Artificial Intelligence

Clustering 2

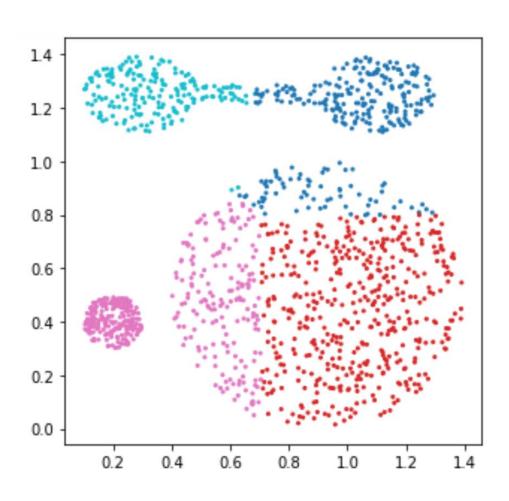
Extended from Kyuseok Shim's slides



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정 우 환 (whjung@hanyang.ac.kr) Fall 2021

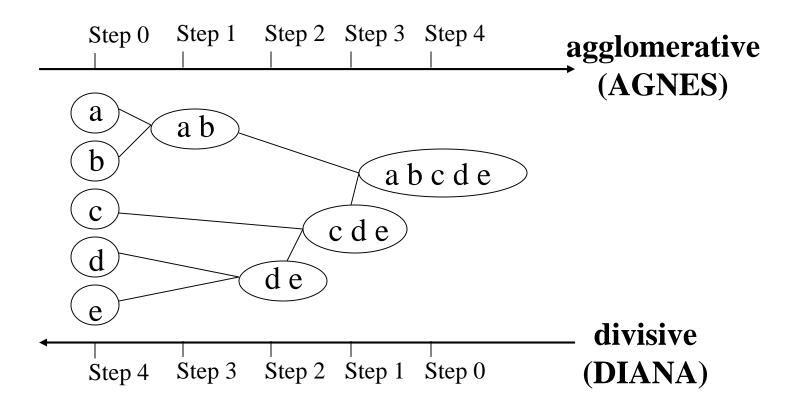
K-means clustering



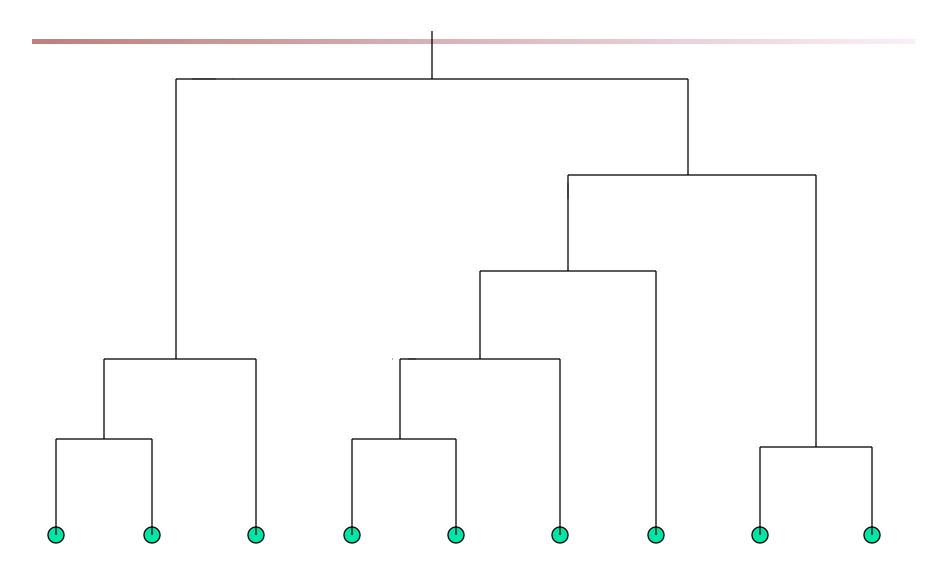
Hierarchical Clustering Approach

- Given k, the hierarchical algorithm is implemented in four steps:
 - Say "Every point is it's own cluster"
 - Find "most similar" pair of clusters
 - Merge it into a parent cluster
 - Repeat...until you've merged the whole dataset into k clusters

