References

- [ABLS20] Ayah Almousa, Juliette Bruce, Michael Loper, and Mahrud Sayrafi, *The virtual resolutions package for Macaulay2*, J. Softw. Algebra Geom. **10** (2020), no. 1, 51–60.
- [AFP⁺19] Marian Aprodu, Gavrill Farkas, Ştefan Papadima, Claudiu Raicu, and Jerzy Weyman, Koszul modules and Green's conjecture, Inventiones mathematicae (2019).
 - [AF11] Marian Aprodu and Gavril Farkas, Green's conjecture for curves on arbitrary K3 surfaces, Compos. Math. 147 (2011), no. 3, 839–851.
 - [BE91] Dave Bayer and David Eisenbud, *Graph curves*, Adv. Math. **86** (1991), no. 1, 1–40. With an appendix by Sung Won Park.
 - [BEL91] Aaron Bertram, Lawrence Ein, and Robert Lazarsfeld, Vanishing theorems, a theorem of Severi, and the equations defining projective varieties, J. Amer. Math. Soc. 4 (1991), no. 3, 587–602.
 - [BES20] Christine Berkesch, Daniel Erman, and Gregory G. Smith, Virtual resolutions for a product of projective spaces, Algebr. Geom. 7 (2020), no. 4, 460–481, DOI 10.14231/ag-2020-013. MR4156411
- [BBC⁺22] Madeline Brandt, Juliette Bruce, Melody Chan, Margarida Melo, Gwyneth Moreland, and Corey Wolfe, On the top-weight rational cohomology of A_q , Geometry & Topology (2022). to appear.
 - [BE22] Michael K. Brown and Daniel Erman, *Tate resolutions on toric varietie* (2022). Pre-print: arxiv:2108.03345.
 - [BE23a] _____, Linear syzygies of curves in weighted projective space (2023). Pre-print: arxiv:2301.0915.
 - [BE23b] _____, A short proof of the Hanlon-Hicks-Lazarev Theorem (2023). Pre-print: arxiv:2303.14319.
- [BEGY20] Juliette Bruce, Daniel Erman, Steve Goldstein, and Jay Yang, Conjectures and computations about Veronese syzygies, Exp. Math. 29 (2020), no. 4, 398–413.
- [BEGY21] _____, The Schur-Veronese package in Macaulay2, J. Softw. Algebra Geom. 11 (2021), no. 1, 83–87.
 - [Bru19] Juliette Bruce, Asymptotic syzygies in the setting of semi-ample growth (2019). Pre-print: arxiv:1904.04944.
 - [Bru22] _____, The quantitative behavior of asymptotic syzygies for Hirzebruch surfaces, J. Commut. Algebra 14 (2022), no. 1, 19–26.
- [BCE⁺22] Juliette Bruce, Daniel Corey, Daniel Erman, Steve Goldstein, Robert P. Laudone, and Jay Yang, Syzygies of $\mathbb{P}^1 \times \mathbb{P}^1$: data and conjectures, J. Algebra **593** (2022), 589–621.
- [BCHS21] Juliette Bruce, Lauren Cranton Heller, and Mahrud Sayrafi, Characterizing Multigraded Regularity on Products of Projective Spaces (2021). Pre-print: arxiv:2110.10705.
- [BCHS22] _____, Bounds on Multigraded Regularity (2022). Pre-print: arxiv:2208.11115.
 - [BB21] Weronika Buczyńska and Jarosław Buczyński, Apolarity, border rank, and multigraded Hilbert scheme, Duke Math. J. 170 (2021), no. 16, 3659–3702.
- [CEVV09] Dustin A. Cartwright, Daniel Erman, Mauricio Velasco, and Bianca Viray, *Hilbert schemes of 8 points*, Algebra Number Theory **3** (2009), no. 7, 763–795.
 - [CGP21] Melody Chan, Søren Galatius, and Sam Payne, Tropical curves, graph complexes, and top weight cohomology of \mathcal{M}_q , J. Amer. Math. Soc. **34** (2021), no. 2, 565–594.
 - [Cha97] Karen A. Chandler, Regularity of the powers of an ideal, Comm. Algebra 25 (1997), no. 12, 3773–3776.
 - [Cox95] David A. Cox, The homogeneous coordinate ring of a toric variety, J. Algebraic Geom. 4 (1995), no. 1, 17–50. MR1299003
 - [CHT99] S. Dale Cutkosky, Jürgen Herzog, and Ngô Viêt Trung, Asymptotic behaviour of the Castelnuovo-Mumford regularity, Compositio Mathematica 118 (1999), no. 3, 243–261.
 - [EL93] Lawrence Ein and Robert Lazarsfeld, Syzygies and Koszul cohomology of smooth projective varieties of arbitrary dimension, Invent. Math. 111 (1993), no. 1, 51–67.
 - [EL12] _____, Asymptotic syzygies of algebraic varieties, Invent. Math. 190 (2012), no. 3, 603–646.
 - [EES15] David Eisenbud, Daniel Erman, and Frank-Olaf Schreyer, Tate resolutions for products of projective spaces, Acta Math. Vietnam. 40 (2015), no. 1, 5–36, DOI 10.1007/s40306-015-0126-z. MR3331930
 - [EG84] David Eisenbud and Shiro Goto, Linear free resolutions and minimal multiplicity, J. Algebra 88 (1984), no. 1, 89–133.

