PHARMACOKINETICS - THE MODELING OF DEUG ADMINISTRATION

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### INTRODUCTION

In the prescription of drugs, Pharmacists often employ Mathematical Models that help formulate optimum disages.

The problem is to determine the best possible Pharmaco Kinetic Model for a given situation. The body has many "mechanisms" at work that constantly deplete an administered drug supply. The bodily function of excretion in the kidneys steadily removes much of the drug from the blood tissue. Body Metabolism can "burn" much at the drug in the digestive tract, if taken ovally. As well, some drugs have an affinity for certain body tissues other than the one that they were prescribed for, thus, the drug may be captived by these tissues. Obviously, finding the correct madel for a drug may be very challenging and requires much laboratory testing.

In determining an optimum dosage many considerations must be made. Many drugs have a "MINIMUM EFFECTIVE CONCENTRATION" (MEC), a level telow which the drug concentration is too low to have the desired effect. Conversely, many drugs have a "MINIMUM TOXIC CONCENTRATION" (MTC) which represents the level above which the drug "barely" produces an observable toxic effect.

Two of the many methods of administration include Rapid Intravenous Injection (IV Boxs) and Dral Injection. These administration methods may be applied to models which involve a single dose or multiple doses of a drug.

Notice that Cn and Rn are geometrical serves, and hence may be rewritten as:

which represents the residual Concentration for any desage number 1.

Now it now, e-nkt >0 yielding:

which is in fact, the lower limit of the Residual Concentrations. Hence this multiple injection scheme scens to achieve a steady-state" with lower bound Ro.

Similarly for Cn:

Cn can be written in geometrical serves form:

$$C_n = C_0 \frac{(1 - e^{-nkT})}{1 - e^{-kT}}$$

which represents the Concentration of the chang immediately after the administration of dese n.

Agam as N-D, e-NKT-70:

And Co is the upper bound of the Concentration of the dry on the compositment. Hence in steady state the dry concentration effectively "Oscillates" between 200 and Co

## ANALYSIS OF CO, RO

Since it 15 known that Co is an upper bound for the drug concentration, is there a period T that will allow ((1)) with stay below any Upper bound, say 4?

want: 
$$C^{\infty} \leq U$$

15 a sufficiently long period that Co stays below U.

Similarly, since  $R^\infty$  provides a lower bound for the drug concentration, a period T can be determined such that  $R^\infty \geq L$ , some lower bound:

Want: 200 2 L

Coe-KT > L

 $\frac{C_0}{L} \ge \frac{1-e^{-kT}}{e^{-kT}}$ 

6 ≥ e KT-/

(0+12 ext

ln(Co+1) 2 ln ekt

ln(Co+L) 2KT

T= L lu (o+L)

"T= I low Co+L

with provide a sufficiently short (actually = gives the maximum) time period such that the lower bound 1200 is not crossed. (ie from above)

Note that if T gets larger the maximum bound (upper) decirases, and it T decreuses. In size, the upper bound is raised.

See Fig 4,2 in CASE (4) for a basic example of this phenomenon of different time periods.

( door minsed.

Also note it the dosage supply is cut-off the curve just tollows the natural Malthosian chimination.

### CONCLUSIONS - CASE (3)

This model, while it effectively demonstrates the result of a Multiple Rapid Infravenas Injection Scheme, has some practical short comings:

The assumption the K is constant may be somewhat suspect as metabolic rates and excretion rates may Secondly, if the mections are given only in waking hours the residual concentration falls during the night, honce the Total Concentration may then tall in

Another short coming is the time required to reach MEC. For the first few my octons the concentration of the drug may be below MEC. Solutions for this problem include decreasing the period between injections or by using a LOADING DOSE, which may be double or triple the "usual" Co. This loading dose quakly builds up the Residual Concentration, and would also be effective for the case in the preceding paragraph.

Frally the drug may not conform to a single compartment model. A two or more compartment Scheme may have to be devised which accounts for slower tissue release of the diray ( rather thun being proportional to the blood).

Therefore, while this model seems a little More robust than its single dose predecessor, it is not without fault.

