

# Electron capture, excitation and ionization in slow collisions of $\text{Li}^{3+}$ ions with ground-state and metastable hydrogen atoms

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**Abstract.** Using the advanced adiabatic method we have calculated the cross sections for excitation, ionization and electron capture of  $\text{H}(1s)$  and  $\text{H}(2s)$  colliding with  $\text{Li}^{3+}$  in the energy ranges 0.1–20 keV/u and 0.1–7 keV/u, respectively. All radial and rotational couplings among the adiabatic states with united atom principal quantum number  $N \leq 10$  have been included in the calculations, as well as the electron promotion to the continuum via the  $S$ - and  $Q$ -superseries of hidden crossings. The obtained results are compared, when possible, with the results of other cross section calculations or measurements.

## 1. Introduction

There is a growing interest in current fusion research in the use of lithium beams and lithium pellets for diagnostics of tokamak edge plasma parameters (Aumayr *et al* 1992) and fusion-born alpha particle velocity distribution (Fisher *et al* 1995), respectively. The transport of ionized lithium atoms in the plasma, particularly at its cold periphery, is significantly affected by their collisions with the neutral hydrogen gas. In the present article we shall consider the inelastic collision processes (electron capture, excitation and ionization) of  $\text{Li}^{3+}$  ions with ground-state and metastable hydrogen atoms,  $\text{H}(1s)$  and  $\text{H}(2s)$ , at low collision energies (below 20 keV/u for  $\text{H}(1s)$  and below 7 keV/u for  $\text{H}(2s)$ ).

Previous theoretical studies of  $\text{Li}^{3+} + \text{H}(1s)$  collision system in the low-energy region concentrated mainly on the electron transfer process and were motivated by the electron capture cross section measurements of Seim *et al* (1981) performed in the 0.57–6 keV/u energy range. The most extensive molecular orbital (MO)-based close-coupling calculations for electron capture in this collision system were performed by Kimura and Thorson (1983) with a 10 MO basis set, and by Salin (1982) with a 24 MO basis (which includes all the states with united atom principal quantum number  $N \leq 4$ ). The most elaborate atomic orbital (AO)-based close-coupling calculations were performed by Bransden and Noble (1982) with a 20 AO basis, and by Fritsch and Lin (1982) with a 24 AO+ basis (the  $1s$  orbital on H, all  $n = 2$  and  $n = 3$  orbitals on  $\text{Li}^{2+}$  and the  $2s$ ,  $2p$ ,  $3s$  and  $3d$  united atom ( $\text{Be}^{3+}$ ) orbitals on both nuclei). We should mention also the close-coupling calculations of Lüdde and Dreizler (1982) employing 100–150 two-centre pseudostates. All these calculations have achieved a good overall description of the process, with a satisfactory agreement of the total electron

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capture cross section with the experimental data (within the uncertainty of the latter). State-selective electron capture cross sections were reported only by Bransden and Noble (1982) and Fritsch and Lin (1982) for the  $2l$  and  $3l$   $\text{Li}^{2+}$  states, and cross sections for excitation of hydrogen atom to its  $2l$  and  $3l$  states were given by Bransden and Noble (1982) only.

The inelastic processes in  $\text{Li}^{3+} + \text{H}(2s)$  collisions at low energies have not been extensively studied so far. The only available theoretical study is that of Casaubon and Piacentini (1984) for the electron capture in this system, which was performed within the Landau–Zener model using exact adiabatic energies. Only two, mutually independent reaction channels were included in this study, each of the channels containing one pair of strongly coupled molecular states ( $6h\sigma-5g\sigma$  and  $5f\sigma-4d\sigma$ ).

