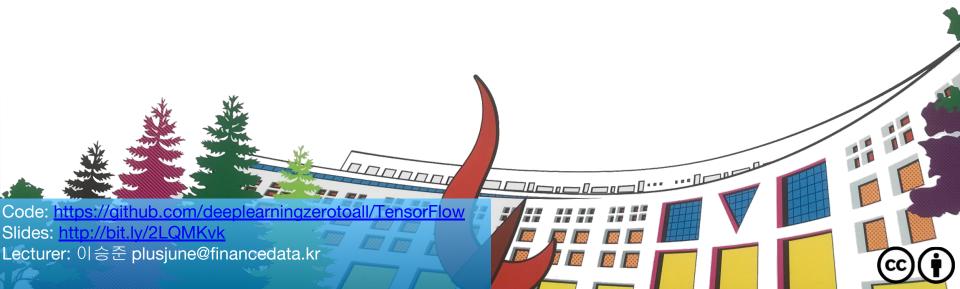
ML/DL for Everyone Season2



03 - How to minimize cost LAB



Simplified hypothesis

Hypothesis H(x)=Wx

Cost
$$cost(W) = rac{1}{m} \sum_{i=1}^m (Wx_i - y_i)^2$$

우리의 가설(예측) - 실제

Cost function in pure Python

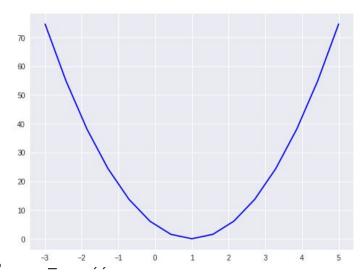
$$cost(W) = rac{1}{m} \sum_{i=1}^m \left(Wx_i - y_i
ight)^2$$

```
import numpy as np
X = np.array([1, 2, 3])
                                                                W
                                                                          cost
Y = np.array([1, 2, 3])
                                                              -3.000 I
                                                                       74.66667
def cost_func(W, X, Y):
                                                             -2.429 | 54.85714
                                                              -1.857 | 38.09524
    c = 0
                                                             -1.286 | 24.38095
    for i in range(len(X)):
                                                             -0.714 \mid 13.71429
        c += (W * X[i] - Y[i]) ** 2
                                                              -0.143 | 6.09524
    return c / len(X)
                                                              0.429 | 1.52381
                  -3부터 5까지 15개의, 구간으로 나누기
                                                              1.000 | 0.00000
for feed W in np.linspace(-3, 5, num=15):
                                                              1.571 I 1.52381
    curr cost = cost func(feed W, X, Y)
                                                              2.143 | 6.09524
    print("{:6.3f} | {:10.5f}".format(feed W, curr cost))
                                                              2.714 |
                                                                       13.71429
                                                               3.286 |
                                                                       24.38095
                                                               3.857 | 38.09524
                                                               4.429 |
                                                                       54.85714
                                                               5.000 I
                                                                       74.66667
```

Cost function in pure Python

$$cost(W) = rac{1}{m} \sum_{i=1}^m \left(Wx_i - y_i
ight)^2$$

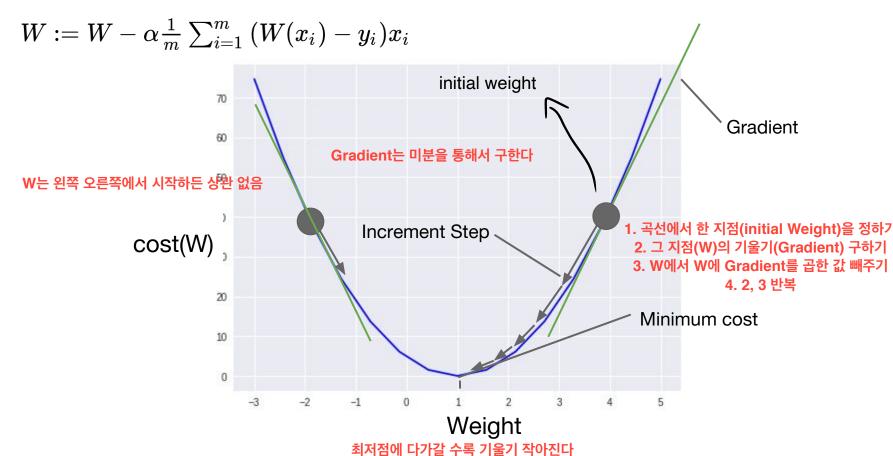
```
import numpy as np
X = np.array([1, 2, 3])
Y = np.array([1, 2, 3])
def cost_func(W, X, Y):
    c = 0
    for i in range(len(X)):
        c += (W * X[i] - Y[i]) ** 2
    return c / len(X)
for feed W in np.linspace(-3, 5, num=15):
    curr cost = cost func(feed W, X, Y)
    print("{:6.3f} | {:10.5f}".format(feed W,
```



