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Binary Tree Classifier from Scratch for Mushroom Classification

Final Project in the Subject Machine Learning

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1 Introduction

2 Tree Classifier Implementation

Tree predictors are fundamental tools in machine learning, widely applied to classification and regression tasks. They represent a hierarchy of decision rules, where data points are recursively split into subsets based on feature values. The main advantage of tree predictors is their ability to handle both numerical and categorical features. Tree predictors are also straightforward, making them a popular choice when interpretability is a priority.

In this study, a complete binary tree classifier - where each internal node has exactly two children - has been implemented in Python. A detailed description of the classes and methods created is provided below.

2.1 TreeNode Class

The TreeNode class represents a single node in a binary tree classifier. Each node can either be an internal node or a leaf node. Internal nodes split the data based on a specific feature and threshold, while leaf nodes store the predicted label. The attributes and methods of this class are designed to support the recursive structure of the tree classifier.

Attributes:

- feature_index (int or None): The feature index used for splitting the data at this node.
- threshold_value (float or None): The threshold value that determines how the data is split at this node.
- left_child (TreeNode or None): The left child node.
- right_child (TreeNode or None): The right child node.
- left_ratio (float or None): The ratio of samples that go to the left child. This value is particularly useful for handling missing values and calculating probabilities.
- leaf_value (int or None): The predicted label associated with the leaf node.

If the node is a leaf node, then feature_index, threshold_value, left_child, right_child, and left_ratio are None, while leaf_value is an integer. If the node is not a leaf node, then only leaf_value is None.

Methods:

• is_leaf(): This method checks whether the current node is a leaf node. It returns True if the node has a leaf_value, and False otherwise.

2.2 DecisionTreeClassifier Class

The DecisionTreeClassifier class implements a decision tree for binary classification. It recursively splits the data based on specific features and thresholds, creating a tree structure that can be used for predicting labels. The attributes and methods of this class are designed to support model training, hyperparameter tuning, and prediction.

Attributes:

- min_samples_split (int): The minimum number of samples required to split a node.
- max_depth (int or None): The maximum depth of the tree. If set to None, the tree expands until all nodes are pure, contain fewer than min_samples_split samples, or further splitting results in an information gain below min_information_gain.
- n_features (int, float, or str): The number of features to consider when identifying the best split. This can be specified as an integer, a float, or one of the following strings: 'sqrt' or 'log2'.
- criterion (str): The function to measure the quality of a split. Options are: 'gini', 'scaled_entropy', and 'square_root'.
- min_information_gain (float): The minimum information gain required to perform a split.
- n_quantiles (int or None): The number of quantiles to consider when determining the best threshold for continuous features. If set to None, the algorithm uses midpoints of unique values.
- isolate_one (bool): Whether to isolate a single value for categorical features, creating a one-vs-rest split.
- root (TreeNode or None): The root node of the decision tree.
- depth (int): The final depth of the tree after it has been built.

min_samples_split Parameter:

The min_samples_split parameter controls the minimum number of samples a node must contain to be eligible for splitting. If a node has fewer than min_samples_split samples, it becomes a leaf node, and no further splits are attempted.

A higher value for min_samples_split reduces the depth of the tree, making it less prone to capturing noise in the data. Conversely, a lower value allows the tree to grow deeper and potentially capture finer details, which can be beneficial for highly complex datasets but may increase the risk of overfitting. The default value is 2.

n_features Parameter:

The n_features parameter specifies the number of features to consider when identifying the best split. The default value is None, which results in all features in the dataset being considered. Otherwise:

- If n_features is an integer, this specifies the exact number of features to consider. If the value exceeds the total number of features in the dataset, all features are considered instead.
- If n_features is a float, it represents a fraction of the total number of features. The number of features to consider is calculated by multiplying this fraction by the total number of features and truncating the decimal part to obtain an integer. At least one feature is considered.
- If n_features is a string, it can be either 'sqrt' or 'log2', and the number of features is calculated as follows:
 - 'sqrt': Sets the number of features to the square root of the total number of features, truncating the decimal part to obtain an integer. At least one feature is considered.
 - 'log2': Sets the number of features to the base-2 logarithm of the total number of features, truncating the decimal part to obtain an integer. At least one feature is considered.

