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**Algorithm 1:**  $\alpha$ -StackSort

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1 def alpha_stack_sort(t):
2    $\mathcal{X} \leftarrow \emptyset$ 
3    $n \leftarrow \text{len}(t)$ 
4    $i \leftarrow 0$ 
5   while  $i < n$  do
6      $R = (\text{start}, \text{end}, \text{is\_increasing}) \leftarrow \text{run\_detect}(t, i, n)$ 
7     if not is_increasing then
8        $t[\text{start} : \text{end} + 1] \leftarrow t[\text{start} : \text{end} + 1][::-1]$ 
9        $\mathcal{X} \leftarrow \mathcal{X} + R$ 
10       $\mu(t, \mathcal{X})$ 
11       $i \leftarrow \text{end} + 1$ 
12   while  $\text{Card}(\mathcal{X}) \geq 1$  do
13      $R_1 = (\text{start}_1, \text{end}_1, \text{is\_increasing}_1) \leftarrow \mathcal{X}.\text{pop}()$ 
14      $R_2 = (\text{start}_2, \text{end}_2, \text{is\_increasing}_2) \leftarrow \mathcal{X}.\text{pop}()$ 
15      $\mathcal{X} \leftarrow \mathcal{X} + R_1 \oplus R_2$ 
16      $\text{merge}(t, \text{start}_1, \text{end}_1 + 1, \text{end}_2 + 1)$ 
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