

# Heterogeneous Innovation and Intertemporal Productivity Choice

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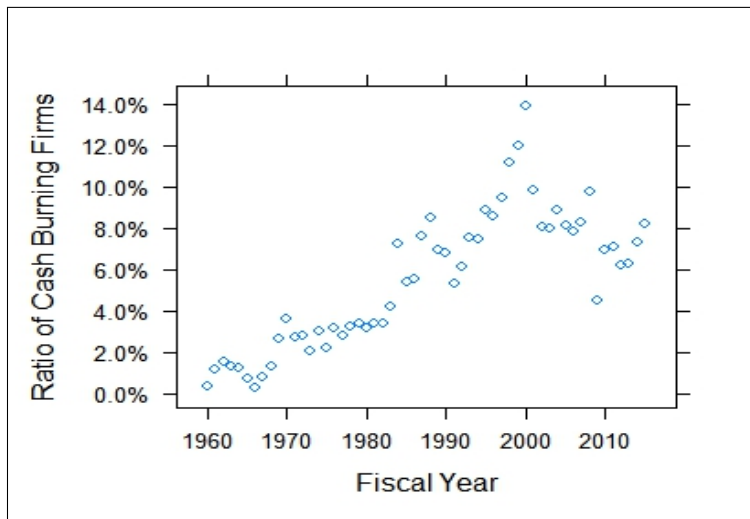
# Research Motivation

Since the rebirth of endogenous growth in mid-2000s, literature became richer:

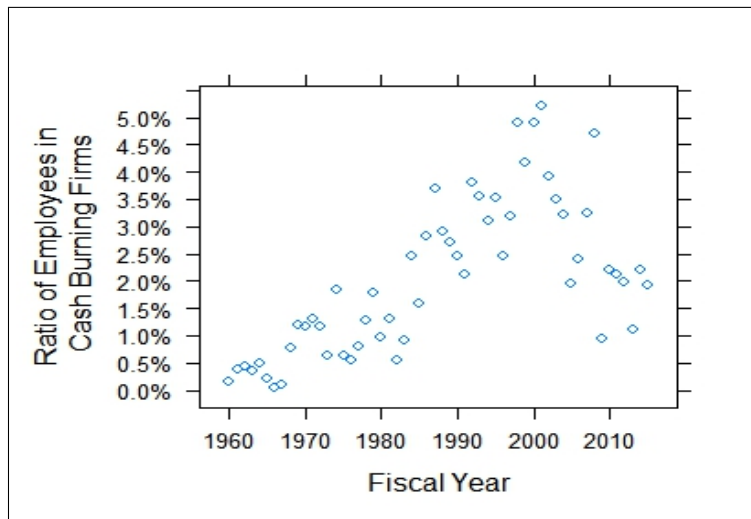
- Classics: Romer (1990), Grossman and Helpman (1991), Aghion and Howitt (1992);
- Micro-data renewal: Klette and Kortum (2004), Lentz and Mortensen (2008);
- Current state of the art: Acemoglu et al. (2013), Akcigit and Kerr (2016).

⇒ We now account for creative destruction/turnover, R&D spillover, imitation, incumbents' innovation, firm heterogeneity...but...

# Research Motivation



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## Questions:

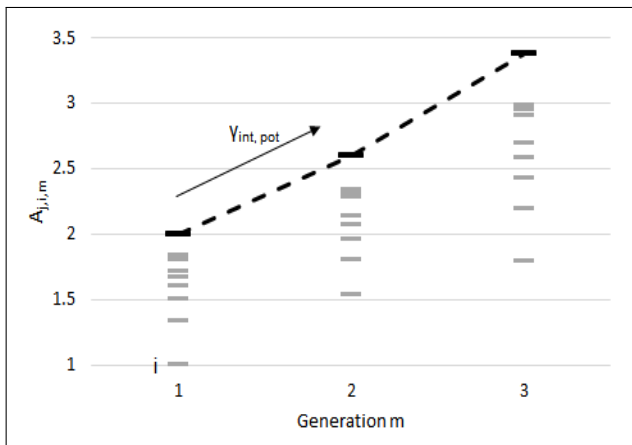
- What's the impact of intertemporal TFP choice on aggregate TFP?
- What are the implications to the innovation strategy of firms?
- How long does it take to "get TFP back"?

## Why is it interesting?

- Having Bluetooth in your car  $\neq$  Tesla, or innovation heterogeneity sparks different firm behavior;
- Less TFP now for more TFP latter could impact aggregate measurement;
- Finance has a role in "footing the bill" and reallocation;
- Normative: how to spur abrupt innovation?

