Curriculum Vitae of Jun Liu

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RESEARCH INTERESTS

- PDE-Constrained Optimization and Optimal Control, Numerical PDEs, Numerical Linear Algebra.
- Inverse PDE Problems, Medical Imaging, Mathematical Biology and Oncology, Numerical Optimization.
- Sinc Methods, Finite Difference Methods, Multigrid Method, Domain Decomposition Method.

EMPLOYMENT

- Assistant Professor, Department of Mathematics and Statistics, Southern Illinois University Edwardsville, 8/2017-now.
- Assistant Professor, Department of Mathematics and Statistical Sciences, Jackson State University, 8/2015-8/2017.
- Teaching/Research Assistant, Department of Mathematics, Southern Illinois University Carbondale, 8/2010-8/2015.
- Software Engineer (Java), China National Software and Service Co., Ltd., Guangzhou, China, 7/2004-8/2007.

EDUCATION

- Ph.D., Computational Mathematics, Southern Illinois University Carbondale (SIUC), USA, 8/2010-8/2015.
- M.S., Computational Mathematics, South China Normal University, China, 9/2007-7/2010.
- B.S., Information and Computing Science, Guangdong University of Technology, China, 9/2000-6/2004.

TEACHING EXPERIENCE

Undergraduate courses:

- Introduction to Contemporary Mathematics
- College Algebra
- Business Calculus
- Calculus I,II,III (with Mathematica)
- Linear Algebra
- Engineering Mathematics
- Ordinary Differential Equations
- Partial Differential Equations

Graduate courses:

- Real Analysis
- Numerical Analysis
- Engineering Numerical Analysis
- Numerical Methods (I, II)
- Numerical Linear Algebra
- Numerical Methods for PDEs (course webpage)
- Theory of Ordinary Differential Equations
- Partial Differential Equations & Fourier Series

STUDENTS ADVISING at SIUE

- 2018-2019, Kelsey Cutler, Thesis Project Title: Compare Methods for Improving FISTA Convergence in Optimization.
- 2018-2019, Alexander Warthen, Senior Project Title: FISTA for Computed Tomography and Image Deblurring.
- 2017-2018, Breanna Guppy, Senior Project Title: Filtered Back Projection vs Algebraic Iterative Reconstruction.

GRANTS

- 1. Co-PI (Former PI), "CBMS Conference: Computational Methods in Optimal Control", NSF DMS-1743826, 2018.
- 2. PI, "Numerical Algorithms for PDE Dynamical Models of Metastatic Cancers", SIUE Internal STEP Grant, 2018-2019.

SUBMITTED MANUSCRIPTS (Under Review or Revision)

- 1. Ruimin Feng, Jun Liu, Yongming He, and Shengnan Chen, A radial-flow transient technique for fast permeability measurements of sorptive reservoirs: Part 1 - Mathematical modeling and numerical analysis, 2020.
- 2. Ruimin Feng, Jun Liu, Yongming He, and Shengnan Chen, A radial-flow transient technique for fast permeability measurements of sorptive reservoirs: Part 2 - Experimental data interpretation, 2020.
- 3. Jun Liu and Xiang-Sheng Wang, Should the general public reserves all face masks for the healthcare workers during the COVID-19 outbreak in the United States?, 2020.
- 4. Weiwei Hu and Jun Liu, Sampled-data based Failure Rate Identification for a Multi-state Reparable System, 2020.
- 5. **Jun Liu** and Shu-Lin Wu, A fast block α -circulant preconditioner for all-at-once systems from wave equations, 2019.

- 6. Koung Hee Leem, **Jun Liu**, and George Pelekanos, *A numerical comparison of qualitative algorithms for solving 2D inverse elastic scattering problems*, 2019.
- 7. **Jun Liu**, Yan Qi, Na Cui, and Dave Bergner, *Optimized Route to Clear Diverging Diamond Interchange Using Discrete Optimization Method*, 2019.
- 8. Weiwei Hu and **Jun Liu**, Optimal Bilinear Control of a Reparable System, 2019.
- 9. Ruimin Feng, Rohit Pandey, **Jun Liu**, and Shengnan Chen, *A modified transient technique for porosity and permeability determination in tight formations: experimental investigation and numerical simulation*, 2019.

