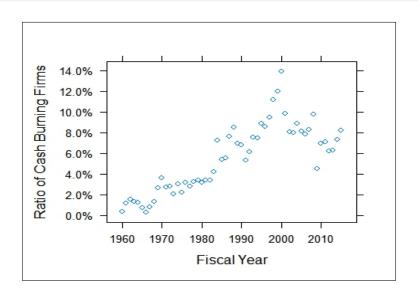
# Heterogeneous Innovation and Intertemporal Productivity Choice

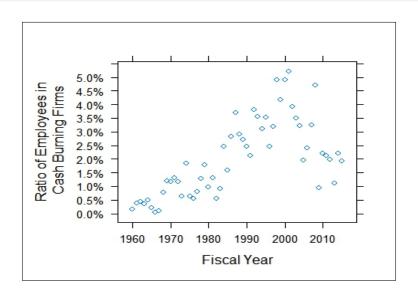
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Since the rebirth of endogenous growth in mid-2000s, literature became richer:

- Classics: Romer (1990), Grossman and Helpman (1991), Aghion and Howitt (1992);
- Micro-data renewal: Klette and Kortum (2004), Lentz and Mortensen (2008);
- Current state of the art: Acemoglu et al. (2013), Akcigit and Kerr (2016).
- $\Rightarrow$  We now account for creative destruction/turnover, R&D spillover, imitation, incumbents' innovation, firm heterogeneity...but...



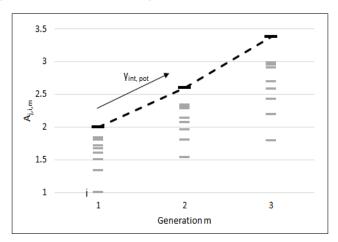


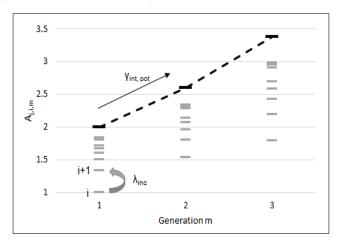
#### **Questions:**

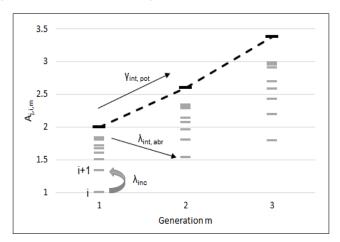
- What's the impact of intertemporal TFP choice on aggregate TFP?
- What are the implications to the innovation strategy of firms?
- How long does it take to "get TFP back"?

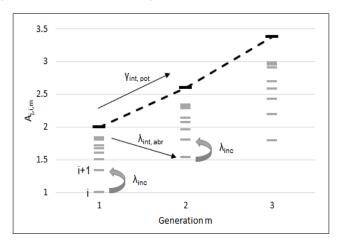
#### Why is it interesting?

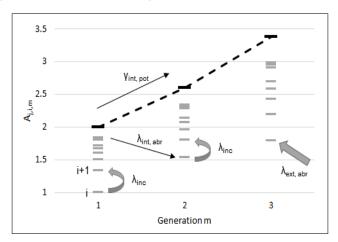
- Having Bluetooth in your car ≠ Tesla, or innovation heterogeneity sparks different firm behavior;
- Less TFP now for more TFP latter could impact aggregate measurement;
- Finance has a role in "footing the bill" and reallocation;
- Normative: how to spur abrupt innovation?

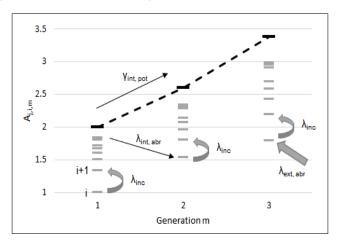












• Law of motion  $(A_{m+1} = A_m \gamma_{int,pot})$ :

$$A_{t+\Delta t} = \begin{cases} A_{m}(1-\alpha^{s}) , \ \lambda_{inc}\Delta t , \ \alpha \in (0,1) , & s \in \{1,2,...\} \\ A_{t}\gamma_{int,abr} , \ \lambda_{int,abr}\Delta t \\ A_{t} , \ \left[1-\lambda_{inc}\Delta t ; 1-\lambda_{int,abr}\Delta t\right] \end{cases}$$

- Incremental R&D cost:  $\psi_{inc}(\lambda_{inc}, A_t) = \xi_j A_t \lambda_{inc}^{\eta}$
- Catching-up: laggards pay  $\psi_{inc}(\lambda_{inc}, A_t)$  and get an arrival  $\lambda_{inc} + h$ ;
- Abrupt R&D cost (for  $n_p>0$ ):  $\psi_{abr}(\lambda_{ext,abr},\bar{A}_t)=\xi_j\bar{A}_t\lambda_{ext,abr}^\eta$ ,  $\bar{A}_t$  sector average;
- Cournot competition: profits  $\pi_t$  scale with  $\frac{A_{j,i,m}}{\sum_i A_{j,i,m}}$  within an industry.