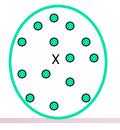
 Use distance matrix as clustering criteria. This method does not require the number of clusters k as an input, but needs a termination condition

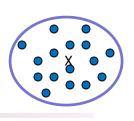


Dendrogram: Shows How Clusters are Merged



Distance between Clusters





- Single link: smallest distance between an element in one cluster and an element in the other, i.e., dist(K_i, K_j) = min(t_{ip}, t_{iq})
- Complete link: largest distance between an element in one cluster and an element in the other, i.e., dist(K_i, K_i) = max(t_{ip}, t_{iq})
- Average: avg distance between an element in one cluster and an element in the other, i.e., dist(K_i, K_j) = avg(t_{ip}, t_{jq})
- Centroid: distance between the centroids of two clusters, i.e.,
 dist(K_i, K_j) = dist(C_i, C_j)
- Medoid: distance between the medoids of two clusters, i.e., dist(K_i, K_j) = dist(M_i, M_j)
 - Medoid: a chosen, centrally located object in the cluster

Centroid, Radius and Diameter of a Cluster (for numerical data sets)

Centroid: the "middle" of a cluster

$$C_{m} = \frac{\sum_{i=1}^{N} (t_{ip})}{N}$$

• Radius: square root of average distance from any point of the cluster to its centroid $\sum_{r=0}^{N} \frac{1}{(r-r)^2}$

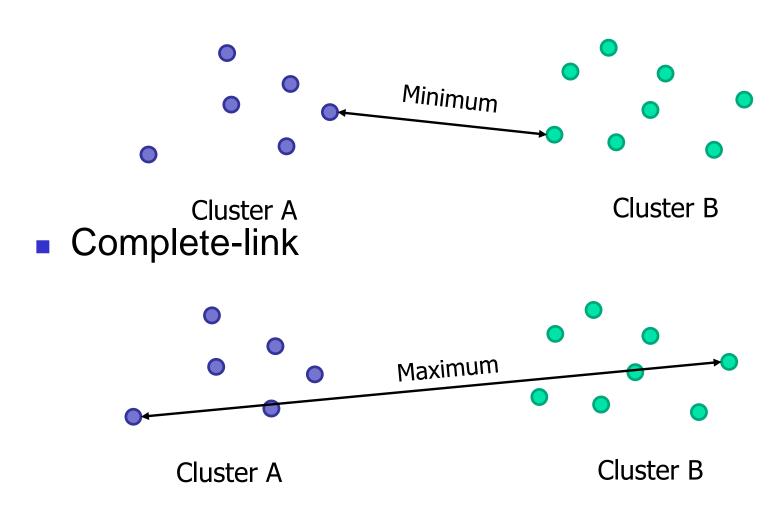
$$R_m = \sqrt{\frac{\sum_{i=1}^{N} (t_{ip} - c_m)^2}{N}}$$

 Diameter: square root of average mean squared distance between all pairs of points in the cluster

$$D_{m} = \sqrt{\frac{\sum_{i=1}^{N} \sum_{i=1}^{N} (t_{ip} - t_{iq})^{2}}{N(N-1)}}$$

