1.

(a) (3 pts) An acyclic (or approximately acyclic) directed network

食物鏈,生物學家調查,人為控制外來種或保育瀕臨絕種的動物

(b) (3 pts) A cyclic directed network

神經系統, vertex 是神經元, edge 是神經突觸

(c) (3 pts) A tree (or approximate tree)

族譜,區公所取得,研究遺傳性疾病

(d) (3 pts) A planar (or approximately planar) network

道路網;GOOGLE MAP 都有用顏色標示路段為暢通或堵塞,哪些路段在尖峰時間易堵塞

(e) (3 pts) A bipartite network

演員和電影,IMDB,什麼演員會演什麼類型的電影

(f) (3 pts) A temporal network (or sequence of edges)

流行病的傳染;透過健保單位收集資料;若有一個疾病發生,可能會在哪些區域較

2.

(a)

| Α | 1 | 2 | 3 | 4 | 5 |
|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 1 |
| 2 | 1 | 0 | 1 | 1 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 |
| 4 | 0 | 1 | 1 | 0 | 1 |
| 5 | 0 | 0 | 0 | 1 | 0 |

(b)

| А | |
|---|-------------------|
| 1 | {5,1} |
| 2 | {1,1},{3,1},{4,1} |
| 3 | |
| 4 | {2,1},{3,1},{5,1} |
| 5 | {4,1} |

(c)

adjacency matrix(上)

| Α | 1 | 2 | 3 | 4 | 5 |
|---|---|---|---|---|---|
| | | | _ | | _ |

| 1 | 0 | 1 | 1 | 0 | 0 |
|---|---|---|---|---|---|
| 2 | 1 | 0 | 1 | 0 | 0 |
| 3 | 1 | 1 | 0 | 1 | 0 |
| 4 | 0 | 0 | 1 | 0 | 1 |
| 5 | 0 | 0 | 0 | 1 | 0 |

adjacency matrix(下)

| А | 1 | 2 | 3 | 4 | 5 | 6 |
|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 1 | 1 | 1 | 1 |
| 2 | 0 | 0 | 0 | 0 | 1 | 0 |
| 3 | 1 | 0 | 0 | 0 | 1 | 0 |
| 4 | 1 | 0 | 0 | 0 | 0 | 1 |
| 5 | 1 | 1 | 1 | 0 | 0 | 0 |
| 6 | 1 | 0 | 0 | 1 | 0 | 0 |

(d) adjacency matrix

| Α | 1 | 2 | 3 | а | b | 6 | 7 |
|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| 2 | 0 | 0 | 0 | 1 | 1 | 0 | 0 |
| 3 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| а | 1 | 1 | 0 | 0 | 1 | 1 | 0 |
| b | 0 | 1 | 1 | 1 | 0 | 1 | 1 |
| 6 | 0 | 0 | 0 | 1 | 1 | 0 | 0 |
| 7 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |

a:(1,1,0,0,1,1,0)

b:(0,1,1,1,0,1,1)

$$\cos\theta = \frac{1 \times 1 + 1 \times 1}{\sqrt{5}\sqrt{4}} = 0.4472$$