TSDT14 Signal Theory

Lecture 12 Complex Signals

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Modulation

$$s(t) = s_{\rm I}(t)\sqrt{2}\cos(2\pi f_{\rm c}t) - s_{\rm Q}(t)\sqrt{2}\sin(2\pi f_{\rm c}t)$$

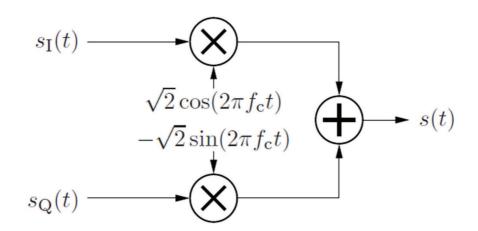
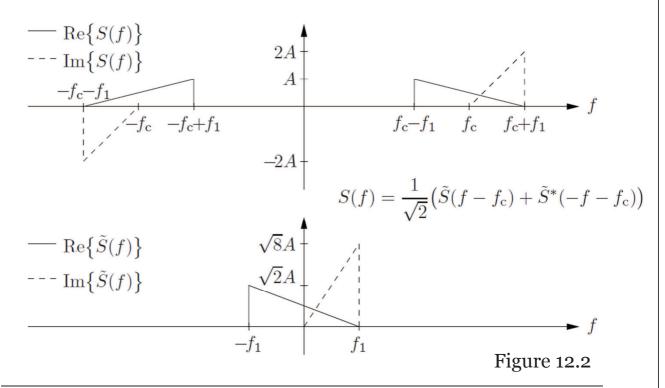


Figure 12.1

Modulations in the frequency domain





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In Phase and Quadrature Phase

$$\operatorname{Re}\{S_{\mathrm{I}}(f)\} = \frac{1}{2}\operatorname{Re}\{\tilde{S}(f) + \tilde{S}(-f)\},$$

$$\operatorname{Im}\{S_{\mathrm{I}}(f)\} = \frac{1}{2}\operatorname{Im}\{\tilde{S}(f) - \tilde{S}(-f)\},$$

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$$\operatorname{Im}\{S_{\mathrm{I}}(f)\} = \frac{1}{2}\operatorname{Im}\{\tilde{S}(f) - \tilde{S}(-f)\},$$

$$\operatorname{Im}\{S_{\mathrm{Q}}(f)\} = \frac{1}{2}\operatorname{Im}\{\tilde{S}(-f) + \tilde{S}(f)\},$$

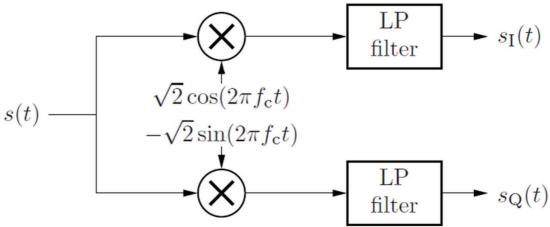
$$\operatorname{Im}\{S_{\mathrm{Q}}(f)\} = \frac{1}{2}\operatorname{Re}\{\tilde{S}(-f) - \tilde{S}(f)\}.$$

$$\operatorname{Im}\{S_{\mathrm{Q}}(f)\} = \frac{1}{2}\operatorname{Re}\{\tilde{S}(-f) - \tilde{S}(f)\}.$$

Figure 12.3

Demodulation

$$\sqrt{2}s(t)\cos(2\pi f_{c}t) = 2s_{I}(t)\cos^{2}(2\pi f_{c}t) - 2s_{Q}(t)\sin(2\pi f_{c}t)\cos(2\pi f_{c}t)
= s_{I}(t)(1 + \cos(4\pi f_{c}t)) - s_{Q}(t)\sin(4\pi f_{c}t)
-\sqrt{2}s(t)\sin(2\pi f_{c}t) = -2s_{I}(t)\cos(2\pi f_{c}t)\sin(2\pi f_{c}t) + 2s_{Q}(t)\sin^{2}(2\pi f_{c}t)
= -s_{I}(t)\sin(4\pi f_{c}t) + s_{Q}(t)(1 - \cos(4\pi f_{c}t))$$