References: 5,6

# CASE (3) ORAL INTECTION, SINGLE DOSE

In the eral administration of a drug (ie. by pill, capsule, or liquid) consideration must be made for the "lentrance" of the drug into the compontment from the gastro-intestinal tract (ie. the gut). Similarly, as with previous cases, the elimination of the drug must also be taken into account.

#### ASSUMPTIONS:

- a one compartment model. (i.e. one in which any change in concentration of the dray in the blood is proportional to the change of the concentration of the dray in the dray in the bedy tissues.
- 2) That we shall analyze the amount of drug on the body, for simplicity of ais the amount of drug is proportional to the Concentration. (Concentration = amount / wolume)
- 3 That The absorption of the drug by the get follows a first order process, as before. And similarly the elimination: of the drug from the blood follows a first order process, for Simplicity
- (4) Assume that all of the day intaken into the got is eventually absorbed into the blood. This removes any consideration of only a fraction of the drug dose entering the blood.
- (5) For generality that all forms of oral drugs act identically und do not interact with only contents in the gut or gastro-intestinal fluids.
- @ All general assumptions still apply

Let:

t-represent time (hrs) and t(0)=6 (mitial time)

G(t)-be the amount of drug in the gut of any fine t ≥0

C2(t)-be the amount of drug in the blood at time t; t ≥0

G(t)-be the amount of drug eliminated (se in Kiling) at time t; t ≥0

Ke-the elimination constant (howr-1), Ke>0

Ka=the ads-cription constant of the drug into the compartment, Ka>0

Co-15 the initial amount of the drug is sued at time to

The following system of linear first order equations is obtained:

- (1) the equation representing the ranged rate of the day from the gut:  $\frac{d\zeta(t)}{dt} = -k_0 \zeta_1(t) \qquad \qquad \zeta(t_0) = C_0$
- 2) The change on amount of dray on the blood, which is the amount obtained from the get, less the amount eliminated:  $\frac{d(z(t))}{dt} = k_0 G(t) k_0 G(t), \quad (z(t_0) = 0)$
- (3) The change on the amount of drug eliminated:  $\frac{dC_3(4)}{dt} = K_{C_2}(4) \qquad , \qquad C_3(6) = 0$

Solving ():

$$\frac{dC_i(t) = -K_aC_i(t)}{dt} = -K_aC_i(t) = C_i(t_0) = C_0$$

$$\int \frac{dC_1}{C_1} = -k_0 \int dt$$

=) 
$$lr/C_1/=-Kat+A$$
 A-constant of integration  $lnC_1=-Kat$  Stree (4)20

exponentiating:

The function (x) was previously analyzed in case D.

Now, using & we can solve equation (2) of the system:

$$\frac{dC_z(t) = K_aC_1(t) - K_eC_2(t)}{dt}, \quad C(t_0) = 0$$

Substituting for G(t) by 8;

This is a Imear first order differential equation, which can be written as:

Integrating Factor:

- the equation becomes:

Id C3(t) = SKe Ka Co (e-tat-e-ket) dt

(18)

factoring a -1 from the denomination:

$$C_3(t) = \frac{\left(\frac{k_0 K_0 C_0}{K_0 - k_0 t}\right) \left(\frac{e^{-k_0 t}}{K_0} - \frac{e^{-k_0 t}}{K_0}\right) + E}{\left(\frac{k_0 C_0}{K_0 - k_0 t}\right) \left(\frac{e^{-k_0 t}}{K_0} - \frac{e^{-k_0 t}}{K_0}\right)}$$

et a consta of integration

Since C3(t)=0 when t=0, we solve for E

$$C_3(0) = 0 = \frac{K_e K_a C_o}{(K_a - K_e)} \left( \frac{e^{-K_a(0)}}{K_a} - \frac{e^{-K_a(0)}}{K_e} \right) + E$$

$$O = \frac{K_{e}K_{a}G_{o}}{K_{a}-K_{e}}\left(\frac{1}{K_{a}}-\frac{1}{K_{e}}\right) + E$$

- The mitral value solution of (3(+):

$$C_3(t) = \frac{K_e K_a G_o}{(K_a - k_e)} \left( \frac{e^{-K_a t}}{K_a} - \frac{e^{-K_e t}}{K_e} \right) + G_o$$

