

Role of indirect-ionization processes in the electron-impact ionization of Fe^{15+}

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We have investigated the contributions of excitation-autoionization and resonant-excitation-double-autoionization indirect-ionization processes to the electron-impact ionization of Fe^{15+} using a close-coupling approximation. The total ionization cross sections are obtained by adding the cross sections for these indirect processes to the direct-ionization cross sections. Eleven autoionizing levels arising from the $2p^5 3s^2$, $2p^5 3s 3p$, $2p^5 3p^2$, and $2p^5 3s 3d$ configurations, together with the ground $2p^6 3s$ state, are included in the close-coupling expansion. Large numbers of bound terms of appropriate symmetry are included in the expansion to account for the resonant-excitation-double-autoionization process. The present results are in good agreement with the recent crossed-beam measurement.

I. INTRODUCTION

Several theoretical and experimental investigations¹ have emphasized the importance of indirect-ionization processes to the electron-impact ionization of positive ions. It has been shown that the importance of indirect-ionization processes over direct ionization increases substantially with increasing ionic charge along the isoelectronic sequence. Excitation-autoionization and resonant-excitation-double-autoionization (REDA) processes are the important indirect physical mechanisms for ionization which received considerable theoretical and experimental attention in recent years. In the excitation-autoionization process an inner-shell electron is excited to a level above the ionization threshold which can subsequently decay by autoionization, whereas REDA occurs when the incident electron is captured temporarily with simultaneous excitation of an inner-shell electron followed by double autoionization. The inner-shell excitation can cause significant rise in the ionization cross section close to the threshold for the excitation process. The REDA process was first described by LaGattuta and Hahn² in connection with the electron-impact ionization of Na-like Fe^{15+} and it gives rise to resonances in the threshold region. The total ionization cross section can be assumed as the sum of direct- and indirect-ionization processes, if the interference between these processes is ignored. Accurate knowledge of electron-impact ionization cross sections is necessary for an understanding of ionization equilibrium or ion abundance, etc., in astrophysical and laboratory plasmas. Apart from any practical applications, the study of indirect-ionization mechanisms is of interest in its own right.

Na-like ions provide interesting and simple cases for the experimental and theoretical study of indirect-ionization processes. Contributions of the indirect processes to the total ionization cross sections of Na-like ions have been considered theoretically by Bely³ and Moores and Nussbaumer⁴ in the Coulomb-Born approximation, while Cowan and Mann,⁵ Griffin and co-workers,^{6,7} and LaGattuta and Hahn² used distorted-wave approxima-

tions. Henry and Msezane⁸ performed close-coupling (CC) calculations for Mg^+ , Al^{2+} , and Si^{3+} ions of the sodium isoelectronic sequence. On the experimental side, Crandall *et al.*⁹ measured absolute total ionization cross sections for Mg^+ , Al^{2+} , and Si^{3+} ions. They noted significant enhancements in the cross sections near threshold due to the excitation-autoionization process. Recently, Gregory *et al.*¹⁰ reported measured absolute cross sections for electron-impact ionization of Fe^{15+} . They found that the contribution of excitation autoionization to the total ionization cross section is approximately four times the direct-ionization cross sections. However, the results of their measurements do not appear to provide any clear evidence to support the predicted large contribution of the REDA process near the excitation threshold. LaGattuta and Hahn² predicted an overall 30–40% contribution of the REDA process to the total ionization. They predicted a larger contribution due to the REDA process over excitation-autoionization and direct-ionization processes in the energy range 750–780 eV. For highly charged ions, the radiative decay rate may compete with the autoionization rate for some transitions and thereby reduces the contributions of indirect-ionization processes.

In view of the existing discrepancy between the theoretical predictions of LaGattuta and Hahn² and the most recent crossed-beam measurements of Gregory *et al.*¹⁰ for the contribution of the REDA process to the electron-impact ionization of Na-like Fe^{15+} , and because of the importance of the ionization cross sections in the modeling of the fusion plasmas where these ions are likely to be present as impurity, we carried out a detailed study of both of the indirect-ionization mechanisms in Fe^{15+} using a close-coupling approximation over a wide energy range of 720–1000 eV. We include the most important autoionizing states in the CC expansion. We consider excitation-autoionization reactions of the type where a $2p$ electron is first excited into a $3s$, $3p$, or $3d$ orbital,

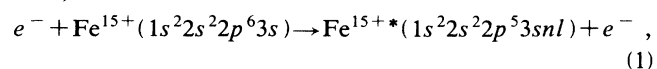


TABLE III. Excitation energies (eV) of the autoionizing states relative to the ground $2p^5 3s^2 S$ state.

