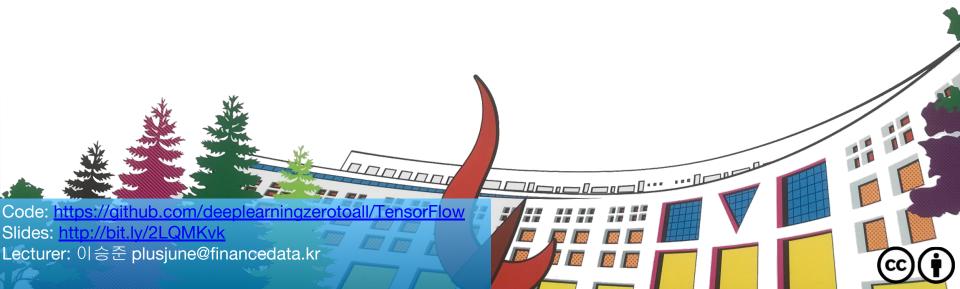
ML/DL for Everyone Season2



03 - How to minimize cost LAB



Simplified hypothesis

Hypothesis
$$H(x)=Wx$$

Cost
$$cost(W)=rac{1}{m}\sum_{i=1}^m{(Wx_i-y_i)^2}$$
우리의 가설(예측) - 실제

Cost function in pure Python

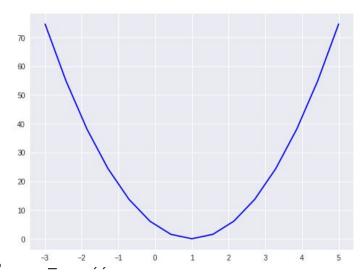
$$cost(W) = rac{1}{m} \sum_{i=1}^m \left(Wx_i - y_i
ight)^2$$

```
import numpy as np
X = np.array([1, 2, 3])
                                                                  W
                                                                            cost
Y = np.array([1, 2, 3])
                                                                -3.000 I
                                                                         74.66667
def cost_func(W, X, Y):
                                                                -2.429 | 54.85714
                                                                -1.857 | 38.09524
    c = 0
                                                                -1.286 | 24.38095
    for i in range(len(X)):
                                                                -0.714 \mid 13.71429
        c += (W * X[i] - Y[i]) ** 2
                                                                -0.143 | 6.09524
    return c / len(X)
                                                                0.429 | 1.52381
-3부터 5까지 15개의. 구간으로 나누기 for feed_W in np.linspace(-3, 5, num=15):
                                                                1.000 | 0.00000
                                                                1.571 I 1.52381
    curr cost = cost func(feed W, X, Y)
                                                                 2.143 | 6.09524
    print("{:6.3f} | {:10.5f}".format(feed W, curr cost))
                                                                 2.714 |
                                                                         13.71429
                                                                 3.286 |
                                                                         24.38095
                                                                 3.857 | 38.09524
                                                                 4.429 |
                                                                         54.85714
                                                                 5.000 I
                                                                         74.66667
```

Cost function in pure Python

$$cost(W) = rac{1}{m} \sum_{i=1}^m \left(Wx_i - y_i
ight)^2$$

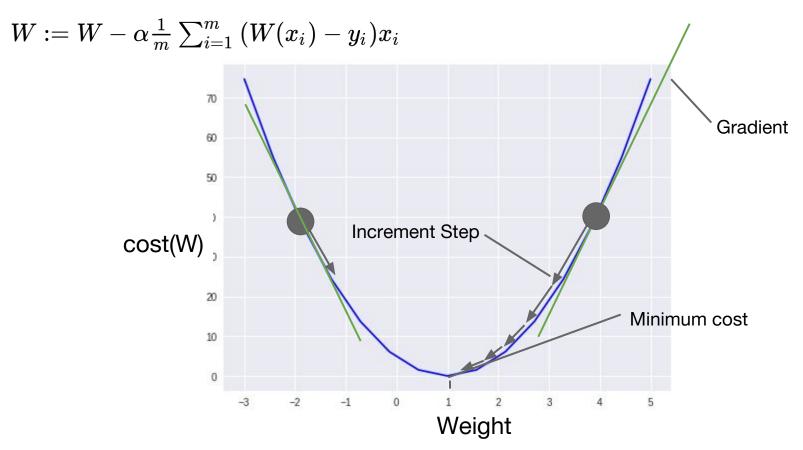
```
import numpy as np
X = np.array([1, 2, 3])
Y = np.array([1, 2, 3])
def cost_func(W, X, Y):
    c = 0
    for i in range(len(X)):
        c += (W * X[i] - Y[i]) ** 2
    return c / len(X)
for feed W in np.linspace(-3, 5, num=15):
    curr cost = cost func(feed W, X, Y)
    print("{:6.3f} | {:10.5f}".format(feed W,
```