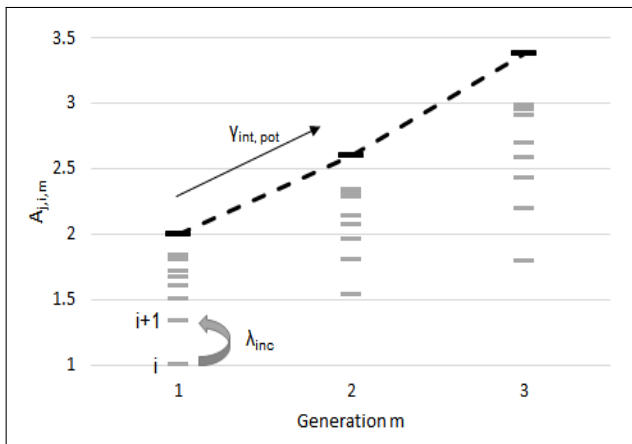
# Framework - Innovation

**Focus:** Innovation: internal (incremental or abrupt), external, and entrants (the last two only abrupt).



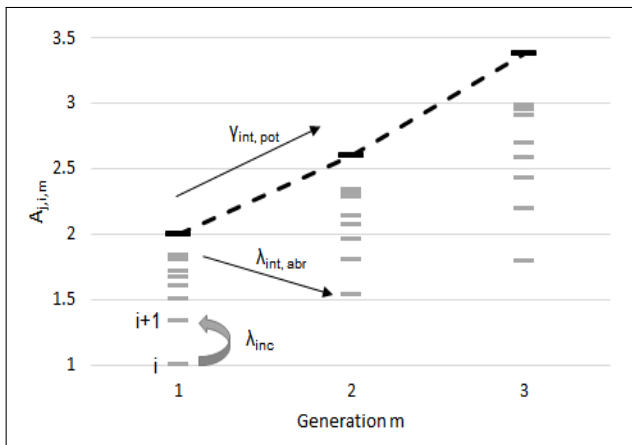
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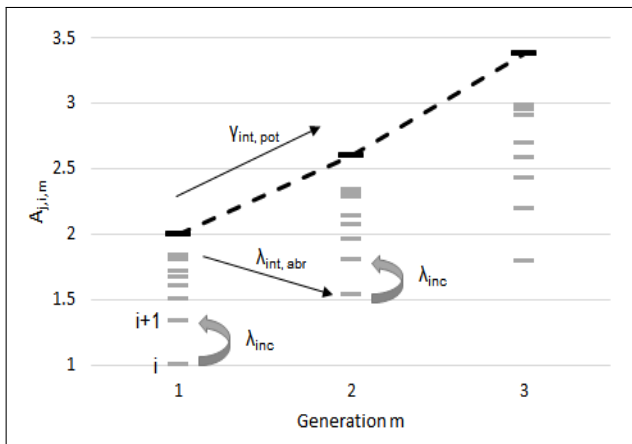
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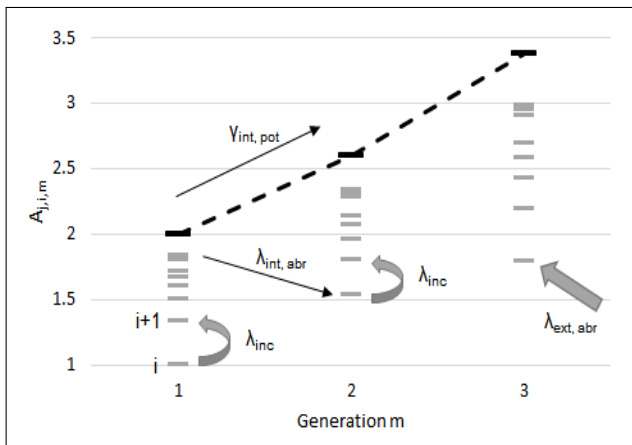
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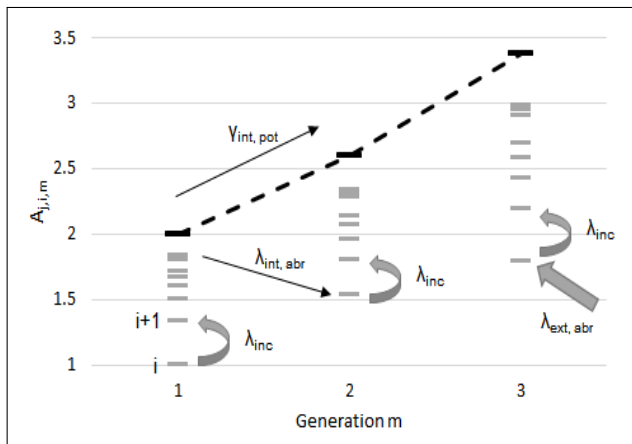
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# Framework - Innovation

- Law of motion:

$$A_{t+\Delta t} = \begin{cases} A_m(1 + \alpha^s), \lambda_{inc}\Delta t, \alpha \in (0, 1), s \in \{1, 2, \dots\} \\ A_t\gamma_{int,abr}, \lambda_{int,abr}\Delta t \\ A_t, [1 - \lambda_{inc}\Delta t; 1 - \lambda_{int,abr}\Delta t] \end{cases}$$