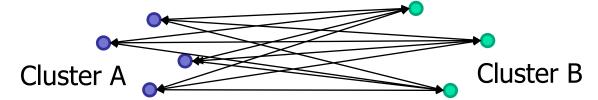
Hierarchical Algorithms

Single-link

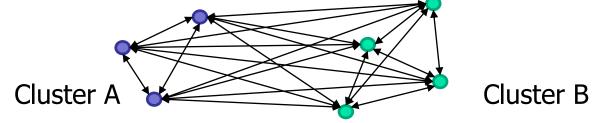


Hierarchical Algorithms

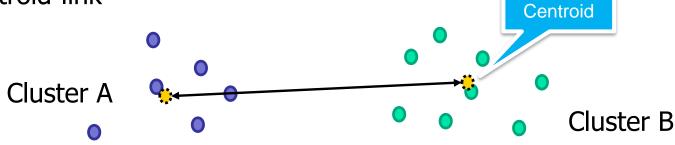
Average-link

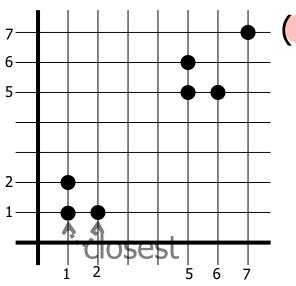


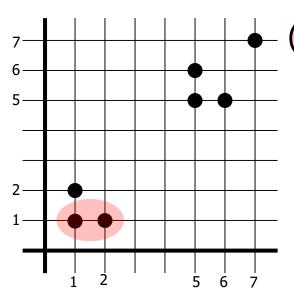
Mean-link

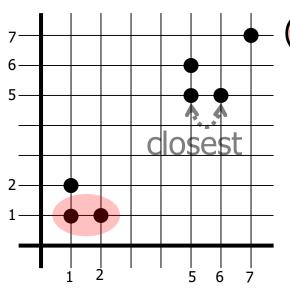


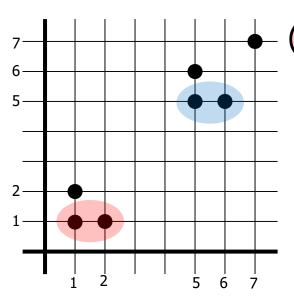
Centroid-link

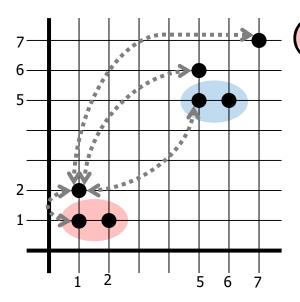






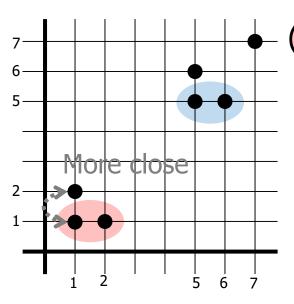


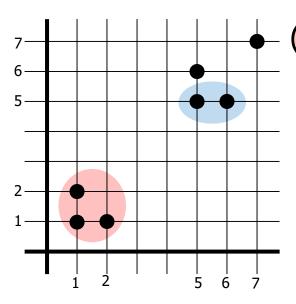


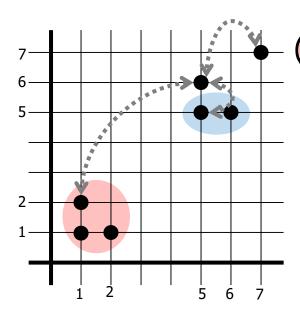


-(1,1)(2,1)(1,2)(5,5)(6,5)(5,6)(7,7)

Compare each distance from closest item in clusters

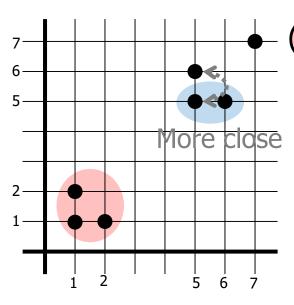


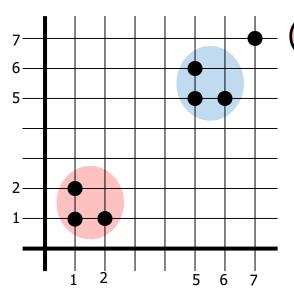


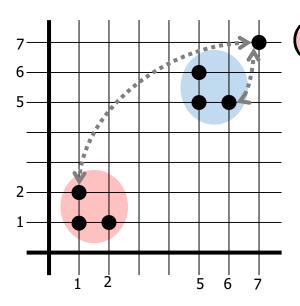


(1, 1)(2, 1)(1, 2)(5, 5)(6, 5)(5, 6)(7, 7)