The present study of  $\text{Li}^{3+} + \text{H}(1s)$ ,  $\text{H}(2s)$  collisions at low energies is aimed at providing more detailed information on the collision dynamics of this system and quantitative cross section information for the most important excitation, ionization and electron capture reaction channels. We shall employ the advanced adiabatic approach to ion–atom collisions which describes the dynamical evolution of the system in terms of analytical properties of adiabatic electron energies in the complex plane of internuclear distance  $R$ , includes all the couplings between the states within a chosen molecular basis and incorporates the effects of electron translational motion (i.e. it is formulated on a dynamical adiabatic molecular basis compatible with the physical boundary conditions). A full description of the method is given elsewhere (Solov'ev 1989). One of the specific features of the method is that it allows a unified description of the reaction channels both within the discrete spectrum and in the continuum (including the energy distribution of emitted electrons). Elaborate applications of the advanced adiabatic method have so far been done for the collision systems  $\text{H}^+ + \text{H}$  ( $n \leq 4$ ) (Janev and Krstić 1992),  $\text{He}^{2+} + \text{H}$  ( $n$ ) (Grozdanov and Solov'ev 1990,  $n \leq 2$ ; Solov'ev 1991,  $n = 1$ ; Krstić and Janev 1993,  $n \leq 4$ ) and  $\text{Be}^{4+}$ ,  $\text{B}^{5+} + \text{H}$  ( $n \leq 2$ ) (Krstić *et al* 1992). The molecular basis in the calculations of Janev and Krstić (1992), Krstić and Janev (1993) and Krstić *et al* (1992) included all the states with united atom principal quantum number  $N \leq 9$  and selected states with  $N = 10$  and  $N = 11$ .

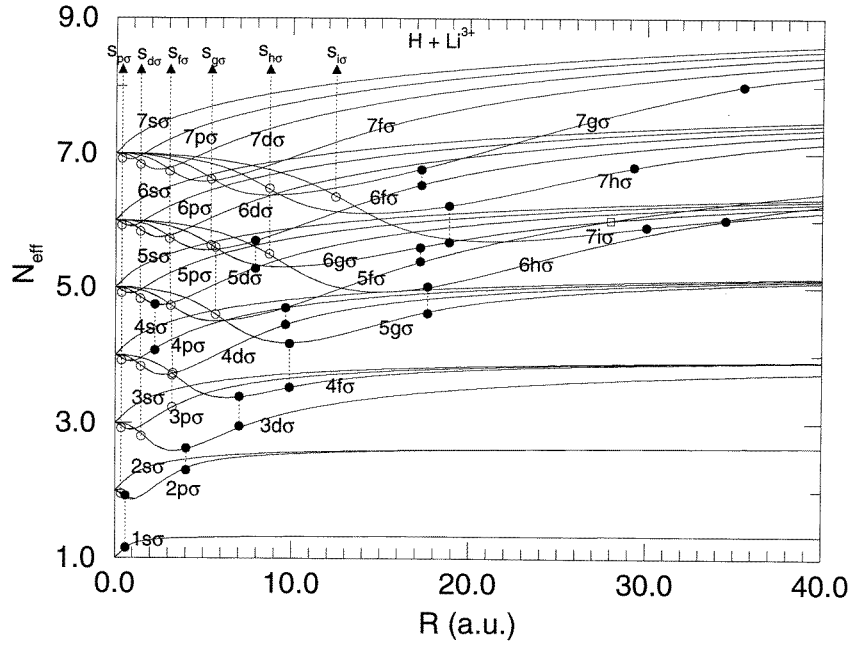
The treatment of the collision dynamics of the  $\text{Li}^{3+}\text{--H}$  system in the present work will be carried out at the same level of complexity: all the couplings (radial and rotational) among the molecular states with  $N \leq 10$  will be included in the dynamics. This basis allows one to describe all the processes in the system leading to population of the separated atom states with  $n \leq 2$  (and of some with  $n = 3$ ) on the H atom and the states with  $n \leq 9$  on the  $\text{Li}^{2+}$  ion, where  $n$  is the separated atom principal quantum number. The states with  $N > 10$  are considered as lying in the continuum.

The organization of the paper is as follows. In section 2 we discuss the structure of the 'hidden crossings' of adiabatic potential energy surfaces of the system  $\text{Li}^{3+} + \text{H}$  in the complex  $R$ -plane. In section 3 we provide a brief account of the method used for calculation of the cross sections of inelastic processes in this system. In section 4 we give the cross section results for excitation, ionization and electron capture in  $\text{Li}^{3+} + \text{H}(1s)$  collisions, whereas in section 5 we present the cross section results for these processes in  $\text{Li}^{3+} + \text{H}(2s)$  collisions. In section 6 we give some concluding remarks.