Cost function in TensorFlow

$$cost(W) = rac{1}{m} \sum_{i=1}^m \left(Wx_i - y_i
ight)^2$$

```
X = np.array([1, 2, 3])
Y = np.array([1, 2, 3])
                                                       70
                                                       60
def cost_func(W, X, Y):
  hypothesis = X * W
  return tf.reduce mean(tf.square(hypothesis - Y))
                                                      40
W values = np.linspace(-3, 5, num=15)
                                                       30
cost values = []
                                                       20
for feed W in W values:
    curr cost = cost func(feed W, X, Y)
                                                       10
    cost values.append(curr cost)
    print("{:6.3f} | {:10.5f}".format(feed W, curr ())
```



$$cost(W) = rac{1}{m} \sum_{i=1}^m \left(Wx_i - y_i
ight)^2$$

$$W := W - lpha rac{1}{m} \sum_{i=1}^m \left(W(x_i) - y_i
ight) x_i$$

함수의 기울기

```
alpha = 0.01
gradient = tf.reduce_mean(tf.multiply(tf.multiply(W, X) - Y, X))
새로운 W 값
descent = W - tf.multiply(alpha, gradient)
W.assign(descent)
```

```
랜덤 시드를 특정한 값으로 초기화 (다음 다시 이 코드를 실행해도 동일한 결과를 위해서)
tf.set random seed(0) # for reproducibility
x data = [1., 2., 3., 4.]
v data = [1., 3., 5., 7.]
                                                           정규 분포를 따르는 행렬 1개짜리
W = tf.Variable(tf.random normal([1], -100., 100.))
                                                        .random_normal([행렬 수], 평균, 편차
for step in range(300):
    hypothesis = W * X
    cost = tf.reduce mean(tf.square(hypothesis - Y))
    alpha = 0.01
    gradient = tf.reduce mean(tf.multiply(tf.multiply(W, X) - Y, X))
    descent = W - tf.multiply(alpha, gradient)
                                                       \overline{W := W - lpha_{rac{1}{m}} \sum_{i=1}^m \left(W(x_i) - y_i
ight)} x_i
    W.assign(descent)
    if step % 10 == 0:
        print('{:5} | {:10.4f} | {:10.6f}'.format(
            step, cost.numpy(), W.numpy()[0]))
```

```
W
tf.set random seed(0) # for reproducibility
                                                               step
                                                                          cost
                                                                  0 | 11716.3086 |
                                                                                    48.767971
x data = [1., 2., 3., 4.]
                                                                       4504.9126 I
                                                                                    30.619968
                                                                 10 I
y data = [1., 3., 5., 7.]
                                                                 20 | 1732.1364 |
                                                                                   19.366755
                                                                 30 | 666.0052 | 12.388859
W = tf.Variable(tf.random normal([1], -100., 100.))
                                                                 40 | 256.0785 | 8.062004
                                                                 50 | 98.4620 | 5.379007
for step in range(300):
                                                                 60 I
                                                                        37.8586 | 3.715335
   hypothesis = W * X
                                                                 70 | 14.5566 |
                                                                                   2.683725
   cost = tf.reduce mean(tf.square(hypothesis - Y))
                                                                                     2.044044
                                                                 80 | 5.5970 |
   alpha = 0.01
                                                                240 |
                                                                         0.0000 |
                                                                                     1.000499
   gradient = tf.reduce mean(tf.multiply(tf.multiply(W, X) - Y, X)
                                                                250 I
                                                                         0.0000 |
                                                                                    1.000309
   descent = W - tf.multiply(alpha, gradient)
                                                                260 I
                                                                         0.0000 |
                                                                                    1.000192
   W.assign(descent)
                                                                270 I
                                                                         0.0000 |
                                                                                    1.000119
                                                                                    1.000074
                                                                280 I
                                                                         0.0000 |
   if step % 10 == 0:
                                                                290 I
                                                                         0.0000 |
                                                                                     1.000046
       print('{:5} | {:10.4f} | {:10.6f}'.format(
           step, cost.numpy(), W.numpy()[0]))
```

Output when W=5

W=5

W = -3

50

```
tf.set random seed(0) # for reproducibility
x data = [1., 2., 3., 4.]
y data = [1., 3., 5., 7.]
W = tf.Variable([5.0]) W = tf.Variable([5.0])
for step in range(300):
   hypothesis = W * X
                                                                            cost
                                                                                         W
                                                                     step
    cost = tf.reduce mean(tf.square(hypothesis - Y))
                                                                     0 1
                                                                            74.6667 |
                                                                                        4.813334
                                                                    10 I
                                                                            28.7093 |
                                                                                        3.364572
    alpha = 0.01
                                                                    20 1
                                                                            11.0387
                                                                                        2.466224
    gradient = tf.reduce mean(tf.multiply(tf.multiply(W, X) - Y, X)
                                                                            4.2444 |
                                                                    30 L
                                                                                        1.909177
    descent = W - tf.multiply(alpha, gradient)
                                                                             1.6320 |
                                                                                        1.563762
                                                                    40
   W.assign(descent)
                                                                    50 I
                                                                             0.6275 |
                                                                                        1.349578
                                                                    60 I
                                                                             0.2413 |
                                                                                        1.216766
    if step % 10 == 0:
                                                                    70 I
                                                                             0.0928 |
                                                                                        1.134412
       print('{:5} | {:10.4f} | {:10.6f}'.format(
                                                                    80 |
                                                                             0.0357 |
                                                                                        1.083346
           step, cost.numpy(), W.numpy()[0]))
                                                                   270 I
                                                                             0.0000 |
                                                                                        1.000009
                                                                   280 I
                                                                             0.0000 |
                                                                                        1.000006
                                                                   290 I
                                                                             0.0000
                                                                                        1.000004
```

What's Next?

• Multi-Variable Linear regression