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## DalitzPlot

This Julia package is designed for high-energy physics applications, originally in visualizing and analyzing particle decays. It consists of the following subpackages:

- **Xs** : Provides tools for calculation cross section and creating Dalitz plots, which are essential for visualizing three-body - decays of particles. Users can specify amplitudes to generate these plots.
- **GEN** : Stands for General Event Generation. This subpackage is used for generating events, allowing users to simulate particle interactions and decays.
- **QFT** : Short for Quantum Field Theory. This subpackage includes functions for calculating spinor or polarized vectors with momentum and spin, gamma matrices, and other related calculations.
- **qBSE** : Refers to the Quasipotential Bethe-Salpeter Equation. This subpackage provides tools for solving the Bethe-Salpeter equation, which is used in the study of bound states in quantum field theory.

Note: This package is designed for phenomenological studies on the theoretical side. For experimental data analysis, please refer to other tools.

# Installation

To install the "DalitzPlot" package, you can follow the standard Julia package manager procedure. Open Julia and use the following commands:

Using the Julia REPL

```
Pkg.add("DalitzPlot")
```

Alternatively, if you want to install it directly from the GitHub repository:

Using the Julia REPL:

```
import Pkg
Pkg.add(url="https://github.com/junhe1979/DalitzPlot.jl")
```

These commands will install the "DalitzPlot" package and allow you to use it in your Julia environment.

# Usage

After installation, the package can be used as:

```
using DalitzPlot
```

To use the subpackages:

```
using DalitzPlot.Xs
using DalitzPlot.GEV
using DalitzPlot.QFT
using DalitzPlot.qBSE
```

# Xs Package: for cross section and Dalitz plot

The cross section, denoted by  $d\sigma$ , can be expressed in terms of amplitudes,  $\mathcal{M}$ , as follows:

$$d\sigma = F |\mathcal{M}|^2 \frac{1}{S} d\Phi = (2\pi)^{4-3n} F |\mathcal{M}|^2 \frac{1}{S} dR$$

Here,  $dR = (2\pi)^{3n-4} d\Phi = \prod_i \frac{d^3 k_i}{2E_i} \delta^4(\sum_i k_i - P)$  represents the Lorentz-invariant phase space for  $n$  particles, and it is generated using the Monte-Carlo method described in Ref. [F. James, CERN 68-12].

The flux factor  $F$  for the cross section is given by:  $F = \frac{1}{2E2E'v_{12}} = \frac{1}{4[(p_1 \cdot p_2)^2 - m_1^2 m_2^2]^{1/2}} \frac{|p_1 \cdot p_2|}{p_1^0 p_2^0}$ . In the laboratory or center of mass frame, the relation  $\vec{p}_1^2 \vec{p}_2^2 = (\vec{p}_1 \cdot \vec{p}_2)^2$  is utilized. In the laboratory frame, the term  $\frac{|p_1 \cdot p_2|}{p_1^0 p_2^0}$  simplifies to 1.

Additionally, if a boson or zero-mass spinor particle is replaced with a non-zero mass spinor particle, the factor  $1/2$  is replaced with the mass of the particle,  $m$ .

The total symmetry factor  $S$  is given by  $\prod_i m_i!$  if there are  $m_i$  identical particles.

For decay width, the flux factor is modified to  $F = \frac{1}{2E}$ .

## Define amplitudes with factors for the calculation

Users are required to supply amplitudes with factors  $(2\pi)^{4-3n} F |\mathcal{M}|^2 \frac{1}{S}$  within the function, named `amp` here.

We can take it as 1.

```
amp(tecm, kf, ch, para)=1.
```

Define more intricate amplitudes for a 2->3 process.

This function, named `amp`, calculates amplitudes with factors for a 2->3 process. The input parameters are:

- `tecm` : Total energy in the center-of-mass frame.

- `kf` : Final momenta generated.
- `ch` : Information about the process (to be defined below).
- `para` : Additional parameters.