) construct

4NALYSIS OF THE EXPLKIT SOLUTIONS GILL, &

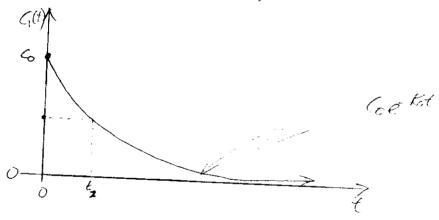
Recall-

## (1) ANALYSIS OF G(t):

For this function, Figure 3.0 is obtained:

FIGURE (3.1)

C,(4) Us. E



This sketch is instantly recognizable as a Malthusian-type

To find the time that any amount of drug C, is still in

$$\Rightarrow \frac{C_1}{C_0} = e^{-kat}$$

$$= \ln(\frac{C_1}{C_0}) = \ln e^{-\kappa_0 t}$$

$$\ln(\frac{C_1}{C_0}) = -\kappa_0 t$$

Agam, This t gives the time any assessent G (04G &Co) that is remaining in the gut

Defermining the hult-life of the drug in the gut; C,= \(\frac{1}{2}\)Co (i.e. at what time is the drug half gone from the gut)

$$t_z = \frac{1}{k_0} \left( \frac{z}{\zeta_0} \right)$$

$$= \frac{1}{k_0} \frac{y_0(z)}{z} \approx \frac{.693}{k_0}$$

Notice that the half-life is independent at the mitial dose amount.

Intuitively, as the equation for  $C_Z(4)$  is based on the d.e.  $\frac{dC_Z(4)}{dt} = K_G(\zeta(4) - K_CC_Z(4)$ 

which says that the change in amount of drug in the blood is equal to the amount absorbed from the gut, less the amount of drug eliminated, leads to the Suspicion that the amount of drug may have a a maximum. at some time.

# Consider the plot of C2(t) us to FIGURE 3.2 ((t) us. t

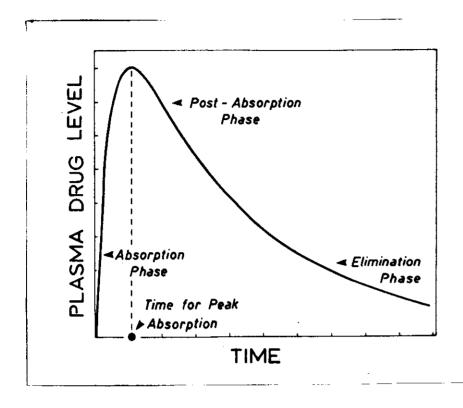


Figure 3.2 Plasma level—time curve for a drug given in a single oral dose. The drug absorption and elimination phases of the curve are shown.

To determine if the maximum indicated by the sketch occurs, the first derivative test is applied to  $C_Z(t)$ 

inas critical points if  $C_2'(t) = 0$  or is undefined: (cannot be undefined as  $-K_a \neq -K_e$  by assumption previously)



$$t_2 = ln(\frac{ke}{ka})\frac{1}{(ke-ka)}$$

Hence a maximim amount of drug is absorbed at tz. Notice that this time is independent of the amount of drug intrally injected.

The amount of dry in the blood at to can be determined:

: the Maximum amount of drug in the compartment is directly proportional to the mitral dosage amount and is independent of time-

Determining the time t, for a given amount of drag in the blood (c) Solve for t:

$$ln\left(\frac{(-k_a+k_e)}{k_a(o)}\right) = ln\left(e^{-k_at}-e^{-k_et}\right)$$

$$\frac{1}{4\pi k_{0}} \int_{C} \int$$

which finds the time for an amount of drig such that Cz >0.

Here, intuitively, the expectation is that "eventually" all of the drug will be eliminated from the system. Further, it does not seem unlikely that this model post" may behave inversely propositional to the adsorption past of the model.

