$$\mathbb{C}^{\text{op}} \xrightarrow{\int_{F,C}^{-1}(a)} \mathbf{Sets}$$

$$C' \qquad y(C)(C') \xrightarrow{\eta_{F,C}^{-1}(a)_{C'}} F(C')$$

$$f \uparrow \qquad y(C)(f) \uparrow \qquad \uparrow_{F,C}^{-1}(a)_{C} \\
C \qquad y(C)(C) \xrightarrow{\eta_{F,C}^{-1}(a)_{C}} F(C)$$