- Incremental R&D cost:  $\psi_{inc}(\lambda_{inc}, A_t) = \xi_j A_t \lambda_{inc}^\eta$
- Catching-up: laggards pay  $\psi_{inc}(\lambda_{inc}, A_t)$  and get an arrival  $\lambda_{inc} + h$ ;
- Abrupt R&D cost (for  $n_p > 0$ ):  $\psi_{abr}(\lambda_{ext,abr}, \bar{A}_t) = \xi_j \bar{A}_t \lambda_{ext,abr}^\eta$ ,  $\bar{A}_t$  sector average;
- Cournot competition: profits  $\pi_t$  scale with  $\frac{A_{j,i,m}}{\sum_j A_{j,i,m}}$  within an industry.

# Framework - Innovation

Outside entrepreneur:

- Value function:

$$rV_0 - \dot{V}_0 = \max_{\lambda_{ext,abr}} [\lambda_{ext,abr} [E_j[V(A_{t,m+1})] - V_0] - v\bar{A}_t\lambda_{ext,abr}]$$

- Cost:  $C_E(\lambda_{ext,abr}, \bar{A}_t) = v\bar{A}_t\lambda_{ext,abr}$ ,  $v$  a constant;
- Free entry condition:  $E_j[V(A_{t,m+1})] = v\bar{A}_t$
- $\Rightarrow$  Each firm faces an aggregate endogenous creative destruction (CD) of rate  $\tau_{CE}$  and internal competition rate  $\tau_I$ .

# Framework - Innovation

Incumbents:

- Value function:  $rV(A_t) - \dot{V}(A_t) =$

$$\max_{\substack{\lambda_{inc}, \lambda_{int,abr} \\ \lambda_{ext,abr}}} \left[ \sum_k^{n_{j,p}} \left[ \begin{aligned} &\pi_t n_{j,p} - \{ \xi_j \lambda_{inc}^\eta A_{t,m}; \xi_j \bar{A}_t \lambda_{int,abr}^\eta \} \\ &+ \{ \lambda_{inc} [V(A_{t,m}^k \cup A_{t+\Delta t,m}^k) - V(A_{t,m})]; \\ &\lambda_{int,abr} [E_j [V(A_{t,m}^k \cup A_{t+\Delta t,m+1}^k) - V(A_{t,m})]] \} \\ &- \tau_I [V(A_{t,m} \setminus \bar{A}_{t+\Delta t,m}^k) - V(A_{t,m})] \\ &- \tau_{CE} [V(A_{t,m} \setminus \bar{A}_{t+\Delta t,m+1}^k) - V(A_{t,m})] \\ &+ \lambda_{ext,abr} [E_j [V(A_{t,m}^k \cup A_{t+\Delta t,m+1}^{k'}) - V(A_{t,m})] \\ &- \xi_j \bar{A}_t \lambda_{int,abr}^\eta - \Phi \bar{A}_t \end{aligned} \right] \right]$$

- 1<sup>st</sup>: instant returns - costs;
- 2<sup>nd</sup>, 3<sup>rd</sup>: return from int. R&D;
- 4<sup>th</sup>: internal competition;
- 5<sup>th</sup>: external CE;
- 6<sup>th</sup>: return from abr. R&D;
- 7<sup>th</sup>: Abr. R&D and fixed costs;

# Empirical Work - Patents

How to discipline  $\{\alpha, \gamma_{int,abr}, \gamma_{ext,abr}, \gamma_{int,pot}\}$ ?

- USPTO patent data (e.g. # patents, # patent citations, if it's self-citation or external...).

Model (complete):

- Endogenous: R&D, productivity (all parameters);
- Exogenous: labor market (wages, supply), consumers (discounting), mass of entrants;
- Estimated (for Patents):  $\{\alpha, \gamma_{int,abr}, \gamma_{ext,abr}, \gamma_{int,pot}\}$ ;
- Calibrated (for Complete version): discounting, curvature of the R&D cost function ( $\eta$ );

# Empirical Work - Patents

Estimation strategy:

- Patent and citation distribution: invariant (at SS);
- Need to discipline patent arrival and quality ladder;
- Find the "decay rate" of patent quality;
- Distinguish external vs. internal (type of citation), abrupt vs. incremental (# of citations);
- Generational productivity step: impose the same shape and compare absolute levels ("envelope").



# Conclusion

- Goal: estimate the R&D part of an endogenous growth model with heterogeneous innovation;
- Possibilities:
  - Add firm-level financials and estimate the parameters of the Partial Equilibrium (indirect inference);
  - Solve the SS;
  - Cure cancer...
- Caveats: lots of firms don't innovate, patents do not represent innovation (nor products, ideally we would have product-level data).

# References

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