Atomic units ( $e = m_e = \hbar = 1$ ) will be used throughout this work, unless otherwise explicitly stated.

## 2. Structure of adiabatic energy hidden crossings in the $\text{Li}^{3+}\text{--H}$ system

The solution of the adiabatic eigenvalue problem for the one electron–two Coulomb centre system ( $Z_1, e, Z_2$ ) in the complex plane of internuclear distance  $R$  ( $Z_1, Z_2$  are the nuclear



**Figure 1.** Dependence of effective principal quantum number  $N_{\text{eff}} = 4/(-2E)^{1/2}$  on internuclear distance for the  $\text{Li}^{3+}\text{-H}$  system. The real parts of the positions of  $S$ - and  $Q$ -branch points are shown by open and full circles, respectively. The open square connecting the  $5f\sigma$  and  $6g\sigma$  'potential curves' indicates the position of their 'true' avoided (Landau-Zener) crossing.

charges) reveals that the potential energy surfaces of adiabatic states having the same symmetry are mutually pairwise connected by a number of square-root branching points, thus forming a multiply connected Riemann surface  $E(R)$  (Solov'ev 1981, Ovchinnikov and Solov'ev 1986, Janev and Krstić 1991). When close enough to the real  $R$ -axis, these branching points ('hidden crossings') appear as avoided crossings of the corresponding potential energy curves on the  $\text{Re}E\text{-Re}R$  plane. The investigations of the topology of adiabatic energy Riemann surface of  $(Z_1, e, Z_2)$  system further revealed that the branching points form series with certain characteristic features. In the asymmetric systems,  $Z_1 \neq Z_2$ , two basically different types of series of branching points have been identified:  $S$ - and  $Q$ -series.

The branch points of a  $S$ -series connect the molecular states  $|Nlm\rangle$  and  $|N+k, lm\rangle$ ,  $k = 1, 2, 3, \dots$  where  $N, l, m$  are the usual spherical quantum numbers in the united atom limit. From the point of view of electronic transitions, only the first branch points ( $k = 1$ ) of the  $S$ -series are important. The first terms of the  $S$ -series form, on their own, series (or superseries)  $S_{lm}$  which connect the states  $|Nlm\rangle$  and  $|N+1, lm\rangle$  consecutively for all  $N \geq l+1$ . The branch points  $R_{Nlm}^{(S)}$  of a superseries  $S_{lm}$  satisfy the relations  $\text{Re}R_{N+1,lm}^{(S)} < \text{Re}R_{Nlm}^{(S)}$ ,  $\text{Im}R_{N+1,lm}^{(S)} < \text{Im}R_{Nlm}^{(S)}$ , all are located in a small region  $\Omega_{lm}^{(S)}$  in the complex  $R$ -plane (not far from the coordinate origin), and have a limit point  $R_{lm}^{(S)} = \lim_{N \rightarrow \infty} R_{Nlm}^{(S)}$  at the continuum edge. Because of these features, the collision system reaching a  $S_{lm}$  superseries in the incoming stage of the collision is rapidly promoted to the continuum ('superpromotion').

The branch points of a  $Q$ -series connect the molecular state  $|Nlm\rangle$  with the higher states

**Table 1.** Positions and Massey parameters of branch points of the  $S_{lm}$  superseries in the  $\text{Li}^{3+} + \text{H}$  system.