Compare each distance from closest item in clusters

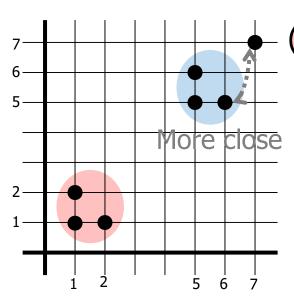


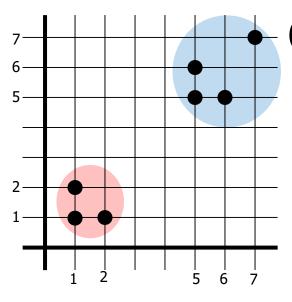


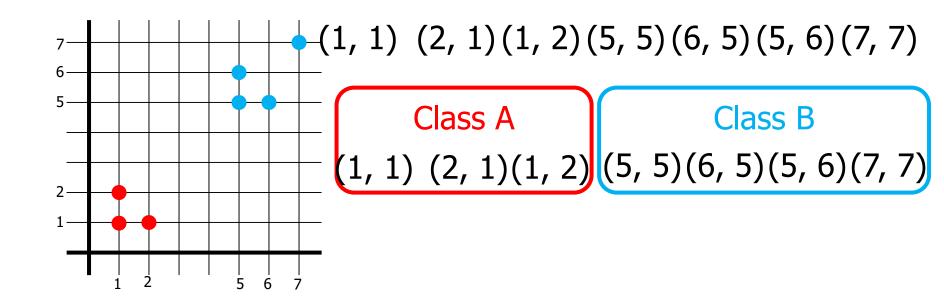


-(1, 1)(2, 1)(1, 2)(5, 5)(6, 5)(5, 6)(7, 7)

Compare each distance from closest item in clusters







Python - Hierarchical Clustering

Enumerate function

The iteration index is stored in it

```
for i, x in enumerate(('A', 'B', 'C')):
    print("i: {}, x: {}".format(i, x))
```

```
i: 0, x: A
```

i: 1, x: B

i: 2, x: C

```
from sklearn.cluster import AgglomerativeClustering
for i, linkage in enumerate(('single', 'complete')):
    clustering = AgglomerativeClustering(
        linkage=linkage, n_clusters=4)
    y_pred = clustering.fit_predict(X)
    plt.figure(i + 1, figsize=(5, 5))
    plt.scatter(X[:, 0], X[:, 1], c=y_pred, s=4, cmap=cmap)
    plt.title(linkage)
plt.show()
```

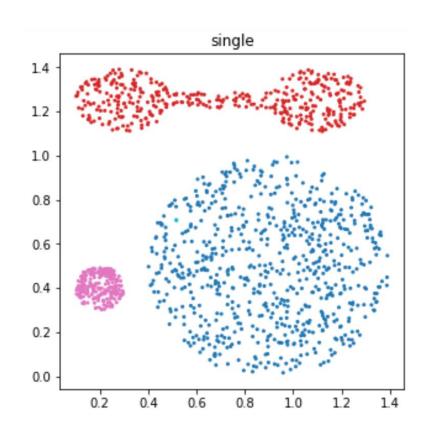
Link Types

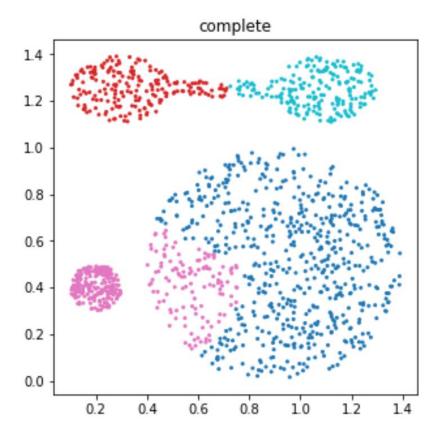
Iteration Index

```
from/sklearn.cluster import AgglomerativeClustering
for i, linkage in enumerate(('single', 'complete')):
    clustering = AgglomerativeClustering(
        linkage=linkage, n_clusters=4)
    y_pred = clustering.fit_predict(X)
    plt.figure(i + 1, figsize=(5, 5))
    plt.scatter(X[:, 0], X[:, 1], c=y_pred, s=4, cmap=cmap)
    plt.title(linkage)
plt.show()
```

```
from sklearn.cluster import AgglomerativeClustering
for i, linkage in enumerate(('single', 'complete')):
    clustering = AgglomerativeClustering(
        linkage=linkage, n_clusters=4)
    y_pred = clustering.fit_predict(X)
    plt.figure(i + 1, figsize=(5, 5))
    plt.scatter(X[:, 0], X[:, 1], c=y_pred, s=4, cmap=cmap)
    plt.title(linkage)
plt.show()
The index of each figure
```