State	Energy (eV)
$2p^5 3s^2 P^\circ$	721.14
$2p^5 3s(^1P^\circ)3p^2 D$	750.05
$2p^5 3s(^1P^\circ)3p^2 S$	753.48
$2p^5 3s(^3P^\circ)3p^2 D$	761.11
$2p^5 3s(^3P^\circ)3p^2 S$	774.75
$2p^5 3p^2(^1D)^2 P^\circ$	780.42
$2p^5 3p^2(^3P)^2 P^\circ$	800.27
$2p^5 3s(^1P^\circ)3d^2 P^\circ$	800.38
$2p^5 3s(^1P^\circ)3d^2 F^\circ$	807.65
$2p^5 3s(^3P^\circ)3d^2 F^\circ$	808.77
$2p^5 3s(^3P^\circ)3d^2 P^\circ$	816.31

tion of

$$2p^5 3s(^1P^\circ)3p^2 S + 2p^5 3s(^3P^\circ)3p^2 S$$

and

$$2p^5 3s(^1P^\circ)3d^2 P^\circ + 2p^5 3s(^3P^\circ)3d^2 P^\circ$$

states, respectively. Each of these orbitals was expanded in Slater-type orbitals of the form¹²

$$P_{nl}(r) = \sum_i c_i r^{p_i} \exp(-\xi_i r). \quad (6)$$

In Table I we give the parameters of the Slater-type orbitals for the $3p$ and $3d$ functions. In Table II a list of configurations used for each state is given. The coefficient of each configuration in the configuration-interaction (CI) expansion is given below the configuration. It is easily seen from this table that CI effects are very important for the autoionization states, while the mixing in the ground state is very small.

The calculated excitation energies in eV relative to the ground state are presented in Table III. The oscillator strengths for the resonance transitions are given in Table IV. The good agreement between the length and velocity forms of these oscillator strengths provides confidence in the accuracy of wave functions used in the present calculation.

III. COLLISION CALCULATION

The total wave function representing the electron-ion collision is expanded in terms of the N -electron target wave functions X_i and $(N+1)$ -electron bound-state configurations ϕ_j by the CC expansion

$$^2S \rightarrow 2p^5 3s^2 P^\circ, \quad 2p^5 3s(^1,3P^\circ)3p^2 D, ^2S, \quad 2p^5 3p^2(^3P, ^1D)^2 P^\circ, \quad 2p^5 3s(^1,3P^\circ)3d^2 P^\circ, ^2F^\circ.$$

The branching ratio is given by

$$B_j^a = \frac{\sum_m A_a(j \rightarrow m)}{\sum_m A_a(j \rightarrow m) + \sum_k A_r(j \rightarrow k)}, \quad (9)$$

where $A_a(j \rightarrow m)$ is the autoionization rate from level j

TABLE IV. Oscillator strengths for allowed transitions.

Transition	Present Calculation	
	f_L	f_V
$^2S \rightarrow 2p^5 3s^2 P^\circ$	0.087	0.084
$^2S \rightarrow 2p^5 3s(^1P^\circ)3d^2 P^\circ$	0.780	0.724
$^2S \rightarrow 2p^5 3s(^3P^\circ)3d^2 P^\circ$	2.076	1.980
$^2S \rightarrow 2p^5 3p^2(^1D)^2 P^\circ$	0.023	0.026
$^2S \rightarrow 2p^5 3p^2(^1S)^2 P^\circ$	0.029	0.032
$^2S \rightarrow 2p^5 3d^2(^1S)^2 P^\circ$	0.014	0.015

$$\psi = A \sum_i X_i \theta_i + \sum_j c_j \phi_j, \quad (7)$$

where A is the antisymmetrization operator and θ_i are the numerical basis functions describing the motion of the scattered electron. The bound configurations in the second summation are included to account for the REDA process. Application of a variational principle leads to a set of coupled integrodifferential equations which are solved numerically by the R -matrix method.^{13,14} In the R -matrix method the configuration space is partitioned into two regions. In the inner region electron exchange and correlation effects are taken into account, while in the outer region electron exchange effects are ignored. A zero logarithmic derivative was imposed at the boundary $a = 2.6$ a.u. on the continuum basis functions. Twenty-two continuum orbitals of each angular symmetry were included, giving good convergence in the energy range of interest. Each term in the first summation of Eq. (7) gives rise to an interaction channel. The largest number of channels included is 27 in the present work. The bound configurations in the second summation of Eq. (7) were obtained by adding the scattering electron in all possible ways to the configurations included in the description of target states, consistent with the total orbital angular momentum (L), spin (S), and parity (Π).