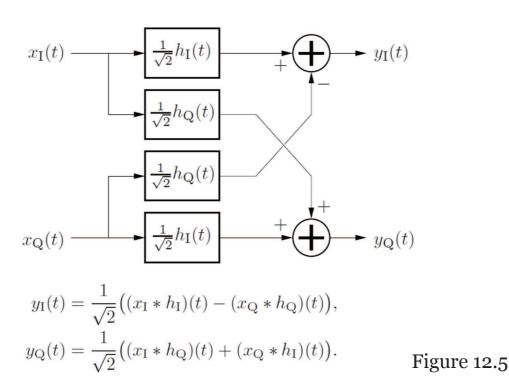


$$\begin{split} \mathcal{F} \big\{ \sqrt{2} s(t) \cos(2\pi f_{\rm c} t) \big\} &= \\ &= S_{\rm I}(f) + \frac{1}{2} \big(S_{\rm I}(f - 2f_{\rm c}) + S_{\rm I}(f + 2f_{\rm c}) + j S_{\rm Q}(f - 2f_{\rm c}) - j S_{\rm Q}(f + 2f_{\rm c}) \big) \\ \mathcal{F} \big\{ - \sqrt{2} s(t) \sin(2\pi f_{\rm c} t) \big\} &= \\ &= S_{\rm Q}(f) + \frac{1}{2} \big(S_{\rm I}(f - 2f_{\rm c}) - S_{\rm I}(f + 2f_{\rm c}) - j S_{\rm Q}(f - 2f_{\rm c}) - j S_{\rm Q}(f + 2f_{\rm c}) \big). \end{split}$$

Figure 12.4

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Filtering in the Baseband





Alternative Filtering in the Baseband

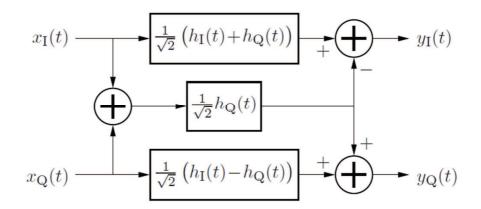


Figure 12.6

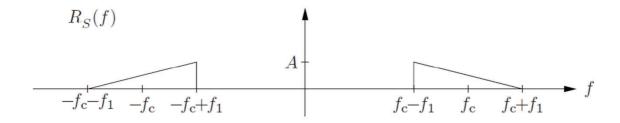


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Modulation of Stochastic Processes



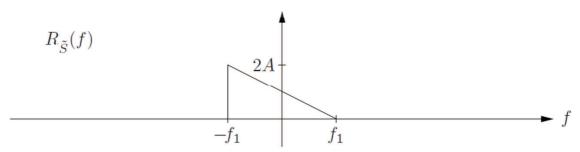


Figure 13.1



Rounding Up the Course

Stochastic processes: Stationarity, ergodicity, mean, ACF, PSD...

LTI filtering: Mean, ACF, PSD.

Cross-correlation and cross-spectrum. Joint stationarity.

Poisson processes.

Prediction.

Non-linearities: Squaring and such, saturation, quantization.

Modulation: AM, FM, PM, noise.

Estimation (only on laborations).

Linear mappings: Sampling, PAM, reconstruction.

Two-dimensional: Signals, systems,...

Complex processes



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Written Examination

When: Friday 2016-10-28, 14.00-18.00. Sign up!

Allowed aids:

Olofsson: Tables and Formulas for Signal Theory

Henriksson/Lindman: Formelsamling i Signalteori

Pocket calculator with empty memory

A German 10 mark note of the fourth series (1991-2001)

What:

A three-part introductory task (simple, 2/3 must be OK).

Five problems -5 points each, pass is 10 points.



Written Examination – cont'd

A German 10 mark note of the fourth series (1991-2001)





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Good Practices at Exams

Rules according to the exam cover:

- Only one task on the same piece of paper.
- Use only one side of the paper.
- Number the pages.
 (see common sense →)
- Do not use a red pen(cil). (that's my color)

Let me add:

- Hand in readable solutions.
- Do not hand in scriblings!

Common sense:

- 1. Solve the exam problems.
- 2. Sort the papers according to task numbering.
- 3. Number the pages <u>last!</u>
- 4. Now hand in your exam.

Do not do it in any other order!

Finally:

 Always provide solid arguments for steps taken in your solutions.



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