The title of figure is named by the link type





Parameters

```
clustering = AgglomerativeClustering(
    linkage=linkage, n_clusters=4)
```

- n_clusters: the number of clusters to find
- linkage: the link type
 - Single
 - Complete
 - Average
 - Ward : minimize the variance of distances
- affinity: the distance metric
 - Default: "euclidean"

Clustering

Summary of Drawbacks of Traditional Methods

- Partitional algorithms split large clusters
- Centroid-based method splits large and non-hyperspherical clusters
 - Centers of subclusters can be far apart
- Single-link clustering algorithm is sensitive to outliers and slight change in position
 - Exhibits chaining effect on string of outliers
- Cannot scale up for large databases

DENSITY-BASED CLUSTERING

Density-Based Clustering Methods

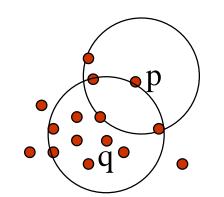
- Clustering based on density (local cluster criterion), such as density-connected points
- Major features:
 - Discover clusters of arbitrary shape
 - Handle noise
 - One scan
 - Need density parameters as termination condition
- Several interesting studies:
 - DBSCAN: Ester, et al. (KDD'96)
 - OPTICS: Ankerst, et al (SIGMOD'99).
 - DENCLUE: Hinneburg & D. Keim (KDD'98)
 - CLIQUE: Agrawal, et al. (SIGMOD'98) (more grid-based)

DBSCAN

 http://primo.ai/index.php?title=Density-Based_Spatial_Clustering_of_Applications_with_ Noise_(DBSCAN)

Density-Based Clustering: Basic Concepts

- Two parameters:
 - Eps: Maximum radius of the neighbourhood
 - MinPts: Minimum number of points in an Epsneighbourhood of that point
- $N_{Eps}(p)$: {q belongs to D | dist(p,q) \leq Eps}
- Directly density-reachable: A point p is directly density-reachable from a point q w.r.t. Eps, MinPts if
 - p belongs to $N_{Eps}(q)$
 - If $|N_{Eps}(q)| \ge MinPts$
 - q is a core point
 - Otherwise, q is a border point



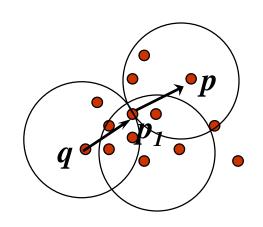
MinPts = 5

Eps = 1 cm

Density-Reachable and Density-Connected

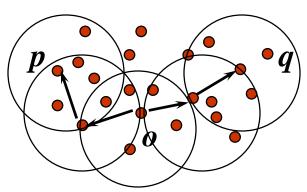
Density-reachable:

■ A point p is density-reachable from a point q w.r.t. Eps, MinPts if there is a chain of points $p_1, ..., p_n, p_1 =$ $q, p_n = p$ such that p_{i+1} is directly density-reachable from p_i



Density-connected

A point p is density-connected to a point q w.r.t. Eps, MinPts if there is a point o such that both, p and q are density-reachable from o w.r.t. Eps and MinPts

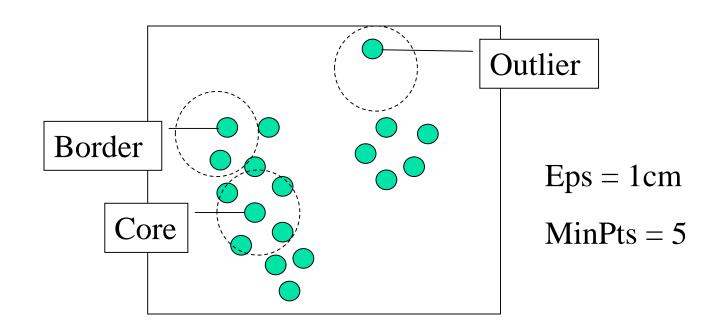


Definition: Density-based Clusters

- Given a set of points D, a cluster C is a densitybased cluster w.r.t. Eps and MinPts if
 - (Maximality) For every p_i, p_j in D, if p_i ∈C and p_j is density-reachable from p_i, p_j belongs to C
 - (Connectivity) For every p_i, p_j in C, p_i is densityconnected from p_j
- Outlier
 - If a point in p is a border point and does not belongs the any other clusters, p is a outlier