REFEREED JOURNAL PUBLICATIONS

- 1. Shu-Lin Wu and **Jun Liu**, A parallel-in-time block-circulant preconditioner for optimal control of wave equations, SIAM Journal on Scientific Computing, 42(3), A1510-A1540, 2020.
- 2. He Yang and **Jun Liu**, A qualitative deep learning method for inverse scattering problems, Applied Computational Electromagnetics Society Journal, 35(2), pp. 153-160, 2020.
- 3. **Jun Liu** and Mingqing Xiao, *The Quasi-Boundary Value Methods for Regularizing Backward Parabolic Equation under the Optimal Control Framework*, **Inverse Problems**, 35, 124003 (29pp), 2019. DOI link.
- 4. Ruimin Feng, Shengnan Chen, Steven Bryant, and **Jun Liu**, *Stress-dependent permeability measurement techniques for unconventional gas reservoirs: Review, evaluation, and application*, **Fuel**, 256, 115987 (17pp), 2019.
- 5. Koung Hee Leem, **Jun Liu**, and George Pelekanos, *An Extended Direct Factorization Method for Inverse Scattering with Limited Aperture Data*, **Inverse Problems in Science and Engineering**, accepted, 2019. DOI link
- 6. Jianliang Tang, **Jun Liu**, and Mingqing Xiao, *Direct Reconstruction of Initial States of Wave Equation via Boundary Observation*, **Wave Motion**, 91, 102383 (12pp), 2019. DOI link
- 7. **Jun Liu** and Xiang-Sheng Wang, *Numerical optimal control of a size-structured PDE model for metastatic cancer treatment*, **Mathematical Biosciences**, 314, pp. 28–42, 2019. DOI link
- 8. **Jun Liu** and John W. Pearson, *Parameter-Robust Preconditioning for the Optimal Control of the Wave Equation*, **Numerical Algorithms**, accepted, 2019. DOI link.
- 9. Jun Liu, Two Fast Finite Difference Schemes for Elliptic Dirichlet Boundary Control Problems, Journal of Applied Mathematics and Computing, 61, pp. 481–503, 2019. DOI link.
- 10. **Jun Liu** and Zhu Wang, *Non-commutative Discretize-then-Optimize Algorithms for Elliptic PDE-Constrained Optimal Control Problems*, **Journal of Computational and Applied Mathematics**, 362, pp. 596-613, 2019. DOI link.
- 11. Koung Hee Leem, **Jun Liu**, and George Pelekanos, *An Adaptive Quadrature-based Factorization Method for Inverse Acoustic Scattering Problems*, **Inverse Problems in Science and Engineering**, 27 (3), pp. 299-316, 2019.
- 12. Koung Hee Leem, **Jun Liu**, and George Pelekanos, *Efficient Adaptive Qualitative Methods for 3D Inverse Scattering Problems*, **Applied Computational Electromagnetics Society Journal** (electronic), 33(10), pp. 1100–1105, 2018.
- 13. Koung Hee Leem, **Jun Liu**, and George Pelekanos, *Two Direct Factorization Methods for Inverse Scattering Problems*, **Inverse Problems**, 34(12), 125004 (26pp), 2018.
- 14. Ruimin Feng, **Jun Liu**, Shengnan Chen, and Steven Bryan, *Effect of gas compressibility on permeability measure-ment in coalbed methane formations: experimental investigation and flow modeling*, **International Journal of Coal Geology**, 198, pp. 144–155, 2018.
- 15. William W. Hager, **Jun Liu**, Subhashree Mohapatra, Anil V. Rao, and Xiang-Sheng Wang, *Convergence Rate for a Gauss Collocation Method Applied to Constrained Optimal Control*, **SIAM Journal on Control and Optimization**, 56(2), pp. 1386–1411, 2018.
- 16. **Jun Liu** and Zhu Wang, *Efficient Time Domain Decomposition Algorithms for Parabolic PDE-Constrained Optimization Problems*, **Computers and Mathematics with Applications**, 75(6), pp. 2115-2133, 2018.
- 17. Buyang Li, Jun Liu, and Mingqing Xiao, A New Multigrid Method for Unconstrained Parabolic Optimal Control Problems, Journal of Computational and Applied Mathematics, 326, pp. 358–373, 2017.
- 18. Ruimin Feng, **Jun Liu**, and Satya Harpalani, *Optimized pressure pulse-decay method for laboratory estimation of gas permeability of sorptive reservoirs: Part 1: Background and numerical analysis*, **Fuel**, 191, pp. 555–564, 2017.
- 19. Ruimin Feng, Satya Harpalani, and **Jun Liu**, *Optimized pressure pulse-decay method for laboratory estimation of gas permeability of sorptive reservoirs: Part 2: Experimental study*, **Fuel**, 191, pp. 565–573, 2017.
- 20. **Jun Liu**, Brittany D. Froese, Adam M. Oberman, and Mingqing Xiao, *A multigrid scheme for 3D Monge-Ampère equations*, **International Journal of Computer Mathematics**, 94(9), pp. 1850–1866, 2017.
- 21. **Jun Liu** and Mingqing Xiao, *A Leapfrog Multigrid Algorithm for the Optimal Control of Parabolic PDEs with Robin Boundary Conditions*, **Journal of Computational and Applied Mathematics**, 307, pp. 216–234, 2016.
- 22. **Jun Liu**, Yu Huang, Haiwei Sun, and Mingqing Xiao, *Numerical methods for weak solution of wave equation with van der Pol type nonlinear boundary conditions*, **Numerical Methods for Partial Differential Equations**, 32(2), pp. 373–398, 2016.
- 23. **Jun Liu** and Mingqing Xiao, *A leapfrog semi-smooth Newton multigrid method for semilinear parabolic optimal control problems*, **Computational Optimization and Applications**, 63(1), pp. 69–95, 2016.
- 24. **Jun Liu** and Mingqing Xiao, *A new semi-smooth Newton multigrid method for control-constrained semi-linear elliptic PDE problems*, **Journal of Global Optimization**, 64(3), pp. 451–468, 2016.