The following sketch of C3(t) V5 t (bottom one) tends to show agreement with the above assessment:

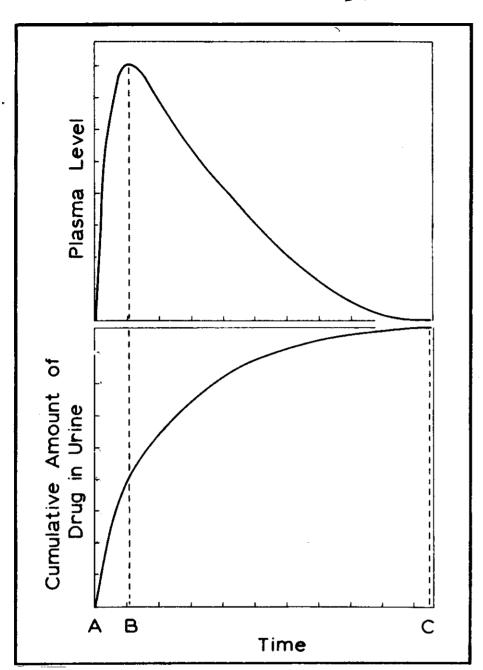


Figure 3.3 Corresponding plots relating the plasma level—time curve and the cumulative urinary drug excretion.

Here, the sketch suggests that a limit occurs at Co as t-no By taking the limit as t-no on C3(t), the supposition is proved:

lem (3(1) = Co

Determining the time to that an amount of dry Cz has been removed from the compositment

$$\frac{\left(3-C_0\right).\left(k_a-k_e\right)}{K_eK_aC_0}=\frac{e^{-k_at}}{K_a}-\frac{e^{-k_et}}{K_e}$$

$$ln\left(\frac{C_3-C_0}{K_eK_aC_0}\right)\left(\frac{K_a-K_e}{K_e}\right) = ln\left(\frac{e^{-K_at}}{K_a} - \frac{e^{-K_et}}{K_e}\right)$$

$$= \ln \left( \frac{e^{-kat}}{Ka} \right)$$

$$= \frac{e^{-kat}}{e^{-ket}}$$



$$\frac{\Rightarrow h/(G-G)(K_0-K_0)-h/K_0}{K_0+K_0}=f$$

$$\frac{1}{K_0+K_0}$$

$$\frac{1}{K_0+K_0}$$

:. (-Ko-Ke) ((3-6) Ka (Ko-Ke))

for any amount of G such that 04G = 6

### CONCLUSIONS - CASE (3)

As in the single dose, rapid introversors injection case, this model only provides a reasonable drug regimen it Ke, the elimination constant, is quite small and/or if Ka the drug absorption constant is large much to allows" enough drug into the compostmento. This would allow the concentration of the drug in the blood to remain above Minimum Effective Concentration.

To prolong the time that the concentration is above MEC, a multiple Oral Dosage scheme could be Considered.

#### DISADVANTAGES:

A major disadvantage of this model is that it assumes that all of the dray enters the compartment A minor revision of the model could involve examining the problem of only a fraction of the dray entering the blood, while the remainder simply passes through the gastro-intestinal tract inabsorbed.

References 8

## CASE A) - ORAL INJECTION, MULTIPLE DOSES

Frally, consideration is made of the Miltple Oral Dosage Regimen. Again, a fixed (oral) dose is administered over equally spaced time periods.

#### ASSUMPTIONS:

- 1) All the general assumptions apply
- 2) All the assumptions from case 3) apply
- 3) Similarly from Case 2, "The principle of superposition assumes that early doses of drug do not affect the pharmacokinetics of subsequent doses. Therefore, the blood levels after the second, third or it dose will overlay or super impose he blood level attained after the (1-1)th close."
- A) To avoid complications, assume that there is no drug left in the gut whom a new dose is taken. }?

Note that there is no need to consider the drug levels in the gut on the amount of drug eliminated. This multiple closage case will only consider the effect of the amount of drug in the blood.