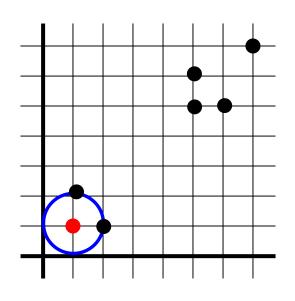
DBSCAN: Density-Based Spatial Clustering of Applications with Noise

- Relies on a density-based notion of cluster: A cluster is defined as a maximal set of density-connected points
- Discovers clusters of arbitrary shape in spatial databases with noise



DBSCAN: The Algorithm

- Arbitrary select a point p
- Retrieve all points density-reachable from p w.r.t. Eps and MinPts
- If p is a core point, a cluster is formed
- If p is a border point, no points are density-reachable from p and DBSCAN visits the next point of the database
- Continue the process until all of the points have been processed



Epsilon = 1 MinNumPoints = 3

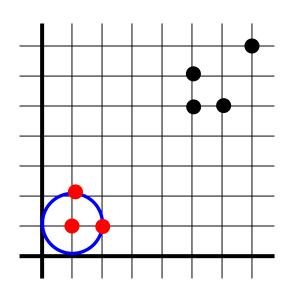
Start from (1,1) point

Class A

(1,1)

Unclassified

(5,5)(5,6)



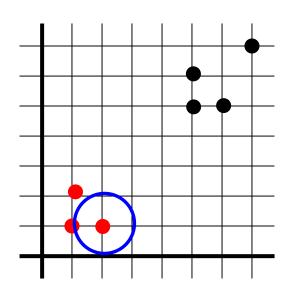
Start from (1,1) point

Class A

(1,1)(1,2)(2,1)

Unclassified

(5,5)(5,6) (6,5)(7,7)



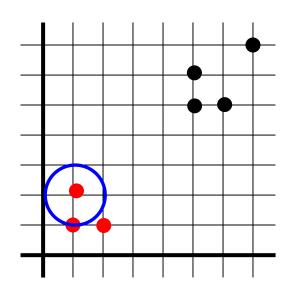
Start from (2,1) point

Class A

$$(1,1)(1,2)$$

 $(2,1)$

Unclassified



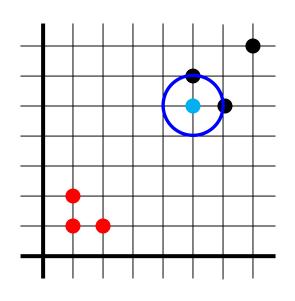
Start from (1,2) point

Class A

$$(1,1)(1,2)$$

 $(2,1)$

Unclassified



Start from (5,5) point

Class A

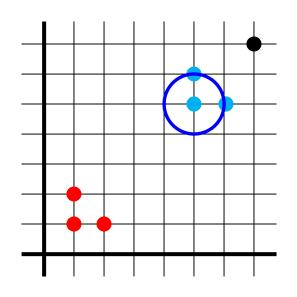
(1,1)(1,2)(2,1)

Class B

(5,5)

Unclassified

(5,6) (6,5)(7,7)



Start from (5,5) point

Class A

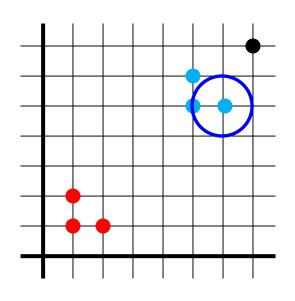
(1,1)(1,2) (2,1)

Class B

(5,5) (5,6) (6,5)

Unclassified

(7,7)