- 25. Buyang Li, **Jun Liu**, and Mingqing Xiao, *A fast and stable preconditioned iterative method for optimal control problem of wave equations*, **SIAM Journal on Scientific Computing**, 37(6), pp. A2508–A2534, 2015.
- 26. **Jun Liu** and Haiwei Sun, *A fast high-order Sinc-based algorithm for pricing options under jump-diffusion processes*, **International Journal of Computer Mathematics**, 91(10), pp. 2163–2184, 2014.
- 27. Xuejun Gao, Tingwen Huang, Yu Huang, Jun Liu, and Mingqing Xiao, Observer design for axial flow compressor, ASME Journal of Dynamic Systems, Measurement, and Control, 136(5), 051017-1:12, 2014.
- Spike T. Lee, Jun Liu, and Haiwei Sun, Combined compact difference scheme for linear second-order partial differential equations with mixed derivative, Journal of Computational and Applied Mathematics, 264, pp. 23–37, 2014.
- 29. **Jun Liu**, and Mingqing Xiao, *Rank-one characterization of joint spectral radius of finite matrix family*, **Linear Algebra and its Applications**, 438(8), pp. 3258–3277, 2013.
- 30. Xiongping Dai, Yu Huang, **Jun Liu**, and Mingqing Xiao, *The finite-step realizability of the joint spectral radius of a pair of d-by-d matrices one of which being rank-one*, **Linear Algebra and its Applications**, 437(7), pp. 1548–1561, 2012
- 31. Xiaoshan Chen, Wen Li, Xiaojun Chen, and **Jun Liu**, *Structured backward errors for generalized saddle point systems*, **Linear Algebra and its Applications**, 436(9), pp. 3109–3119, 2012.
- 32. Liying Sun and Jun Liu, Constraint preconditioning for nonsymmetric indefinite linear systems, Numerical Linear Algebra with Applications, 17(4), pp. 677–689, 2009.

