Optimal gap with locality