This parameter allows the decision tree model to use a subset of features, which can help improve the model's efficiency and performance, particularly when working with high-dimensional datasets.

criterion Parameter:

The criterion parameter specifies the function used to measure the quality of a split in the decision tree. The available options are:

• 'gini' (the default): The Gini impurity is used, which is computed as:

$$Gini = 2 \cdot p_0 \cdot (1 - p_0)$$

where p_0 is the probability of class '0' within the node.

• 'scaled_entropy': The scaled entropy is used. The entropy is scaled by halving the probabilities before applying the standard entropy formula:

Scaled Entropy =
$$-\sum_{i} \frac{p_i}{2} \cdot \log_2(p_i + \epsilon)$$

where p_i is the probability of class i, and ϵ is a small constant to avoid taking the logarithm of zero.

• 'square_root': The "square root" impurity is used, which is calculated as:

Square Root Impurity =
$$\sqrt{p_0 \cdot (1 - p_0)}$$

where p_0 is the probability of class '0' within the node.

min_information_gain Parameter:

The min_information_gain parameter specifies the minimum amount of information gain required to perform a split. Information gain measures the reduction in impurity after a split. It is computed as follows:

where the impurity is calculated using the selected **criterion**, such as Gini impurity, scaled entropy, or square root impurity. The weighted impurity after the split is calculated as:

Weighted Impurity After Split =
$$\frac{L}{n}$$
 · Impurity of Left Child + $\frac{R}{n}$ · Impurity of Right Child

where:

- L and R are the number of samples in the left and right child nodes, respectively.
- \bullet *n* is the total number of samples in the parent node.

The min_information_gain parameter accepts a float value that sets the threshold for the minimum information gain. If the calculated information gain from a potential split is less than this threshold, the split is not performed, and the node becomes a leaf node. The default value is 0.0.

n_quantiles Parameter:

The n_quantiles parameter determines how candidate thresholds are chosen when splitting based on numerical features. If set to None (the default), all midpoints between unique values are considered. Otherwise:

• If n_quantiles is an integer, the values are divided into that many quantiles, and the candidate thresholds are the boundaries between these quantiles.

While lower values of n_quantiles reduce the number of candidate thresholds, speeding up computation but potentially leading to suboptimal splits, higher values or setting it to None (to consider all midpoints) increase the search granularity, increasing the probability of finding an optimal split, but at the cost of additional computation time.

isolate_one Parameter:

The isolate_one parameter controls how splits are made when splitting based on categorical features. If set to False (the default), all data points with a feature value lower or equal (i.e., lower or equal alphabetically) to the threshold are assigned to the left child, while all other data points are assigned to the right child. Otherwise:

• If isolate_one is set to True, the algorithm creates a one-vs-rest split, where all data points with a feature value equal to the threshold go to the left child, while all other data points go to the right child.

This parameter affects the granularity of splits for categorical features. Setting <code>isolate_one</code> to <code>True</code> results in more precise splits, capturing finer patterns in the data but potentially increasing the risk of overfitting. In contrast, setting it to <code>False</code> produces broader, more generalized splits, improving computational efficiency and helping reduce overfitting.

Private Methods:

- _build_tree(): Recursively builds the tree by splitting the data based on the best feature and threshold. It stops if any stopping condition is met, e.g., max_depth.
- _get_most_common_label(): This method finds and returns the most common label in a given array.
- _find_best_split(): Finds the best feature and threshold for splitting the data.
- _calculate_information_gain(): Computes the information gain from a potential split based on a selected criterion.
- _split(): Splits the data based on the selected feature and threshold.
- _gini_impurity(): Computes the Gini impurity for the given labels.
- _scaled_entropy(): Computes the scaled entropy for the given labels.
- _square_root_impurity(): Computes the "square root" impurity for the given labels.
- _traverse_tree(): Traverses the tree for a single input sample and returns the predicted label.

Public Methods:

- fit(): Initializes the root node and builds the tree using the _build_tree() method.
- predict(): Predicts the labels for the given input samples by traversing the tree for each sample using the _traverse_tree() method.