- [Eis05] David Eisenbud, *The geometry of syzygies*, Graduate Texts in Mathematics, vol. 229, Springer-Verlag, New York, 2005. A second course in commutative algebra and algebraic geometry.
- [EY18] Daniel Erman and Jay Yang, Random flag complexes and asymptotic syzygies, Algebra Number Theory 12 (2018), no. 9, 2151–2166.
- [GVT15] Elena Guardo and Adam Van Tuyl, Arithmetically Cohen-Macaulay sets of points in $\mathbb{P}^1 \times \mathbb{P}^1$, SpringerBriefs in Mathematics, Springer, Cham, 2015. MR3443335
 - [FP05] Gavril Farkas and Mihnea Popa, Effective divisors on $\overline{\mathcal{M}}_g$, curves on K3 surfaces, and the slope conjecture, J. Algebraic Geom. 14 (2005), no. 2, 241–267.
 - [Far06] Gavril Farkas, Syzygies of curves and the effective cone of $\overline{\mathcal{M}}_g$, Duke Math. J. **135** (2006), no. 1, 53–98.
 - [FK16] Gavril Farkas and Michael Kemeny, *The generic Green-Lazarsfeld secant conjecture*, Invent. Math. **203** (2016), no. 1, 265–301.
 - [FK17] _____, The Prym-Green conjecture for torsion line bundles of high order, Duke Math. J. **166** (2017), no. 6, 1103–1124.
- [GLL15] Ofer Gabber, Qing Liu, and Dino Lorenzini, Hypersurfaces in projective schemes and a moving lemma, Duke Math. J. **164** (2015), no. 7, 1187–1270.
- [Gre84a] Mark L. Green, Koszul cohomology and the geometry of projective varieties, J. Differential Geom. 19 (1984), no. 1, 125–171.
- [Gre84b] _____, Koszul cohomology and the geometry of projective varieties. II, J. Differential Geom. 20 (1984), no. 1, 279–289.
- [HHL23] Andrew Hanlon, Jeff Hicks, and Oleg Lazarev, Resolutions of toric subvarieties by line bundles and applications (2023). Pre-print: arxiv:2303.03763.
- [Kod00] Vijay Kodiyalam, Asymptotic behaviour of Castelnuovo-Mumford regularity, Proc. Amer. Math. Soc. 128 (2000), no. 2, 407–411.
- [Kon93] Maxim Kontsevich, Formal (non)commutative symplectic geometry, The Gelfand Mathematical Seminars, 1990–1992, Birkhäuser Boston, Boston, MA, 1993, pp. 173–187.
- [Kon94] _____, Feynman diagrams and low-dimensional topology, First European Congress of Mathematics, Vol. II (Paris, 1992), Progr. Math., vol. 120, Birkhäuser, Basel, 1994, pp. 97–121.
- [LPP11] Robert Lazarsfeld, Giuseppe Pareschi, and Mihnea Popa, Local positivity, multiplier ideals, and syzygies of abelian varieties, Algebra Number Theory 5 (2011), no. 2, 185–196.
- [Lem18] Alexander Lemmens, On the n-th row of the graded Betti table of an n-dimensional toric variety, J. Algebraic Combin. 47 (2018), no. 4, 561–584.
 - [M2] Daniel R. Grayson and Michael E. Stillman, Macaulay 2, a software system for research in algebraic geometry. Available at http://www.math.uiuc.edu/Macaulay2/.
- [MS05] Diane Maclagan and Gregory G. Smith, *Uniform bounds on multigraded regularity*, J. Algebraic Geom. **14** (2005), no. 1, 137–164.
- [MS04] _____, Multigraded Castelnuovo-Mumford regularity, J. Reine Angew. Math. **571** (2004), 179–212.
- [Mum70] David Mumford, Varieties defined by quadratic equations, Questions on Algebraic Varieties (C.I.M.E., III Ciclo, Varenna, 1969), Edizioni Cremonese, Rome, 1970, pp. 29–100.
- [Mum66] D. Mumford, On the equations defining abelian varieties. I, Invent. Math. 1 (1966), 287–354.
 - [OP01] Giorgio Ottaviani and Raffaella Paoletti, Syzygies of Veronese embeddings, Compositio Math. **125** (2001), no. 1, 31–37.
 - [Par00] Giuseppe Pareschi, Syzygies of abelian varieties, J. Amer. Math. Soc. 13 (2000), no. 3, 651–664.
 - [PP03] Giuseppe Pareschi and Mihnea Popa, Regularity on abelian varieties. I, J. Amer. Math. Soc. 16 (2003), no. 2, 285–302.
 - [PP04] _____, Regularity on abelian varieties. II. Basic results on linear series and defining equations, J. Algebraic Geom. 13 (2004), no. 1, 167–193.
 - [Sch86] Frank-Olaf Schreyer, Syzygies of canonical curves and special linear series, Math. Ann. 275 (1986), no. 1, 105–137.
 - [Voi02] Claire Voisin, Green's generic syzygy conjecture for curves of even genus lying on a K3 surface, J. Eur. Math. Soc. (JEMS) 4 (2002), no. 4, 363–404.

- [Voi05] _____, Green's canonical syzygy conjecture for generic curves of odd genus, Compos. Math. 141 (2005), no. 5, 1163–1190.
- [Wil15] Thomas Willwacher, M. Kontsevich's graph complex and the Grothendieck-Teichmüller Lie algebra, Invent. Math. 200 (2015), no. 3, 671–760, DOI 10.1007/s00222-014-0528-x. MR3348138