Cost function in TensorFlow

$$cost(W) = rac{1}{m} \sum_{i=1}^m \left(Wx_i - y_i
ight)^2$$

```
X = np.array([1, 2, 3])
Y = np.array([1, 2, 3])
                                                       70
                                                       60
def cost_func(W, X, Y):
  hypothesis = X * W
  return tf.reduce mean(tf.square(hypothesis - Y))
                                                      40
W values = np.linspace(-3, 5, num=15)
                                                       30
cost values = []
                                                       20
for feed W in W values:
    curr cost = cost func(feed W, X, Y)
                                                       10
    cost values.append(curr cost)
    print("{:6.3f} | {:10.5f}".format(feed W, curr ())
```



$$cost(W) = rac{1}{m} \sum_{i=1}^m \left(Wx_i - y_i
ight)^2$$

$$W := W - lpha rac{1}{m} \sum_{i=1}^m \left(W(x_i) - y_i
ight) x_i$$

Gradient

```
alpha = 0.01
gradient = tf.reduce_mean(tf.multiply(tf.multiply(W, X) - Y, X))

새로운 W 값 descent = W - tf.multiply(alpha, gradient)
W.assign(descent)
```

```
랜덤 시드를 특정한 값으로 초기화 (다음 다시 이 코드를 실행해도 동일한 결과를 위해서)
 tf.set random seed(0) # for reproducibility
 x data = [1., 2., 3., 4.]
 y_{data} = [1., 3., 5., 7.]
                                                       정규 분포를 따르는 행렬 1개짜리
 W = tf.Variable(tf.random_normal([1], -100., 100.))
                                                    .random normal([행렬 수], 평균, 편차
 for step in range(300):
     hypothesis = W * X
     cost = tf.reduce mean(tf.square(hypothesis - Y))
     alpha = 0.01
     gradient = tf.reduce mean(tf.multiply(tf.multiply(W, X) - Y, X))
     descent = W - tf.multiply(alpha, gradient)
                                                      W := W - lpha rac{1}{m} \sum_{i=1}^m \left(W(x_i) - y_i
ight) x_i
     W.assign(descent)
     if step % 10 == 0:
         print('{:5} | {:10.4f} | {:10.6f}'.format(
             step, cost.numpy(), W.numpy()[0]))
```

```
W
tf.set random seed(0) # for reproducibility
                                                               step
                                                                          cost
                                                                  0 | 11716.3086 |
                                                                                    48.767971
x data = [1., 2., 3., 4.]
                                                                       4504.9126 I
                                                                                    30.619968
                                                                 10 I
y data = [1., 3., 5., 7.]
                                                                 20 | 1732.1364 |
                                                                                   19.366755
                                                                 30 | 666.0052 | 12.388859
W = tf.Variable(tf.random normal([1], -100., 100.))
                                                                 40 | 256.0785 | 8.062004
                                                                 50 | 98.4620 | 5.379007
for step in range(300):
                                                                 60 I
                                                                        37.8586 | 3.715335
   hypothesis = W * X
                                                                 70 | 14.5566 |
                                                                                   2.683725
   cost = tf.reduce mean(tf.square(hypothesis - Y))
                                                                                     2.044044
                                                                 80 | 5.5970 |
   alpha = 0.01
                                                                240 |
                                                                         0.0000 |
                                                                                     1.000499
   gradient = tf.reduce mean(tf.multiply(tf.multiply(W, X) - Y, X)
                                                                250 I
                                                                         0.0000 |
                                                                                    1.000309
   descent = W - tf.multiply(alpha, gradient)
                                                                260 I
                                                                         0.0000 |
                                                                                    1.000192
   W.assign(descent)
                                                                270 I
                                                                         0.0000 |
                                                                                    1.000119
                                                                                    1.000074
                                                                280 I
                                                                         0.0000 |
   if step % 10 == 0:
                                                                290 I
                                                                         0.0000 |
                                                                                     1.000046
       print('{:5} | {:10.4f} | {:10.6f}'.format(
           step, cost.numpy(), W.numpy()[0]))
```

Output when W=5

W=5

W = -3

```
50
tf.set random seed(0) # for reproducibility
x data = [1., 2., 3., 4.]
y data = [1., 3., 5., 7.]
W = tf.Variable([5.0]) W를 값을 앞에서는 랜덤 값을 주었는데, 특정 값을 줘도 같은 결과
for step in range(300):
    hypothesis = W * X
                                                                     step
                                                                             cost
                                                                                          W
    cost = tf.reduce mean(tf.square(hypothesis - Y))
                                                                      0 1
                                                                             74.6667 |
                                                                                         4.813334
                                                                     10 I
                                                                             28.7093 |
                                                                                         3.364572
    alpha = 0.01
                                                                     20 1
                                                                             11.0387
                                                                                         2.466224
    gradient = tf.reduce mean(tf.multiply(tf.multiply(W, X) - Y, X)
                                                                             4.2444 |
                                                                     30 L
                                                                                         1.909177
    descent = W - tf.multiply(alpha, gradient)
                                                                              1.6320 |
                                                                                         1.563762
                                                                     40
    W.assign(descent)
                                                                     50 I
                                                                              0.6275 |
                                                                                         1.349578
                                                                     60 I
                                                                              0.2413 |
                                                                                         1.216766
    if step % 10 == 0:
                                                                     70 I
                                                                              0.0928 |
                                                                                         1.134412
        print('{:5} | {:10.4f} | {:10.6f}'.format(
                                                                              0.0357 |
                                                                                         1.083346
                                                                     80 |
            step, cost.numpy(), W.numpy()[0]))
                                                                    270 I
                                                                              0.0000 |
                                                                                         1.000009
                                                                    280 I
                                                                              0.0000 |
                                                                                         1.000006
                                                                    290 I
                                                                              0.0000
                                                                                         1.000004
```

What's Next?

• Multi-Variable Linear regression