

Drug Diffusion in Biological Tissues: Mathematical Analysis and Numerical Simulation

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1 Introduction

Présentation du problème étudié, motivation biomédicale, objectifs du rapport.

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2.2 Biomedical Applications

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3.2 Mathematical Structure

3.3 Simplified Analytical Solution

3.4 Physical Interpretation of the Solution

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6.1 Summary of Results

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References

References

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