



$$\begin{aligned}
 S' &= b - dS - \beta_S SI \\
 L' &= \beta_S SI + \gamma_T T + \gamma_I I - dL - \epsilon L - t_L L \\
 I' &= \epsilon L + \beta_T TI - (d + \delta)I - \gamma_I I - t_I I \\
 T' &= t_L L + t_I I - dT - \beta_T TI - \gamma_T T
 \end{aligned}$$

DFE: $L = I = T = 0$
 $\Rightarrow S^* = \frac{b}{d}$

$$\mathcal{I} = \{L, I, T\}$$

$$\mathcal{F} = \begin{pmatrix} \beta_S SI \\ 0 \\ 0 \end{pmatrix} \quad \mathcal{V} = \begin{pmatrix} (d + \epsilon + t_L)L - \gamma_T T - \gamma_I I \\ \gamma_I I + t_I I + (d + \delta)I - \beta_T TI - \epsilon L \\ \gamma_T T + \beta_T TI - t_L L - I + dT \end{pmatrix}$$

$$F = D\mathcal{F}_{(DFE)} = \begin{pmatrix} 0 & \beta_S S^* & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad V = D\mathcal{V}_{(DFE)}$$

$$V = \begin{pmatrix} d + \epsilon + t_L & -\gamma_I & -\gamma_T \\ -\epsilon & \gamma_I + t_I + d + \delta - \beta_T & -\beta_T I \\ -t_L & \beta_T & \gamma_T + \beta_T I + d \end{pmatrix}$$

$$FV^{-1} = \begin{pmatrix} 0 & \beta_S S^* & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} V_{11}^{-1} & V_{12}^{-1} & V_{13}^{-1} \\ V_{21}^{-1} & V_{22}^{-1} & V_{23}^{-1} \\ V_{31}^{-1} & V_{32}^{-1} & V_{33}^{-1} \end{pmatrix} = \begin{pmatrix} \beta_S S^* V_{11}^{-1} & * & * \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

invV[2,1]:

$$(\text{epsilon} (\text{gamma}_T + d)) /$$

$$((\text{gamma}_T + d) (t_I + \text{gamma}_I + \text{delta} + d) (t_L + \text{epsilon} + d) - \text{gamma}_T (t_I + \text{gamma}_I + \text{delta} + d) t_L - \text{epsilon} \text{gamma}_I (\text{gamma}_T + d))$$