Users are expected to customize the amplitudes within this function according to their specific requirements.

```
function amp(tecm, kf, ch, para)
    # get kf as momenta in the center-of-mass ,
    #k1,k2,k3=getkf(kf)
    #get kf as momenta in laboratory frame
    k1, k2, k3 = getkf(para.p, kf, ch)

    # Incoming particle momentum
    # Center-of-mass frame: p1 = [p 0.0 0.0 E1]
    #p1, p2 = pcm(tecm, ch.mi)
    # Laboratory frame
    p1, p2 = plab(para.p, ch.mi)

    #flux
    #flux factor for cross section in Laboratory frame
    fac = 1 / (4 * para.p * ch.mi[2] * (2 * pi)^5)

    k12 = k1 + k2
    s12 = cdot(k12, k12)
    m = 3.2
    A = 1e9 / (s12 - m^2 + im * m * 0.1)

    total = abs2(A) * fac * 0.389379e-3

    return total
```

## Define the masses of initial and final particles

The mass of initial and final particles is specified in a NamedTuple (named `ch` here) with fields `mi` and `mf`.

Particle names can also be provided for PlotD as `namei` and `namef`.

The function for amplitudes with factors is saved as `amp` .

Example usage:

```
ch = (mi=[mass_i_1, mass_i_2], mf=[mass_f_1, mass_f_2, mass_f_3], namei=["pi1", "pi2"])
```

Make sure to replace `mass_i_1` , `mass_i_2` , `mass_f_1` , `mass_f_2` , and `mass_f_3` with the actual masses of the particles (1.0, 1.0, 1.0, 2.0, 3.0 here).

## Define the momentum or total energy

Momentum in the Laboratory frame and transfer it to the total energy in the center-of-mass frame.

Example usage:

```
p_lab = 20.0
tecm = pcm(p_lab, ch.mi)
```

## Calculate

Calculate the cross section and related spectra using the GENEV function.

The function `Xsection` takes the momentum of the incoming particle in the Laboratory frame (`p_lab`), the information about the particles (`ch`), the axes representing invariant masses (`axes`), the total number of events (`nevtot`), the number of bins (`Nbin`), and additional parameters (`para`). The function uses the `plab2pcm` function to transform the momentum from the Laboratory frame to the center-of-mass frame.

Example usage:

