# Examples of single location, single population models using ordinary differential equations Lecture 02

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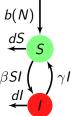
The SLIRS models

An extension of KMK - SLIAR models

## The SLIRS models

An extension of KMK – SLIAR models

## Simplifying the SIRS model



- ► We have already seen the epidemic KMK SIR model and the endemic SIRS model
- ▶ By making some simplifications, we can obtain the SIS model: assume the time spent in the R compartment goes to zero, i.e.,  $\nu \to \infty$

The main characteristics of the model are the same as the SIRS

$$\mathcal{R}_0 = \frac{\beta}{d+\gamma}$$

and determines whether we go to the DFE  $(N^*, 0)$  or to the endemic equilibrium

p. 1 - The SLIRS models

#### The SLIRS models

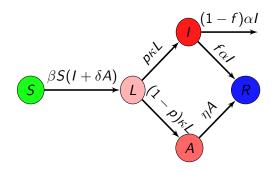
An extension of KMK - SLIAR models

SIR is a little too simple for many diseases:

- No incubation period
- ► A lot of infectious diseases (in particular respiratory) have mild and less mild forms depending on the patient

⇒ model with SIR but also L(atent) and (A)symptomatic individuals, in which I are now symptomatic individuals

Arino, Brauer, PvdD, Watmough & Wu. Simple models for containment of a pandemic (2006)



## Basic reproduction number

$$\mathcal{R}_{0} = S_{0}\beta \left(\frac{p}{\alpha} + \frac{\delta(1-p)}{\eta}\right) = \frac{S_{0}\beta\rho}{\alpha}$$

$$\rho = \alpha \left(\frac{p}{\alpha} + \frac{\delta(1-p)}{\eta}\right)$$
(1)

where

### Final size relation

$$S_0(\ln S_0 - \ln S_\infty) = \mathcal{R}_0(S_0 - S_\infty) + \frac{\mathcal{R}_0 I_0}{\rho}$$
 (2)