#### Let:

Ke-be the dray elimination constant, Ke 20
Ka-the dray absorption constant, Ka 20
Co-the mitial desage amount, 6>0
n-be the desage number n=1
T-be the provided of time between closes.
t-be time, to-0

Cn(t) - be the total amount of drug in the compartment at time to after dose n Fn(t) - be the residual dosage after dose rember n+1, 17(to) =0. The rak of change of the amount of dray on the blood, as given on case 3 is:

$$\frac{d(A)}{dt} = K_a L_i(A) - K_c(A) , \quad C(O) = C_O$$

where G(t) is the amount of drug being absorbed.

$$C(t) = \frac{K_a G_o}{(-K_a + K_e)} \left( e^{-K_a t} - e^{-K_e t} \right)$$

Now at  $t_0=0$  the mitial dose is taken (i.e. n=1) and and  $R(t_0)=0$ , by assumption

$$C_1 = C(0) = G(T_1) = 0$$
,  $R_0 = 0$ 

at IT: 
$$R_1 = \frac{k_a G_o}{(E_a + k_e)} \left( e^{-k_a T} - e^{-k_e t} \right)$$

at 2T: 
$$R_z = \frac{K_a G_a}{(-K_a + K_e)} \left( e^{-K_a T} - e^{-K_e T} \right) + \frac{K_a G_e}{(-K_a + K_e)} \left( e^{-K_a 2T} - e^{-K_e 2T} \right)$$

$$C_3 = C_4 + R_2$$

Notice that the amount of drug on the blood at dose i cyvals the residual amount of drug after dose I-1.

on medicata

Jan 1

The preceding situation is represented by Figure A.D.:
FIGURE (A.D.) - Multiple Oral Dosage Sketch

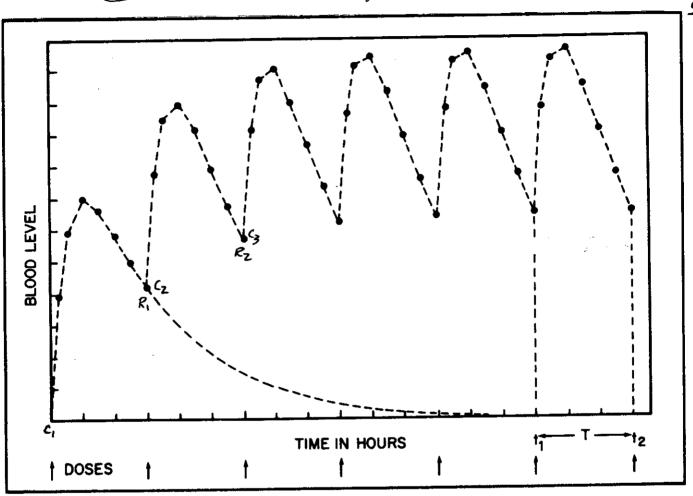


Figure 4.1. Simulated data showing blood levels after administration of multiple doses and accumulation of blood levels when equal doses are given at equal time intervals.

Thus a conjecture for Ry or Cjy is:  $R_{j} = C_{j+1} = \frac{K_{a}(o) \left(e^{-K_{a}T} + e^{-Z_{k}T} + e^{-J_{k}K_{a}T} - e^{-K_{a}T} - e^{-Z_{k}T} - e^{-Z_{k}T}}{K_{a}(e^{-K_{a}T} + e^{-Z_{k}T} + e^{-Z_{k}T} - e^{-Z_{$ 



which gives the Residual amount of drug for the end of the 1th ported, or equivalently, gives the total amount of drug at the beginning of the Orl) the period.

Similarly for any time to, such that pt = (1) to (1e a time between the fith and (pri)th intervals)

Notice that this gives the amount of day for any time to, and closage number n.

Now consider, when n gets very large (ie n >0) From previous experience, a steady-state" will result:

which gives the "steady-state" drug amount for any time to, and period To

Since this limit Co Fluctuates " as absorption and Quelman elimination occur as timerceses, there is a Maximum C and a Maximum C and a Mormon C which represent the upper & lower bounds that Co approaches in steady-state.

# Determing Com

At the start of a period, t=T, by assumption there is no absorption occurring. Hence the absorption part of the equation is effectively eliminated:

# Determining Com

To determine the opportuned for the steddy state" Ora! this is proper to the proper to the mould Regimen, recall from CASE 3 that the maximum amount present occurred at time:

cencl nT < tmax = (n+1)T.