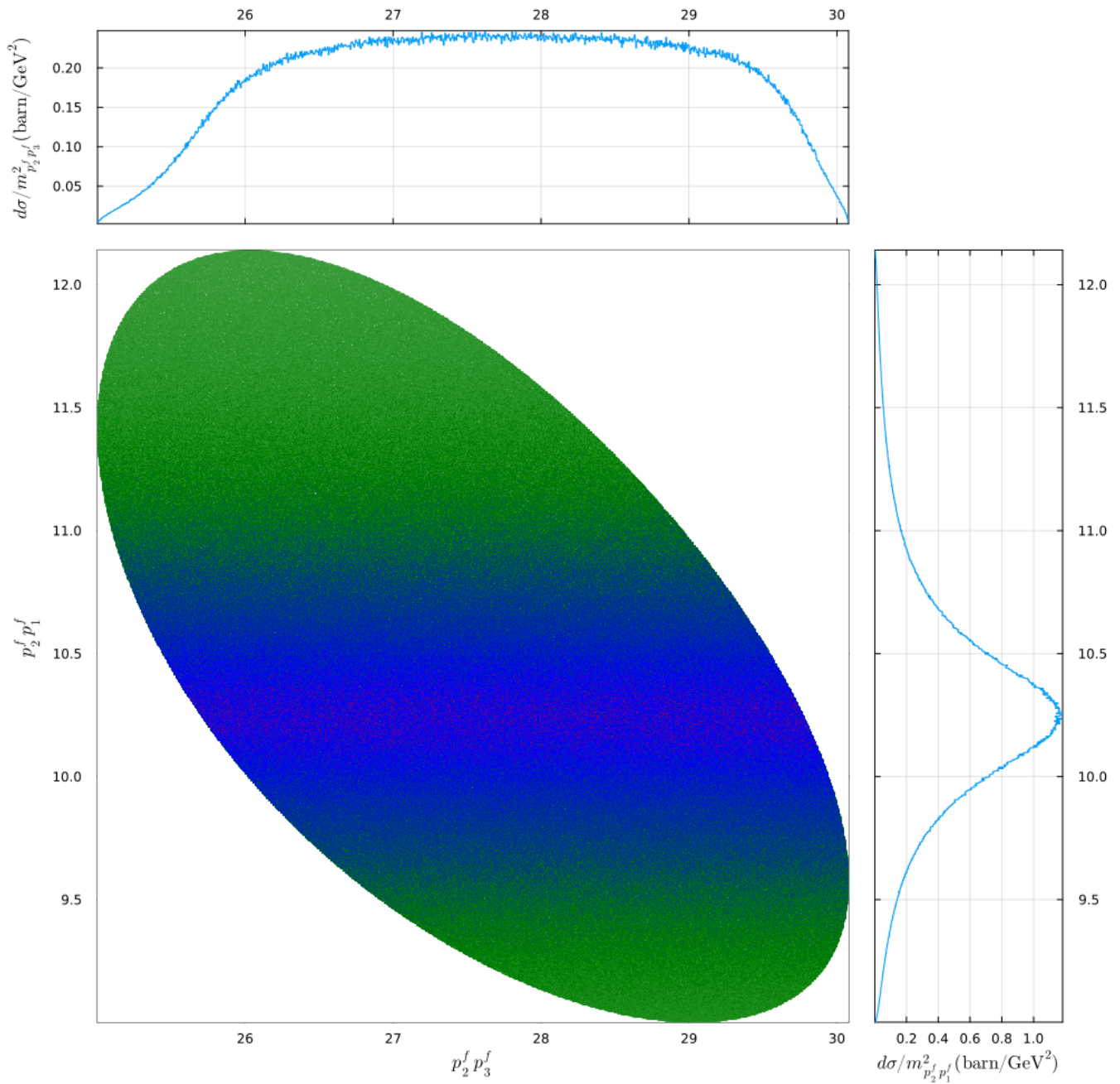
```
res = Xsection(plab2pcm(p_lab, ch.mi), ch, axes=[23, 21], nevtot=Int64(1e7), Nbin=500, para=)
```

The results are stored in the variable `res` as a `NamedTuple` . Specifically, `res.cs0` corresponds to the total cross section, `res.cs1` represents the invariant mass spectrum, and

`res.cs2` captures the data for the Dalitz plot.

## Plot Dalitz Plot

```
plotD(res)
```



# GEN Package: for Generating Events

The GEN package is used for generating events for cross-section calculations and Dalitz plots. The Lorentz-invariant phase space used here is defined as:

$$dR = (2\pi)^{3n-4} d\Phi = \prod_i \frac{d^3 k_i}{2E_i} \delta^4(\sum_i k_i - P)$$

for  $n$  particles. The events are generated using the Monte-Carlo method described in Ref. [F. James, CERN 68-12].

The primary function provided by this package is `GENEV`, which can be used as follows:

```
PCM, WT=GENEV(tecm,EM)
```

- Input: total momentum in center of mass frame `tecm`, and the mass of particles `EM`.
  - `tecm`: a `Float64` value representing the total momentum in the center of mass frame.
  - `EM`: a `Vector{Float64}` containing the masses of the particles.
- Output: the momenta of the particles `PCM`, and a weight `WT`.
  - `PCM`: a `StaticArrays @MArray zeros(Float64, 5, 18)` storing the momenta of the particles. Note that at most 18 particles can be considered.
  - `WT`: `Float64` value representing the weight for this event.

# QFT Package: for Numerical Calculation of Feynman Rules