REFEREED CONFERENCE PUBLICATIONS

- 1. William W. Hager, **Jun Liu**, Subhashree Mohapatra, Anil V. Rao, and Xiang-Sheng Wang, *A pseudospectral method for optimal control based on collocation at the Gauss points*, Proceedings of the 57th IEEE Conference on Decision and Control (CDC), 2018.
- 2. Koung Hee Leem, **Jun Liu**, and George Pelekanos, *An Adaptive Factorization Method for Inverse Scattering Problems*, 2018 International Applied Computational Electromagnetics Society (ACES) Symposium, Denver, CO, 2018.
- 3. **Jun Liu**, Buyang Li, and Mingqing Xiao, *An Effective Computational Scheme for the Optimal Control of Wave Equations*, NOLCOS 2016, IFAC-PapersOnLine Vol. 49 (18), pp. 891–896, 2016.
- 4. Buyang Li, **Jun Liu**, and Mingqing Xiao, *Leapfrog multigrid methods for parabolic optimal control problems*, Proceedings of the 27th Chinese Control and Decision Conference, pp. 137–143, 2015. (Finalists for Zhang Si-Ying Outstanding Youth Paper Award).
- 5. **Jun Liu**, Tingwen Huang, and Mingqing Xiao, *A semismooth Newton multigrid method for constrained elliptic optimal control problems*, Advances in Global Optimization, Springer Proceedings in Mathematics & Statistics Vol. 95, pp. 397–405, 2015.
- 6. **Jun Liu** and Mingqing Xiao, *A new semi-smooth Newton multigrid method for parabolic PDE optimal control problems*, Proceedings of the 53rd IEEE Conference on Decision and Control, pp. 5568–5573, 2014.
- 7. **Jun Liu**, Yu Huang, Haiwei Sun, and Mingqing Xiao, *High-order numerical methods for wave equations with van der Pol type boundary conditions*, Proceedings of the SIAM Conference on Control and Its Applications, pp. 144–151, 2013.
- 8. **Jun Liu** and Mingqing Xiao, *Computation of joint spectral radius for network model associated with rank-one matrix set*, Neural Information Processing, Springer Lecture Notes in Computer Science, Vol. 7665, pp. 356–363, 2012.
- 9. Xuejun Gao, Tingwen Huang, **Jun Liu**, and Mingqing Xiao, *Local observer for axial flow aeroengine compressors*, Proceedings of the 10th World Congress on Intelligent Control and Automation, pp. 2233–2238, 2012.
- 10. **Jun Liu** and Haiwei Sun, *Sinc-Galerkin method for the option pricing under jump-diffusion model*, East-West Journal of Mathematics, pp. 317–327, 2009.

THESES AND RESEARCH REPORTS

- 1. **Jun Liu**, *New Computational Methods for Optimal Control of Partial Differential Equations*, Ph.D. Dissertation, 150 pages, Southern Illinois University Carbondale, 2015.
- 2. Bruce Bugbee, Brianna Cash, **Jun Liu**, Helen Parks, Wei Qi, Deling Wei, and Xi Zhang, *Uncertainty-enabled design of an active MEMS valve for a high-pressure micro gas analyzer*, Proceedings of the 18th Industrial Math and Statistical Modeling Workshop in Statistical and Applied Mathematical Sciences Institute (SAMSI), pp. 1–40, 2012.
- 3. **Jun Liu**, Efficient preconditioners for the Helmholtz equation discretized by combined compact difference method, Master's Thesis, 70 pages, South China Normal University, 2010.
- 4. **Jun Liu**, Insight and outlook of the degree/diameter problem, Bachelor's Thesis, 54 pages, Guangdong University of Technology, 2004.

ACADEMIC HONORS AND TRAVEL AWARDS

• SIAM Early Career Travel Award for SIAM Conference on Control and Its Applications (CT17), July, 2017.

- Funded travel to AIM REUF workshop at ICERM, June, 2017.
- Funded travel to IMA Optimization Course, August, 2016.
- Funded travel to AIM REUF workshop on the Mathematics of Data at Duke university, July, 2016.
- Funded travel to IMA workshop on Control of Infinite-dimensional Systems, March, 2016.
- IEEE Student Travel Award for the 53rd IEEE Conference on Decision and Control, December, 2014.
- Dissertation Research Assistantship Award, Southern Illinois University, 2014 Fall-2015 Spring (9 months).
- Funded travel to IMA Control Course, June, 2014.
- SIAM Student Travel Award for SIAM Conference on Optimization, May, 2014.
- Doctoral Fellowship Award, Southern Illinois University, 2013 Fall-2014 Summer (11 months).
- Fully funded travel to participate the SAMSI Industrial Math/Stat Modeling Workshop, July, 2012.
- Excellence Award for Master's Thesis, South China Normal University, July, 2010.
- Innovation Award for Bachelor's Thesis, Guangdong University of Technology, July, 2004.
- 3rd, 2nd, and 3rd Prize in the Undergraduate Math Contest in Modeling, Guangdong, 2001-2003.
- Top 5 Finalist in the Entrepreneurial Design Contest, Guangdong University of Technology, 2001.