Assuming the direct- and indirect-ionization processes to be independent we can calculate the total ionization cross section by the relation

$$\sigma_{\text{tot}} = \sigma_{\text{direct}} + \sum_j \sigma_{\text{excit}}^j B_j^a, \quad (8)$$

where σ_{direct} is the direct ionization cross section, σ_{excit}^j is the excitation cross section to the j autoionizing state, and B_j^a is the branching ratio for autoionization from the level j . We are interested in the excitation cross sections for the transitions of the type

to the continuum channel m , and $A_r(j \rightarrow k)$ is the radiative rate from level j to a bound state k . As we mentioned in the Introduction, for highly charged Fe^{15+} the radiative rate may not be negligible and this would result in a nonunity value of the branching ratios. Griffin has provided us the branching ratios which he calculated us-

ing the configurations and eigenvector components given in Table II. Griffin *et al.*⁷ found that the branching ratios are very sensitive to the CI and intermediate coupling effects. We included one-electron Darwin and mass-correction relativistic terms in the present semirelativistic calculation in the Breit-Pauli approximation. The inclusion of spin-orbit interaction will give rise to a large number of channels. The spin-orbit interaction, therefore, is not included to keep the calculation manageable. A fully relativistic calculation in the framework of the close-coupling approximation would need a tremendous amount of computer time and memory.

IV. RESULTS AND DISCUSSION

An estimate of the direct-ionization cross sections in Fe^{15+} can be obtained by the use of the Lotz formula.¹⁵ However, we have used more reliable distorted-wave cross sections for the direct ionization of valence $3s$ electron in our calculation. These were obtained by using Younger's formula¹⁶ and the parameters given by Pindzola *et al.*¹⁷ The distorted-wave results for direct ionization are about 15% lower than the prediction of the Lotz formula. The inner-shell excitation cross sections for the $2p \rightarrow 3s$, $2p \rightarrow 3p$, and $2p \rightarrow 3d$ transitions are given in Table V for energies from 816.5 to 952.0 eV. It is clear from this table that $2p \rightarrow 3d$ transitions give the dominant contribution to the excitation autoionization. In this table we have also listed the ratios of indirect to direct cross sections which are in excellent agreement with the experimental estimates of Gregory *et al.*¹⁰

The results of our calculation for the electron-impact ionization of Fe^{15+} are displayed in Fig. 1, where they are compared with the experimental data of Gregory *et al.*¹⁰ The dashed curve gives the distorted-wave direct-ionization cross sections. The solid and dotted curves represent the present results obtained by adding the direct-ionization cross sections to the excitation cross sections with unit and nonunit branching ratios, respectively, in Eq. (8). The radiative decay of the autoionizing levels to the bound levels of Fe^{15+} is found to reduce the excitation cross sections by about 5%. We considered inner-shell excitations of the type $2p^6 3s \rightarrow 2p^5 3s nl$ ($n=3$), while Griffin *et al.*⁷ considered additional inner-

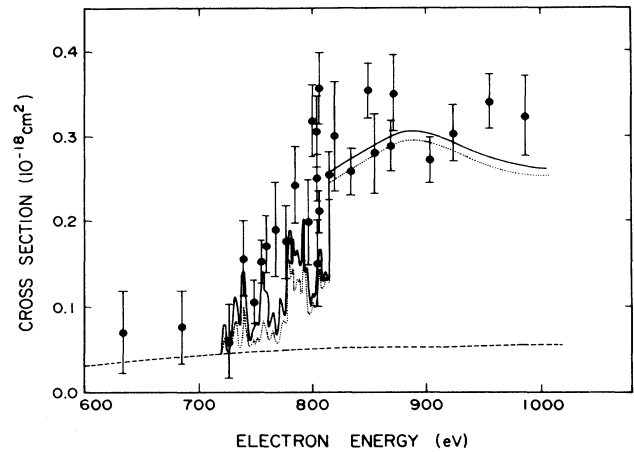


FIG. 1. Electron-impact ionization cross section for the ground $2p^6 3s \ ^2S$ state of Fe^{15+} . Solid curve, present CC cross sections with unit branching ratios; dotted curve, present CC cross sections with nonunit branching ratios; dashed curve, distorted-wave direct-ionization cross sections; solid circles, experimental results (Ref. 10).