Superseries	$\text{Re}R_c; \text{Im}R_c$	$\Delta_0$	Superseries	$\text{Re}R_c; \text{Im}R_c$	$\Delta_0$
$S_{p\sigma}$			$S_{d\pi}$		
2p $\sigma$ –3p $\sigma$	0.351; 0.585	0.6438	3d $\pi$ –4d $\pi$	0.604; 1.700	0.6427
3p $\sigma$ –4p $\sigma$	0.347; 0.562	0.2197	4d $\pi$ –5d $\pi$	0.602; 1.608	0.2858
4p $\sigma$ –5p $\sigma$	0.343; 0.551	0.1001	5d $\pi$ –6d $\pi$	0.599; 1.571	0.1526
5p $\sigma$ –6p $\sigma$	0.343; 0.550	0.0544	6d $\pi$ –7d $\pi$	0.596; 1.552	0.0912
6p $\sigma$ –7p $\sigma$	0.342; 0.548	0.0326	7d $\pi$ –8d $\pi$	0.595; 1.541	0.0589
7p $\sigma$ –8p $\sigma$	0.341; 0.547	0.0211	8d $\pi$ –9d $\pi$	0.593; 1.534	0.0402
8p $\sigma$ –9p $\sigma$	0.341; 0.546	0.0145	$S_{f\pi}$		
$S_{d\sigma}$			4pf–5f $\pi$	2.294; 2.765	0.4962
3d $\sigma$ –4d $\sigma$	1.492; 1.080	0.4451	5f $\pi$ –6f $\pi$	2.215; 2.591	0.2558
4d $\sigma$ –5d $\sigma$	1.441; 1.010	0.1933	6f $\pi$ –7f $\pi$	2.175; 2.513	0.1502
5d $\sigma$ –6d $\sigma$	1.419; 0.983	0.1018	7f $\pi$ –8f $\pi$	2.152; 2.471	0.0959
6d $\sigma$ –7d $\sigma$	1.406; 0.970	0.0602	8f $\pi$ –9f $\pi$	2.136; 2.446	0.0651
7d $\sigma$ –8d $\sigma$	1.399; 0.963	0.0386			
8d $\sigma$ –9d $\sigma$	1.394; 0.958	0.0262	$S_{g\pi}$		
$S_{f\sigma}$			5g $\pi$ –6g $\pi$	4.666; 3.820	0.3831
4f $\sigma$ –5f $\sigma$	3.256; 1.596	0.3143	6g $\pi$ –7g $\pi$	4.470; 3.567	0.2174
5f $\sigma$ –6f $\sigma$	3.126; 1.475	0.1578	7g $\pi$ –8g $\pi$	4.369; 3.447	0.1365
6f $\sigma$ –7f $\sigma$	3.064; 1.424	0.0912	8g $\pi$ –9g $\pi$	4.307; 3.379	0.0916
7f $\sigma$ –8f $\sigma$	3.028; 1.396	0.0577			
8f $\sigma$ –9f $\sigma$	3.005; 1.380	0.0388	$S_{h\pi}$		
$S_{g\sigma}$			6h $\pi$ –7h $\pi$	7.707; 4.874	0.3023
5g $\sigma$ –6g $\sigma$	5.660; 2.142	0.2321	7h $\pi$ –8h $\pi$	7.363; 4.546	0.1837
6g $\sigma$ –7g $\sigma$	5.419; 1.962	0.1284	8h $\pi$ –9h $\pi$	7.179; 4.383	0.1213
7g $\sigma$ –8g $\sigma$	5.296; 1.881	0.0795			
8g $\sigma$ –9g $\sigma$	5.222; 1.835	0.0528	$S_{i\pi}$		
$S_{h\sigma}$			7i $\pi$ –8i $\pi$	11.408; 5.934	0.2440
6h $\sigma$ –7h $\sigma$	8.721; 2.716	0.1782	8i $\pi$ –9i $\pi$	10.895; 5.533	0.1561
7h $\sigma$ –8h $\sigma$	8.336; 2.472	0.1058			
8h $\sigma$ –9h $\sigma$	8.130; 2.356	0.0689	$S_{j\pi}$		
$S_{i\sigma}$			8j $\pi$ –9j $\pi$	15.771; 7.007	0.2009
7i $\sigma$ –8i $\sigma$	12.444; 3.315	0.1411			
8i $\sigma$ –9i $\sigma$	11.888; 3.002	0.8840	$S_{g\sigma}$		
$S_{j\sigma}$			5g $\sigma$ –6g $\sigma$	3.006; 4.968	0.4763
8j $\sigma$ –9j $\sigma$	16.837; 3.935	0.1145	6g $\sigma$ –7g $\sigma$	2.911; 4.657	0.2729
			7g $\sigma$ –8g $\sigma$	2.858; 4.507	0.1724
			8g $\sigma$ –9g $\sigma$	2.825; 4.420	0.1162
			$S_{h\sigma}$		
			6h $\sigma$ –7h $\sigma$	5.962; 6.607	0.3876
			7h $\sigma$ –8h $\sigma$	5.716; 6.187	0.2384
			8h $\sigma$ –9h $\sigma$	5.582; 5.976	0.1585
			$S_{i\sigma}$		
			7i $\sigma$ –8i $\sigma$	9.614; 8.225	0.3194
			8i $\sigma$ –9i $\sigma$	9.190; 7.705	0.2069