RESEARCH PRESENTATIONS

- "Optimal control of a continuously size-structured model for the growth and treatment of metastatic cancer", Invited Minisymposium Talk, The 1st Annual Meeting of SIAM Texas-Louisiana Section, October, 2018.
- "An Adaptive Factorization Method for Inverse Scattering Problems", Colloquium Talk, Department of Mathematics and Statistics, Southern Illinois University Edwardsville (SIUE), April 6, 2018.
- "An Adaptive Factorization Method for Inverse Scattering Problems", 2018 International Applied Computational Electromagnetics Society (ACES) Symposium, Denver, Colorado, USA, March 24-29, 2018.
- "Efficient Numerical Methods for PDE-Constrained Optimization", Applied Mathematics Seminar Talk, Department of Mathematics, University of Louisiana at Lafayette, November, 2017.
- "Efficient Time Domain Decomposition Algorithms for PDE-constrained Optimization Problems", Invited Minisymposium Talk, The 3rd Annual Meeting of SIAM Central States Section, Fort Collins, CO, October, 2017.
- "Efficient Time Domain Decomposition Algorithms for Time-dependent PDE-constrained Optimization Problems", SIAM Conference on Control and Its Applications (CT17), Pittsburgh, PA, July, 2017.
- "Time domain decomposition algorithms for Parabolic PDE-Constrained Optimization", Langenhop Lecture and Applied Mathematics Conference, Department of Mathematics, Southern Illinois University Carbondale, May, 2017.
- "Efficient Numerical Methods for PDE-Constrained Optimization Problems", Applied and Computational Mathematics Seminar Talk, Department of Mathematics, University of South Carolina, April, 2017.
- "Efficient Iterative One-Shot Methods for PDE-Constrained Optimization", Seminar Talk, Department of Mathematics and Statistics, Mississippi State University, Feburary, 2017.
- "From Real Analysis to Numerical Analysis", Colloquium Talk, Department of Mathematics and Statistical Sciences, Jackson State University, Jackson, Mississippi, November, 2016.
- "Multilevel Discretize-then-Optimize Algorithms for PDE-Constrained Optimizations", Invited Minisymposium Talk, The 2nd Annual Meeting of SIAM Central States Section, Little Rock, Arkansas, October, 2016.
- "New Second-order Time Schemes for Optimal Control of PDEs," Poster Presentation, IMA Workshop on Computational Methods for Control of Infinite-dimensional Systems, March 14-18, 2016.
- "Iterative One-shot Methods for PDE-Constrained Optimization," Colloquium Talk, Department of Mathematics, The University of Southern Mississippi, November, 2015.
- "A Fast Iterative Method for Optimal Control of Wave Equations," Seminar Talk, Electrical and Computer Engineering Department, Southern Illinois University, April, 2015.
- "A Stable Leapfrog Scheme for Optimal Control of Wave Equations," The 1st Annual Meeting of SIAM Central States Section, Rolla, Missouri, April, 2015.
- "A New Semi-Smooth Newton Multigrid Method for Parabolic PDE Optimal Control Problems," The 53rd IEEE Conference on Decision and Control, Los Angeles, CA, December, 2014.
- "Multigrid method for Optimization Problems governed by Partial Differential Equations," Seminar Talk, Electrical and Computer Engineering Department, Southern Illinois University, October, 2014.
- "A Fast Leapfrog Scheme for the Numerical Solution of Parabolic Optimal Control Problems," The 34th Southeastern-Atlantic Regional Conference on Differential Equations, The University of Memphis, Memphis, October, 2014.
- "A New Semi-smooth Newton Multigrid Method for Parabolic PDE Optimal Control Problems," SIAM Annual Meeting, Chicago, Illinois, July, 2014.
- "A New Semi-Smooth Newton Multigrid Method for Control-Constrained Semi-Linear Elliptic PDE Problems," SIAM Conference on Optimization, San Diego, California, May, 2014.
- "High-Order Numerical Methods for Wave Equations with Van Der Pol Type Boundary Conditions," Session Chair,