Sonce this thun represents the peak of the day amount level, it occurs with respect to the first derivative of co:



which is our single dose case, thus

$$d(3) = \frac{d}{dt} \left( \frac{K_a C_o}{K_a + k_e} \left( e^{-K_a T} + e^{-Z_a T} - e^{-K_e T} - e^{-K_e T} \right) \right)$$

$$= \frac{d}{dt} \left( \frac{K_a C_o}{K_a + k_e} \left( e^{-K_a T} \left( 1 + e^{-K_a T} \right) - e^{-K_e T} \left( 1 + e^{-K_e T} \right) \right)$$

$$= \frac{K_a C_o}{-K_a + K_e} \left( \frac{-K_a T}{K_a + K_e} - \frac{2K_a T}{K_e} + K_e e^{-K_e T} + 2K_e e^{2K_e T} \right)$$

t is max when de has a critical point (re de =0 or Undermad) Hene: -Kae-KaT-Zkae-Zkat + Kee-Ket + Zkee-Zket =0

Kee-ket + Zke ettet = Kae kat + Zkaetat

based on the above caralysis, a conjecture for that disage number no

$$= \frac{t^{n}}{-k_{0} \cdot k_{0}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t} \cdot e^{-k_{0} \cdot t} \cdot k_{0}} \frac{l_{1} \cdot e^{-k_{0} \cdot t} \cdot k_{0} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t} \cdot k_{0}}$$

$$= \frac{l_{1} \cdot k_{0} \cdot k_{0}}{k_{0} \cdot k_{0} \cdot k_{0} \cdot k_{0}} \frac{l_{1} \cdot e^{-k_{0} \cdot t}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot e^{-k_{0} \cdot t}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot e^{-k_{0} \cdot t}}{l_{1} \cdot e^{-k_{0} \cdot t}}$$

$$= \frac{l_{1} \cdot k_{0} \cdot k_{0}}{k_{0} \cdot k_{0} \cdot k_{0}} \frac{l_{1} \cdot e^{-k_{0} \cdot t}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot e^{-k_{0} \cdot t}}} \frac{l_{1} \cdot k_{0} \cdot k_{0}}{l_{1} \cdot k_{0} \cdot k_{0}}}{l_{1} \cdot k_{0} \cdot k_{0}}}$$

Plugging this value into, the equation for COD to Find Comey o

$$=\frac{k_{a}C_{o}}{-k_{a}k_{e}}\left(\frac{k_{e}\cdot l\cdot e^{-k_{a}T}}{k_{a}k_{e}} + \frac{k_{e}}{k_{a}} \cdot \frac{k_{e}}{l\cdot e^{-k_{e}T}} + \frac{k_{e}}{k_{a}} + \frac{k_{e}}{l\cdot e^{-k_{e}T}} + \frac{k_{e}}{k_{a}} + \frac{k_{e}}{l\cdot e^{-k_{e}T}} + \frac{k_{$$

$$=\frac{k_{a}C_{o}}{-k_{a}+k_{e}}\left(\frac{k_{e}\cdot l-e^{-k_{a}T}}{k_{a}+k_{e}}\frac{t_{a}+k_{e}}{(l-e^{-k_{e}T})-(l-e^{-k_{a}T})}\right)$$

$$=\frac{k_{a}C_{o}}{-k_{a}+k_{e}}\left(\frac{k_{e}\cdot l-e^{-k_{a}T}}{(l-e^{-k_{a}T})(l-e^{-k_{e}T})}\right)$$

This CMAX is the upper limit that miltiple Oral dese regimen reaches, for a constant dosage amount over a constant time period.

## Observations:

- D Like the Multiple Rapid Intravenous Injection case, This model, in time, reaches a "steady-state" where limits earst for the upper & lower bounds of the dwg amount in the blood.
- 2) That when the drug Supply terminates, the model tollows a natural Malthusian decay.
- 3) As in Case (2) a change in the Time period

  To causes a shift in the limits of

  The Steady-state as shown:





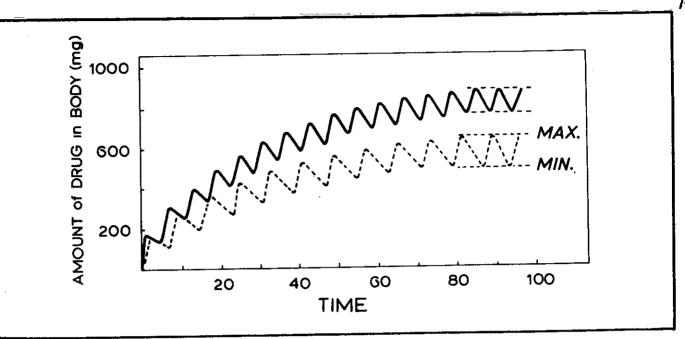


Figure 4.2 Amount of drug in the body as a function of time. Equal doses of drug were given every 6 hr (upper curve) and every 8 hr (lower curve).  $K_a$  and K remain constant.