$|N + k, l + k, m\rangle$ ,  $k = 1, 2, 3, \dots$ . With increasing  $k$ , the imaginary part of the branching points of a  $Q$ -series increases by (roughly) a constant amount, while their real part remains almost unchanged. Therefore, from the point of view of electronic transitions, only the first term,  $k = 1$ , of a  $Q$ -series is important. The first terms of  $Q$ -series form, on their own, new series,  $Q$ -superseries, which connect the states  $|Nlm\rangle$  and  $|N + 1, l + 1, m\rangle$  pairwise

and successively. The branching points  $R_{Nlm;N+1,l+1,m}^{(Q)}$  of a  $Q$ -superseries are characterized by the relation  $\text{Re}R_{Nlm;N+1,l+1,m}^{(Q)} < \text{Re}R_{N+1,l+1,m;N+2,l+2,m}^{(Q)}$  and, therefore, a  $Q$ -superseries provides a path for promotion of the system to states with higher  $N$  (and to the continuum) during the outgoing stage of the collision.

The probability for transition from one adiabatic state  $|\alpha\rangle$  to another  $|\beta\rangle$ , connected by a branching point  $R_c$ , is given, at an adiabatically low collision velocity  $v$ , by (see e.g. Solov'ev 1989)

$$p_{\alpha\beta} = \exp\left(-\frac{2}{v}\Delta_{\beta\alpha}\right) \quad (1)$$

where  $\Delta_{\beta\alpha}$  is the generalized Massey parameter defined by

$$\Delta_{\beta\alpha} = \left| \text{Im} \int_{\text{Re}x(R_c)}^{x(R_c)} \Delta E_{\beta\alpha}(R(x)) dx \right|. \quad (2)$$

$\Delta_{\beta\alpha}(R) = E_{\beta}(R) - E_{\alpha}(R)$  is the difference of the energies of adiabatic states  $|\beta\rangle$  and  $|\alpha\rangle$ ,  $x = vt = (R^2 - b^2)^{1/2}$  (in a straightline approximation for the classical trajectory), and  $b$  is the impact parameter. The integral (2) is calculated along a contour in the complex  $R$ -plane, which connects the real axis and the branch point. In the straightline trajectory approximation and for  $b \ll |R_c|$ ,  $\Delta_{\beta\alpha}$  can be expanded as

$$\Delta_{\beta\alpha}(b) \simeq \Delta_{\beta\alpha}(0) \left(1 + \frac{b^2}{2|R_c|^2}\right) \quad (3)$$

where  $\Delta_{\beta\alpha}(0) = \Delta_0$  is the value of the integral (2) for  $b = 0$ . The quantity  $\Delta_0$  is an important characteristic of the branching point  $R_c$  connecting the states  $|\alpha\rangle$  and  $|\beta\rangle$ ; according to equation (1) it represents a measure of adiabaticity of the transition.

Using the existing computer programs (Solov'ev 1991), we have solved the adiabatic eigenvalue problem for the system  $\text{Li}^{3+}\text{-H}$  in the complex  $R$ -plane with a basis containing all  $N \leq 10$  states, we have determined the positions of branching points of all  $S$ - and  $Q$ -superseries appearing in this molecular basis and calculated the corresponding generalized Massey parameters,  $\Delta_{\beta\alpha}(b)$ . Figure 1 shows the dependence of effective principal quantum number  $N_{\text{eff}} = (Z_1 + Z_2)/(-2E)^{1/2} = 4(-2E)^{-1/2}$  on  $\text{Re}R$  for the  $\sigma$ -states with  $N \leq 7$ . The values  $\text{Re}R_c$  for the first several members of some  $S$ - and  $Q$ -superseries are also shown in this figure to indicate the transition region between particular states. More detailed information on the branch points of most important  $S$ - and  $Q$ -superseries, including the values of corresponding Massey parameters  $\Delta_0$ , is given in table 1 and table 2. In table 2, we give also the parameters of a number of isolated branching points corresponding to the avoided (Landau-Zener) crossings; they are denoted by an asterisk. The positions of the first several branch points of some of the  $S$ - and  $Q$ -superseries are also shown in figures 2 and 3, respectively. The branch points with  $\text{Re}R > 30$  and small values of  $\Delta_0$  in figure 3 represent the avoided Landau-Zener crossings, and they are visibly separated from the other points.