- SIAM Conference on Control and Its Applications, San Diego, California, July, 2013.
- "Rank-one Characterization of Joint Spectral Radius," School of Mathematical Sciences, South China Normal University, Guangzhou, China, May, 2013.
- "Joint Spectral Radius of Finite Rank-One Matrix Family," SIAM Conference on Control and Its Applications, Baltimore, Maryland, July, 2011.
- "A Fast Sinc Method and its Application in Option Pricing," Department of Mathematics, Chinese University of Hong Kong, Hong Kong, China, December, 2009.
- "Sinc Method and its Application in Option Pricing," Department of Mathematics, University of Macau, Macao, China, March, 2009.

PROFESSIONAL DEVELOPMENT

- IMA Workshop: Stochastic Control, Computational Methods, and Applications, Minneapolis, MN, May 7 11, 2018.
- ICERM Research Experiences for Undergraduate Faculty (REUF), Providence, RI, June 26-30, 2017.
- NSF/CBMS: Nonlocal Dynamics: Theory, Computation and Applications, Chicago, IL, June 4-9, 2017.
- Participated JSU ADVANCE Implicit Bias Think Tank, Jackson, Mississippi, March 22-23, 2017.
- A faculty leader in Interdisciplinary Engagement Team of JSU's First in the World (FITW) program, 2016-2017.
- IMA New Directions Short Course: Mathematical Optimization, IMA, Minneapolis, August 1-12, 2016.
- AIM Research Experiences for Undergraduate Faculty (REUF) on the Mathematics of Data, Information Initiative at Duke (iiD), Duke University, Durham, July 18-22, 2016.
- IMA Workshop: Computational Methods for Control of Infinite-dimensional Systems, University of Minnesota, Minneapolis, March 14-18, 2016.
- Cohort IV of the Academy for Research and Scholarly Engagement at Jackson State University, 2015-2016.
- XSEDE HPC workshop in Southern University at New Orleans, October 23-24, 2015.
- IMA New Directions Short Course: Topics in Control Theory, IMA, Minneapolis, May 27-June 13, 2014.
- SAMSI Industrial Math/Stat Modeling Workshop, North Carolina State University, Raleigh, July 16-24, 2012.
- Workshop on Computational Issues in Nonlinear Control, Monterey, California, November 7-8, 2011.
- The 3rd Winter School on Applied Mathematics, City University of Hong Kong, December 1-11, 2009.

PROFESSIONAL SERVICE

- Referee for the following international academic journals:
 - Inverse Problems
 - Mathematics and Computers in Simulation
 - Computational & Applied Mathematics
 - Journal of Computational and Applied Mathematics
 - International Journal of Control
 - International Journal of Dynamics and Control
 - Computers & Mathematics with Applications
 - International Journal of Computer Mathematics

- Nonlinear Dynamics
- Communications in Computational Physics (CiCP)
- Optimization Letters
- IEEE Transactions on Automatic Control
- IEEE Transactions on Industrial Electronics
- European Journal of Control
- Nonlinear Analysis: Hybrid Systems
- Cognitive Computation
- Advised 2 teams (6 students) to participate in 2017 COMAP's Mathematical Contest in Modeling (MCM).
- Committee Chair of the 2017 (37th) Annual Mathematics and Engineering Fair at Jackson State University.
- Referee for the Eighteenth Biennial IEEE Conference on Electromagnetic Field Computation (CEFC 2018).
- Referee for the Second Conference on Modelling Identification and Control of Nonlinear Systems (MICNON 2018).
- Referee for 2017 IEEE Conference on Control Technology and Applications.
- Referee for the 10th IFAC Symposium on Nonlinear Control Systems (NOLCOS 2016).
- Referee for the 2016 American Control Conference.
- Reviewer for Mathematical Review (American Mathematical Society), 2013-present.
- Referee for the 10th World Congress on Intelligent Control and Automation, 2012
- Referee for the SIAM Conference on Control and Its Applications (2013,2015).
- Judge for the annual Illinois Junior Academy of Science Region 8 Science Fair at SIUC, 2013-2015.
- Volunteer for the Annual Math Field Day organized by Department of Mathematics, SIUC, 2011-2014.