_build_tree() Method:

The _build_tree() method constructs a decision tree by starting at the root node and progressing recursively to the leaf nodes. At each node, it selects a random subset of features, as specified by the n_features parameter, and employs the _find_best_split() method to determine the optimal feature and threshold for splitting the data. Once the best split is found, the _split() method is called to partition the data accordingly. The process is then repeated recursively on the resulting subsets to continue building the tree.

The recursion halts when a stopping condition is met, such as reaching the max_depth, achieving pure nodes, having fewer than min_samples_split samples per node, or when subsequent splits yield information gains lower than min_information_gain. Upon termination, the method assigns the most frequent label among the samples at that node as the predicted label for that node.

_find_best_split() Method:

The _find_best_split() method identifies the optimal split for a given node in the decision tree. It iterates through all features selected by the _build_tree() method and evaluates all candidate thresholds by calling the _calculate_information_gain() method to determine the feature-threshold combination that maximizes information gain. The creation of candidate thresholds differs between numerical and categorical features:

- For numerical features, potential thresholds are determined based on the n_quantiles parameter (as described above).
- For categorical features, candidate thresholds consist of all unique values in the feature.

Any missing values are excluded when determining the candidate thresholds.

_split() Method:

The _split() method partitions the data based on a specified feature and threshold. The partitioning strategy differs for numerical and categorical features:

- For numerical features, data points with a feature value lower than or equal to the threshold are assigned to the left child, while all other data points are assigned to the right child.
- For categorical features, the partitioning depends on the isolate_one parameter (as described above).

After the split, any data points with a missing feature value are randomly distributed between the left and right child. The probability of being assigned to each child is proportional to the number of data points assigned to that child during the split.

_traverse_tree() Method:

The _traverse_tree() method traverses the decision tree to predict the label for a single instance. Starting at the root node, it follows the tree's decision rules until it reaches a leaf node. If the feature value at the current node is missing, the method randomly decides whether to move to the left or right child, based on the ratio of data points assigned to each child.

3 Training and Validation Procedures

Training a model on the training set and testing it on the test set is a fundamental practice in machine learning. The goal is to develop a model that generalizes well to new, unseen data, and not just memorizes the data seen during training (a phenomenon known as overfitting).

In this study, a set of custom functions has been implemented to facilitate robust model training, validation, and hyperparameter tuning.

Functions:

- train_test_partition(): This function randomly partitions the data into training and testing sets. The proportion of data allocated to each set is specified by the user (the default is 20% testing).
- k_fold_partition(): This function divides the data into k folds for k-fold cross-validation. The number of folds is specified by the user (the default is 5).
- $k_fold_cv_estimate()$: This function uses the $k_fold_partition()$ function to create k folds and trains the model k times, each time using k-1 folds for training and the remaining fold for testing. The average test error across all iterations (i.e., the cross-validation estimate) is returned.
- hyperparameter_tuning(): This function iterates through all parameter combinations generated by the _parameter_combinations() function and uses the k_fold_cv_estimate() function to compute the cross-validation estimate for a model with these parameters. The lowest cross-validation estimate and the corresponding parameters are then returned.
- k_fold_nested_cv(): This function implements nested cross-validation. The k_fold_partition() function is used to create k folds and the model is trained k times. Each time, the hyperparameter_tuning() function is invoked on k-1 folds and the model with the best parameters is tested on the remaining fold. Then the average test error across all iterations is returned.
- _parameter_combinations(): This helper function generates all possible combinations of hyperparameters from a specified grid.
- accuracy_metric(): This function computes the accuracy of the model's predictions.

4 Dataset Description

The dataset used in this study is a simulated version inspired by the Mushroom Data Set from J. Schlimmer. It contains 61,069 hypothetical mushrooms, each described by 20 features and classified as either definitely edible or definitely poisonous/of unknown edibility. Table 1 presents all 21 variables included in the dataset.

The dataset is balanced, with 27,181 mushrooms classified as edible and 33,888 as poisonous, ensuring that no class is overrepresented in subsequent analyses. During preprocessing, 146 duplicate rows were identified and removed to prevent undue weighting of any observation. This step reduced the dataset to 60,923 observations. Additionally, nine variables were identified as containing missing values, as shown in Table 2.