As can be seen from table 1, the values of Massey parameters  $\Delta_0^{(S)}$  of a given  $S_{lm}$  superseries decrease rapidly with increasing  $N$ . For sufficiently high members of the superseries ( $N \gg N_0$ ),  $\Delta_0^{(S)}$  can be estimated by (using certain relations given in Solov'ev 1981, 1986)

$$\Delta_0^{(S)} \simeq \frac{(Z_1 + Z_2)}{N^3} (m+1)[2(l+1/2)^2 - \frac{1}{4}(m+1)^2]^{1/2}. \quad (4)$$

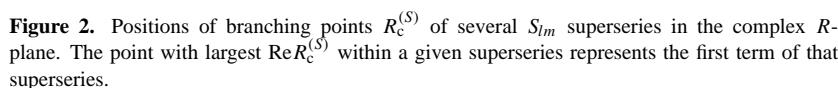
**Table 2.** Positions and Massey parameters of branch points of  $Q_{nlm}$  superseries in the  $\text{Li}^{3+} + \text{H}$  system.

Superseries	$\text{Re}R_c; \text{Im}R_c$	$\Delta_0$	Superseries	$\text{Re}R_c; \text{Im}R_c$	$\Delta_0$
$Q_{1s\sigma}$			$Q_{2p\pi}$		
$1s\sigma-2p\sigma$	0.596; 0.980	2.7856	$2p\pi-3d\pi$	1.721; 2.582	1.3321
$2p\sigma-3d\sigma$	4.016; 1.561	0.3535	$3d\pi-4f\pi$	6.047; 3.725	0.4996
$3d\sigma-4f\sigma$	7.034; 4.009	0.6551	$4f\pi-5g\pi$	13.293; 3.797	0.1353
$4f\sigma-5g\sigma$	9.869; 4.465	0.6337	$5g\pi-6h\pi$	23.287; 9.113	0.0936
$5g\sigma-6h\sigma$	17.657; 4.457	0.1763	$*5g\pi-6h\pi$	30.999; 0.4679	0.0002
$6h\sigma-7i\sigma$	29.239; 9.936	0.0495	$6h\pi-7i\pi$	24.095; 8.824	0.2873
$*6h\sigma-7i\sigma$	34.507; 1.108	0.00145	$7i\pi-8j\pi$	34.963; 7.690	0.1022
$7i\sigma-8j\sigma$	30.019; 9.748	0.3237	$*8j\pi-9k\pi$	52.644; 4.406	0.0115
$8j\sigma-9k\sigma$	41.314; 8.443	0.1183	$Q_{3p\pi}$		
$Q_{2s\sigma}$			$3p\pi-4d\pi$	< 0;	—
$2s\sigma-3p\sigma$	< 0;	—	$4d\pi-5f\pi$	5.627; 5.269	0.3801
$3p\sigma-4d\sigma$	3.224; 2.806	0.3750	$5f\pi-6g\pi$	12.600; 6.223	0.1866
$4d\sigma-5f\sigma$	9.640; 3.104	0.1005	$6g\pi-7h\pi$	22.746; 5.811	0.0655
$5f\sigma-6g\sigma$	17.245; 8.317	0.1323	$*7h\pi-8i\pi$	40.559; 2.381	0.0030
$6g\sigma-7h\sigma$	18.867; 7.850	0.2508	$8i\pi-9j\pi$	36.972; 13.381	0.1552
$7h\sigma-8i\sigma$	29.198; 6.896	0.0871	$Q_{4p\pi}$		
$*8i\sigma-9j\sigma$	46.634; 3.550	0.00721	$4p\pi-5d\pi$	< 0;	—
$Q_{3s\sigma}$			$5d\pi-6f\pi$	4.580; 6.291	0.2746