### CONCLUSIONS - CASE (F)

The multiple Oral Drug desage Model provides good Theoretical results of the Drug Supply in the body. However upon application of the Model attention must be given to desage amount and period between desages to provide the Satest and must effective drug regimen. (i.e. MTC can never be exactly known) Thorefore leeway must be given so as to not cause an overlesse.

Short comings of this model are Much the same as Case (2).

Loading Doses or an effective "Waking Hour" regimen

may be necessary to provide sufficient Residual Concentration.

Therefore Model revision may be necessary. As well, the

short comings of case (3) are magnified here, as

Multiple desages are considered.



- 2. This problem deals with simple compartment models in physiology. See D. S. Riggs (1963) for further discussion, especially his Sec. 6-14 which treats problems of fitting curves to such models.
  - (a) Treat the blood as a compartment containing a substance being removed by a physiological mechanism. What sort of equations could describe the concentration of the substance as a function of time? We need simple models. How can they be tested?
  - (b) Let's be specific and assume that the removal is being done by the kidneys. In this case the rate of removal is usually proportional to the amount of the substance passing through a kidney per unit time. Construct a simple model based on concentrations.
  - (c) The substance in (b) is a drug whose concentration should lie between 2 and 5 milligrams per 100 cubic centimeters. If the drug is taken internally, about 60% is quickly absorbed and most of the remainder is lost. In about 8 hours the body of an average person eliminates about 50% of the drug. A normal adult has about 5 liters of blood. Design a dosage program for the drug.
  - (d) Most drugs are taken orally and require time to be absorbed by the blood. At the same time the drug is being removed by the kidneys. Model the situation. Here is some data on drugs taken from J. V. Swintosky (1956). The first drug is sulfapyridine, and the second is sodium salicylate. An O indicates oral administration. and an I indicates intravenous administration [to which (a) should apply]. The column headed "grams" gives the initial dosage, and the other columns indicate the concentration in the blood at various times after administration. How well does your model fit? Could you explain any discrepancies?

Concentration (milligrams/cubic centimeters)

Administration									
	Grams	l hour	2 hours	4 hours	6 hours	8 hours	10 hours	12 hours	24 hours
0	4.0	2.3	2.7	3.6	3.0		2.0		
O	4.0	1.8	2.8	3.9	3.5	2.6	2.2	_	
1	1.8	3.8	3.4	2.6	2.1		_	_	
I	1.8	3.7	3.3	2.7	2.3	.—		-	_
0	10	5.0			14.4	_	_	15.7	12.5
Ĭ	10	39.4	_		31.4		_	24.2	16.2
i	20	56.7	_		43.0	_		35.2	26.6

Unfortunately, here No explicitly given Ka or Ke 15 provided here, on (c) the elimination constants are to be calculated, but they assume that only point of the drug is absorbed, which is a complication of My Simpler Medels

#### FOOT NOTES

Leon Shorgel and Ardrew B.C. Yu, Applied Bio-Phorma Centres and Phormacokmetics (Norwalk: Appleton - Century -Crofts, 1985), pp. 37-39.

Frank R. Giordano and Maurice D. Weir, A First Course In Mathe Matical Modeling (Menterey: Brooks/Cole, 1985), pp. 316-318.

3 Shargel , p. 229.

4 Giordano, p. 319.

<sup>5</sup>T.G. Berry, "Test Solutions," 6:337, February ZZ, 1990, p. 6,7.

6 Giordono, pp. 319-322.

7 Shorgel , p. 106.

8 Shurgel , pp. 107-109.

9 Shargel, p. 230.

" Shargel, p. 232.

" Shorgel, pp. 237-240

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