shell excitations of the type $2p^6 3s \rightarrow 2p^5 3s nl$ ($n=4,5$) and $2s^2 2p^6 3s \rightarrow 2s 2p^6 3s nl$ ($n=3,4$) in their distorted-wave calculations. The $3l$ excited states would make dominant contributions to excitation autoionization. The excitation-autoionization features associated with the $4l$, $5l$, and higher excited states should be smaller than those for the $3l$ excited states and would occur at higher energies. A comparison of the present CC results with the distorted wave results of Griffin *et al.*⁷ (not shown) in the energy region from 825 to 935 eV (that is, before the onset of $4l$ excitations) indicates that the present results are 10–15% larger than their results. Their results are lower than the measurement and the present results at energies $E < 800$ eV. It should be noted that Griffin *et al.*⁷ did not include the REDA process in their calculation. Our calculation shows resonance structure due to the REDA process in the energy region from 720 to 816 eV. These resonances occur as Rydberg series below each of the excited states included in the present work. We calculated excitation cross section at 698 energy

TABLE V. Cross sections for the inner-shell excitations $2p^6 3s \rightarrow 2p^5 3s 3l$ ($l=0,1,2$).

Electron energy (eV)	Cross sections (10^{-18}cm^2)				Ratios of indirect to direct cross sections
	$2p \rightarrow 3s$	transition $2p \rightarrow 3p$	$2p \rightarrow 3d$	total	
816.5	0.004	0.047	0.156	0.207	4.1
829.6	0.004	0.049	0.160	0.213	4.2
843.2	0.004	0.053	0.168	0.225	4.3
856.8	0.004	0.055	0.178	0.237	4.5
870.4	0.004	0.057	0.186	0.247	4.7
897.6	0.004	0.053	0.191	0.248	4.6
924.8	0.004	0.049	0.185	0.238	4.4
952.0	0.004	0.048	0.169	0.221	4.0

points using a fine energy mesh (0.01 eV) in this energy region. These cross sections are then convoluted with a 2-eV full width at half maximum Gaussian to simulate experimental energy spread. Our convoluted results appear to be in reasonable agreement with the experiment except at energies around 800 eV where the experiment indicates some large structure. The position of resonances may be shifted in comparison to the measurement because of the difference in theoretical and experimental threshold energies. Our results with branching ratios (dotted curve) may be in error for energies $E < 816$ eV due to the fact that we assumed a unit branching ratio for the autoionization of resonant levels of Fe^{14+} to the autoionizing levels of Fe^{15+} [Eq. (4)]. LaGattuta and Hahn predicted much larger REDA contributions to the cross section than the present calculation and the measurement of Gregory *et al.*¹⁰ Mann¹⁸ calculated electron-impact excitation cross sections using a distorted-wave approximation. When his results are added to the direct-ionization cross sections, they are found to overestimate the cross sections. His results are typically 20% larger than the present results at 900 eV.

In conclusion, we have presented electron-impact ionization cross sections for Na-like Fe^{15+} over the energy region from 720 to 1000 eV. We considered both excitation-autoionization and resonant-excitation-double-autoionization indirect-ionization processes in our

calculation. The present results are in good agreement with the recent crossed-beam measurement of absolute ionization cross sections. Our calculation does not show large resonance enhancements due to the REDA process, in disagreement with the prediction of LaGattuta and Hahn. It is possible that the inclusion of quartet autoionizing states may decrease this disagreement. This may be the subject of a future, much larger calculation in which all autoionizing states arising from the configurations $2p^5 3s^2$, $2p^5 3s 3p$, and $2p^5 3s 3d$ will be included in the close-coupling expansion. In order to keep the calculation manageable, we were forced to make various simplifying assumptions which may introduce some errors in the present results, the important one being the omission of spin-orbit interaction from the Hamiltonian. We have neglected the interference between direct- and indirect-ionization processes. We have also ignored the post collision interactions between the scattered and ionizing electrons in our work.

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