$3s\sigma-4p\sigma$	< 0;	—	$6f\pi-7g\pi$	11.605; 8.197	0.1765
$4p\sigma-5d\sigma$	2.248; 2.994	0.2297	$7g\pi-8h\pi$	21.248; 8.867	0.0968
$5d\sigma-6f\sigma$	7.920; 4.799	0.1384	$8h\pi-9i\pi$	34.280; 7.958	0.0391
$6f\sigma-7g\sigma$	17.298; 4.754	0.0478	$Q_{5p\pi}$		
$7g\sigma-8h\sigma$	30.084; 13.288	0.0390	$5p\pi-6d\pi$	< 0;	—
$*7g\sigma-8h\sigma$	35.514; 1.349	0.00091	$6d\pi-7f\pi$	3.450; 6.321	0.1860
$8h\sigma-9i\sigma$	29.871; 11.641	0.1346	$7f\pi-8g\pi$	10.012; 9.482	0.1485
$Q_{4s\sigma}$			$8g\pi-9h\pi$	19.576; 11.309	0.1012
$4s\sigma-5p\sigma$	< 0;	—	$Q_{3d\delta}$		
$5p\sigma-6d\sigma$	1.922; 2.758	0.1275	$3d\delta-4f\delta$	3.353; 4.785	0.8669
$6d\sigma-7f\sigma$	6.281; 5.095	0.1098	$4f\delta-5g\delta$	8.856; 6.388	0.4504
$7f\sigma-8g\sigma$	14.584; 6.921	0.0708	$5g\delta-6h\delta$	16.724; 7.166	0.2162
$8g\sigma-9h\sigma$	26.954; 6.519	0.0282	$6h\delta-7i\delta$	27.731; 6.619	0.0783
$Q_{5s\sigma}$			$*7i\delta-8j\delta$	45.782; 3.205	0.0056
$5s\sigma-6p\sigma$	< 0;	—	$Q_{4d\delta}$		
$6p\sigma-7d\sigma$	1.816; 2.632	0.7631	$4d\delta-5f\delta$	< 0;	—
$7d\sigma-8f\sigma$	5.555; 4.762	0.0744	$5f\delta-6g\delta$	8.539; 8.268	0.3454
$8f\sigma-9g\sigma$	12.186; 7.354	0.06354	$6g\delta-7h\delta$	16.530; 9.724	0.2082
$Q_{6s\sigma}$			$7h\delta-8i\delta$	27.070; 10.133	0.1127
$6s\sigma-7p\sigma$	< 0;	—	$8i\delta-9j\delta$	40.943; 9.048	0.0471
$7p\sigma-8d\sigma$	1.767; 2.563	0.0491	$Q_{5d\pi}$		
$8d\sigma-9f\sigma$	5.246; 4.533	0.0511	$5d\pi-6f\pi$	< 0;	—
$Q_{7s\sigma}$			$6f\pi-7g\pi$	7.614; 9.815	0.2651
$7s\sigma-8p\sigma$	< 0;	—	$7g\pi-8h\pi$	15.787; 12.026	0.1845
$8p\sigma-9d\sigma$	1.734; 2.519	0.0334	$8h\pi-9i\pi$	26.306; 13.245	0.1195

The limit point  $R_{lm}^{(S)}$  of a  $S_{lm}$  superseries can be obtained by using the modified semiclassical approximation and is given by (Solov'ev 1986)

$$R_{lm}^{(S)} \simeq \frac{1}{(Z_1 + Z_2)} \{ (l + 1/2)^2 - \frac{1}{2}(m + 1)^2 \pm i(m + 1)[2(l + 1/2)^2 - \frac{1}{4}(m + 1)^2]^{1/2} \}. \quad (5)$$