## **Empirical Work - Patents**

How to discipline  $\{\alpha, \gamma_{int,abr}, \gamma_{ext,abr}, \gamma_{int,pot}\}$ ?

• USPTO patent data (e.g. # patents, # patent citations, if it's self-citation or external...).

#### Model (complete):

- Endogenous: R&D, productivity (all parameters);
- Exogenous: labor market (wages, supply), consumers (discounting), mass of entrants;
- Estimated (for Patents):  $\{\alpha, \gamma_{int,abr}, \gamma_{ext,abr}, \gamma_{int,pot}\};$
- Calibrated (for Complete version): discounting, curvature of the R&D cost function  $(\eta)$ ;

## **Empirical Work - Patents**

#### Estimation strategy:

- Patent and citation distribution: invariant (at SS);
- Need to discipline patent arrival and quality ladder;
- Find the "decay rate" of patent quality;
- Distinguish external vs. internal (patent classification or type of citation, could do robustness), abrupt vs. incremental (# of citations);
- Generational productivity step: impose the same shape and compare absolute levels ("envelope").

#### Conclusion

- Goal: estimate the R&D part of an endogenous growth model with heterogeneous innovation;
- Possibilities:
  - Add firm-level financials and estimate the parameters of the Partial Equilibrium (indirect inference);
  - Solve the SS;
  - Cure cancer...
- Caveats: lots of firms don't innovate, patents do not represent innovation (nor products, ideally we would have product-level data).

#### References

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- [2] AKCIGIT, U., AND KERR, W. R. Growth through heterogeneous innovations. forthcoming, 2016.
- [3] GROSSMAN, G. M., AND HELPMAN, E. Quality ladders in the theory of growth. *Review of Economic Studies 58*, 1 (1991), 43–61.
- [4] KLETTE, T. J., AND KORTUM, S. Innovating firms and aggregate innovation. *Journal of Political Economy 112*, 5 (2004), 986–1018.
- [5] PHILIPPE AGHION, C. H. P. H., AND VICKERS, J. Competition, imitation and growth with step-by-step innovation. *Review of Economic Studies 68*, 3 (2001), 467–492.
- [6] ROMER, P. Endogenous technological change. *Journal of Political Economy 98*, 5 (1990), S71–102.

## Appendix: Framework - Innovation

#### Outside entrepreneur:

Value function:

$$rV_0 - \dot{V}_0 = \max_{\lambda_{\text{ext,abr}}} \left[ \lambda_{\text{ext,abr}} \left[ E_j \left[ V(A_{t,m+1}) \right] - V_0 \right] - v \bar{A}_t \lambda_{\text{ext,abr}} \right]$$

- Cost:  $C_E(\lambda_{ext,abr}, \bar{A}_t) = v\bar{A}_t\lambda_{ext,abr}$ , v a constant;
- ullet Free entry condition:  $E_jig[V(A_{t,m+1})ig]=var{A}_t$
- $\Rightarrow$  Each firm faces an aggregate endogenous creative destruction (CD) of rate  $\tau_{CE}$  and internal competition rate  $\tau_{I}$ .

## Appendix: Framework - Innovation

#### Incumbents:

• Value function:  $rV(A_t) - \dot{V}(A_t) =$ 

$$\max_{\substack{\lambda_{inc}, \lambda_{int,abr} \\ \lambda_{ext,abr}}} \begin{bmatrix} \pi_t n_{j,p} - \{\xi_j \lambda_{inc}^{\eta} A_{t,m}; \xi_j \bar{A}_t \lambda_{int,abr}^{\eta} \} \\ + \{\lambda_{inc} \big[ V(A_{t,m}^{k-} \cup A_{t+\Delta t,m}^{k}) - V(A_{t,m}) \big]; \\ \lambda_{int,abr} \big[ E_j \big[ V(A_{t,m}^{k-} \cup A_{t+\Delta t,m+1}^{k}) - V(A_{t,m}) \big] \} \\ - \tau_I \big[ V(A_{t,m} \setminus \bar{A}_{t+\Delta t,m}^{k}) - V(A_{t,m}) \big] \\ - \tau_{CE} \big[ V(A_{t,m} \setminus \bar{A}_{t+\Delta t,m+1}^{k}) - V(A_{t,m}) \big] \\ + \lambda_{ext,abr} \big[ E_j \big[ V(A_{t,m}^{k} \cup A_{t+\Delta t,m+1}^{k'}) - V(A_{t,m}) \big] \\ - \xi_j \bar{A}_t \lambda_{int,abr}^{\eta} - \Phi \bar{A}_t \end{bmatrix}$$

- 1st: instant returns costs;
- 2<sup>nd</sup>, 3<sup>rd</sup>: return from int. R&D;
- 4<sup>th</sup>: internal competition;

- 5<sup>th</sup>: external CE;
- 6<sup>th</sup>: return from abr. R&D;
- 7th: Abr. R&D and fixed costs;