Start from (6,5) point

Class A

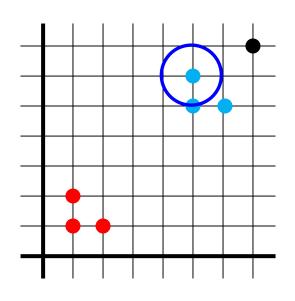
(1,1)(1,2) (2,1)

Class B

(5,5) (5,6) (6,5)

Unclassified

(7,7)



Start from (5,6) point

Class A

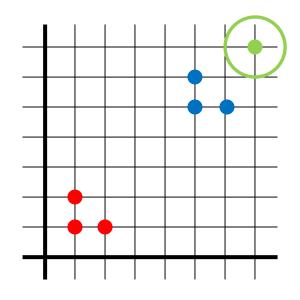
(1,1)(1,2) (2,1)

Class B

(5,5) (5,6) (6,5)

Unclassified

(7,7)



(5,6) point: Border Point

Class A

(1,1)(1,2)

(2,1)

Class B

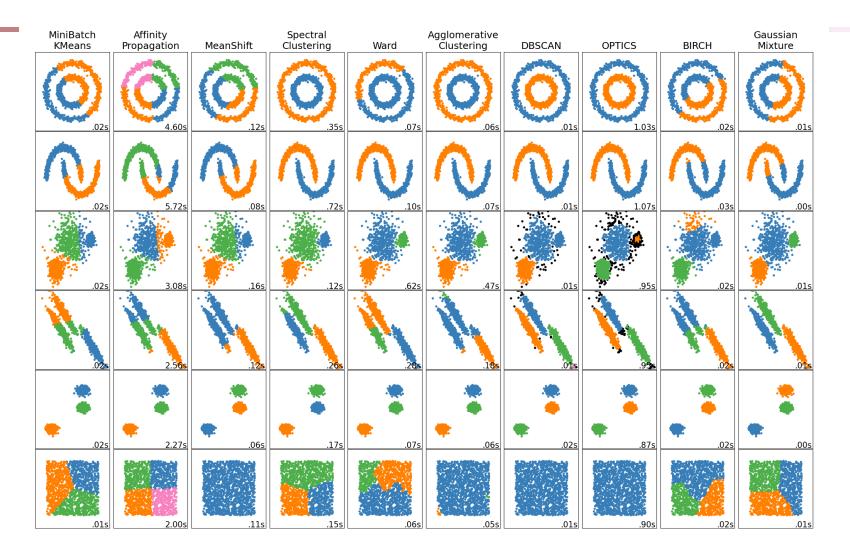
(5,5)(6,5) (5,6)

Class C

(7,7)

→ Outlier

Comparing different clustering algorithms



Python - DBSCAN

```
from sklearn.cluster import DBSCAN
dbscan = DBSCAN(eps=0.05, min samples=20)
y_pred = dbscan.fit predict(X)
print(y_pred[:10])

[ 0 4 -1 -1 -1 -1 -1 -1 -1 -1]

Maximum radius of the neighborhood
The number of points in a neighborhood to be a core point
```

```
from sklearn.cluster import DBSCAN
dbscan = DBSCAN(eps=0.05, min samples=20)
y pred = dbscan.fit predict(X)
print(y pred[:10])
      4 -1 -1 -1 -1 -1 -1 -1 ]
                            Perform clustering and output the
                            cluster index for each data point
        Outliers are indexed as -1
```

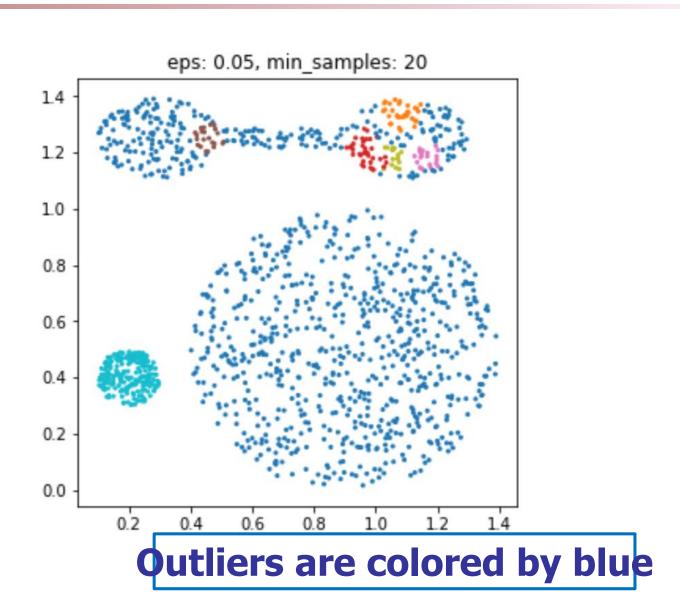
Pairs of (eps, min_samples)

