

assume $i \neq 0$ (interesting case):

$$\dot{i} = 0 \Rightarrow s = \frac{\alpha+b}{\beta},$$

$$\dot{s} = 0 \Rightarrow i = \frac{b(1-x)-bs}{\beta s} = \frac{b(1-x)}{\beta \frac{\alpha+b}{\beta}} - \frac{b}{\beta}$$

$$i = i(x) = \frac{b}{\alpha+b}(1-x) - \frac{b}{\beta} \text{ (affine-linear in x!)}$$

$$\phi(x) = x + n + ai(x), \eta(x) = 1 - x + n + \Omega, \phi(x), \eta(x) : \text{linear}$$

Idee

1. Lokalisiere Sattel-Knoten oder Pitchfork
2. Versuche weitere Bedingungen zu finden, dass $\pm i\omega$ EW sind
3. x erfüllt Polynom 3.Ordnung: $\mu x \theta_Y \eta(x) (\theta_X \phi(x) + \eta(x)) = \mu(1-x) \theta_X \phi(x) (\phi(x) + \theta_Y \eta(x))$
 $\Rightarrow p(x) = 0, \text{grad}(p) = 3$
4. **Saddle-node**: doppelte Nullstellen! $p'(x) = 0$
5. $p(x) = 0, p'(x) = 0 \xrightarrow{\text{Lineare Gleichung}} x = x^* = \dots$
 $\xRightarrow{\text{Einsetzen}} p(x^*) = 0, p'(x^*) = 0 \leftarrow \text{Bedingungen an Parameter}$