1) + n$$

$$x(0)=0$$

$$x(1)=x(n-1) + n=0+1=1$$

$$x(2)=x(n-1)+n=0+1+2=3$$

$$x(3)=x(n-1)+n=0+1+2+3=6$$

$$x(4)=x(n-1)+n=0+1+2+3+4=10$$

$$x(5)=x(n-1)+n=0+1+2+3+4+5=15$$

$$x(n)=1+2+3...+n=\frac{n(n+1)}{2}$$

$$2$$