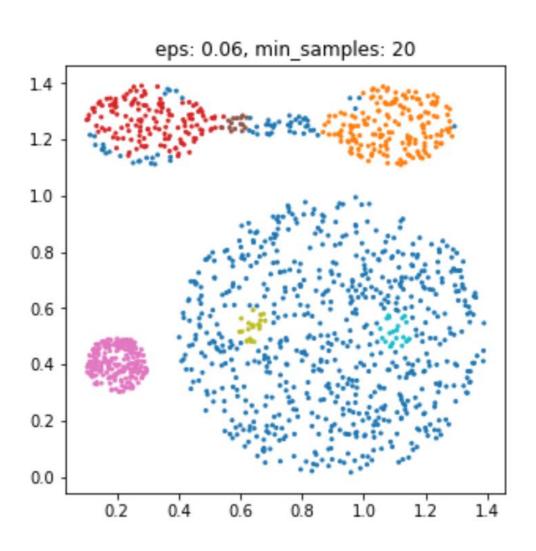
Iterate over 4 pairs of (eps, min_samples)

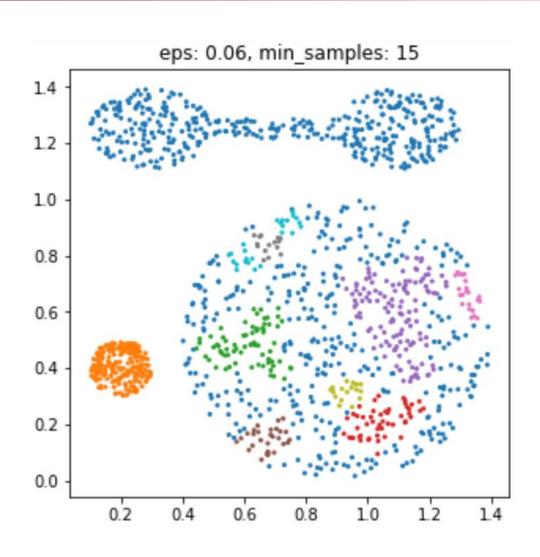
Parameters

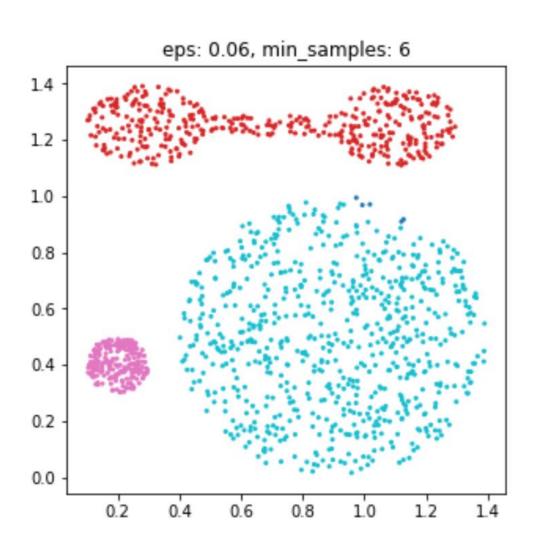
```
dbscan = DBSCAN(
    eps=eps,
    min samples=min samples)
```

- eps: maximum radius of the neighborhood
- min_samples: the number of points in a neighborhood to be a core point
- metric: the distance metric (default: "euclidean")









References (1)

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References (2)

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Homework

- K means 와 DBSCAN 알고리즘 비교
- 제출물
 - Code
 - Report 1페이지 이내
 - Plot 한 개 이상 포함
- Due:10월 7일 23:59