Upon further inspection, a question arose about whether the value "f" should be treated as a regular value or as missing. After careful consideration, it was decided to encode all occurrences of "f" as missing, except in "does-bruise-or-bleed" and "has-ring", where "f" is interpreted as "no" rather than "none". This increased the number of variables with missing values to twelve (see Table 3).

Table 1: Mushroom Dataset Variables

class cap-diameter numerical float number in cm cap-shape categorical cap-surface cap-shape categorical cap-surface categorical categorical cap-surface categorical colors categorical categorical colors categorical categorical categorical categorical categorical categorical colors categorical categor	Variable	Type	Possible Values
cap-shape categorical b (bell), c (conical), x (convex), f (flat), s (sunken), p (spherical), o (others) cap-surface categorical i (fibrous), g (grooves), y (scaly), s (smooth), h (shiny), l (leathery), k (silky), t (sticky), w (wrinkled), e (fleshy), d (not specified by the author) cap-color categorical n (brown), b (buff), g (gray), r (green), p (pink), u (purple), e (red), w (white), y (yellow), l (blue), o (orange), k (black) does-bruise-or-bleed categorical t (bruises or bleeding), f (no) gill-attachment categorical a (adnate), x (adnexed), d (decurrent), e (free), s (sinuate), p (pores), f (none) gill-spacing categorical c (close), d (distant), f (none) gill-color categorical n (brown), b (buff), g (gray), r (green), p (pink), u (purple), e (red), w (white), y (yellow), o (orange), k (black), f (none) stem-height numerical float number in cm stem-width numerical float number in mm stem-root categorical b (bulbous), s (swollen), c (club), r (rooted), f (not specified by the author) stem-surface categorical i (fibrous), y (scaly), s (smooth), h (shiny), k (silky), t (sticky), f (none), g (not specified by the author) stem-color categorical n (brown), b (buff), g (gray), r (green), p (pink), u (purple), e (red), w (white), y (yellow), l (blue), o (orange), k (black), f (none) veil-type categorical n (brown), u (purple), e (red), w (white), y (yellow), k (black) has-ring categorical t (ring), f (none) ring-type categorical e (evanescent), r (flaring), g (grooved), l (large), p (pendant), z (zone), m (movable), f (none) spore-print-color categorical n (brown), g (gray), r (green), p (pink), u (purple), w (white), k (black) habitat categorical a (prayses), l (leaves), m (meadows), p (paths), h (heaths), u (urban), w (waste), d (woods)	class	categorical	e (edible), p (poisonous/of unknown edibility)
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spore-print-color categorical n (brown), g (gray), r (green), p (pink), u (purple), w (white), k (black) habitat categorical g (grasses), l (leaves), m (meadows), p (paths), h (heaths), u (urban), w (waste), d (woods)	has-ring	categorical	(6)// (//
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habitat categorical g (grasses), l (leaves), m (meadows), p (paths), h (heaths), u (urban), w (waste), d (woods)			
(waste), d (woods)	spore-print-color	categorical	n (brown), g (gray), r (green), p (pink), u (purple), w (white), k (black)
	habitat	categorical	g (grasses), l (leaves), m (meadows), p (paths), h (heaths), u (urban), w
season categorical s (spring), u (summer), a (autumn), w (winter)			(waste), d (woods)
	season	categorical	s (spring), u (summer), a (autumn), w (winter)

Table 2: Missing Values Count and Percentage

	Missing Values		
Variable	Count	Percentage	
cap-surface	14120	23.12	
gill-attachment	9855	16.14	
gill-spacing	25062	41.04	
stem-root	51536	84.39	
stem-surface	38 122	62.42	
veil-type	57746	94.56	
veil-color	53510	87.62	
ring-type	2471	4.05	
spore-print-color	54597	89.40	

Table 3: Missing Values Count and Percentage (After Replacing 'f' with NaN)

	Missi	Missing Values		
Variable	Count	Percentage		
cap-shape	13404	21.95		
cap-surface	14120	23.12		
gill-attachment	13269	21.73		
gill-spacing	28476	46.63		
gill-color	3414	5.59		
stem-root	52451	85.89		
stem-surface	39037	63.92		
stem-color	915	1.50		
veil-type	57746	94.56		
veil-color	53510	87.62		
ring-type	50686	83.00		
spore-print-color	54597	89.40		