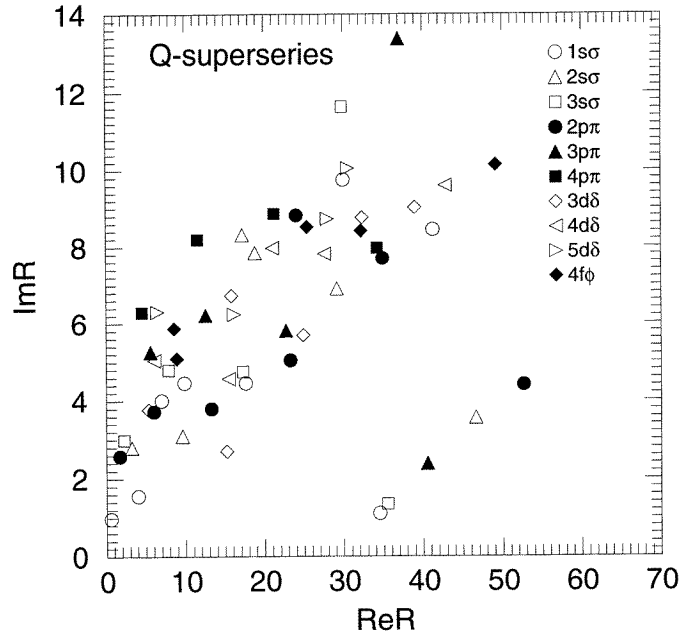
These endpoints of the  $S_{lm}$  superseries are not shown in figure 2. It should be remarked that


$$\Delta_0^{(Q)} \simeq \frac{1}{4}\pi |\Delta E_{\alpha\beta}(\text{Re}R_c^{(Q)})\text{Im}R_c^{(Q)}|. \quad (6)$$

### 3. Method of cross section calculations

$$\vec{r} = R(t)\vec{q} \quad (7)$$

where  $\vec{r}$  is the electron coordinate with respect to the midpoint of the time depending internuclear distance  $R(t)$ , which transforms the adiabatic two-Coulomb centre Hamiltonian



**Figure 3.** Positions of branching points  $R_c^{(Q)}$  of several  $Q_{Nlm}$  superseries in the complex  $R$ -plane. The point with smallest  $\text{Re}R_c^{(Q)}$  within a given superseries (same symbol) represents the first point of that superseries in the  $\text{Re}R > 0$  half-plane. The points with  $\text{Re}R > 30$  and small imaginary part ( $\text{Im}R_c \ll \text{Re}R_c$ ) represent isolated (Landau–Zener) branch points.

into an effective Hamiltonian

$$\tilde{H}(R) = -\frac{1}{2}\nabla_q^2 - \frac{Z_1 R}{|\vec{q} + \hat{R}/2|} + \frac{Z_2 R}{|\vec{q} - \hat{R}/2|} + \omega L_3 + \frac{1}{2}\omega^2 q^2 \quad (8)$$

where  $\hat{R}$  is a unit vector along the internuclear axis,  $L_3$  is the operator of the projection of electron angular momentum onto the direction perpendicular to the collision plane and  $\omega = bv$  ( $b$ , as before, being the impact parameter). After introducing an additional time transformation,  $\tau = \arctan(vt/b)/\omega$ , the original time-dependent Schrödinger equation (with moving Coulomb centres) is transformed into a modified Schrödinger equation with Coulomb centres staying at rest, i.e. the new dynamical adiabatic wavefunctions exhibit correct asymptotic behaviour.

The last two (dynamical) terms of the effective Hamiltonian (8) prevent the separation of variables in the corresponding eigenvalue problem. However, in the framework of the adiabatic approach we can consider the dynamical interactions in equation (8) as a perturbation. It can be easily shown (Solov'ev 1989) that the first-order corrections to the adiabatic energies caused by this perturbation are proportional to  $v^2$  and, therefore, the Massey parameter  $\Delta$  in the dynamical adiabatic basis has the form  $\Delta = \Delta^{(0)} + v^2\Delta^{(1)} + O(v^3)$ , where  $\Delta^{(0)}$  is the Massey parameter calculated within the standard two-Coulomb centre adiabatic basis. The corresponding transition probability is then given by the expansion  $p_{\beta\alpha} = p_{\beta\alpha}^{(0)}(1 + O(v))$ , i.e. in the region of validity of adiabatic approximation both basis sets give the same result for  $p_{\alpha\beta}$ . This is, however, not the case in the regions  $R \rightarrow 0$  and  $R \rightarrow \infty$ , where strong Coulomb degeneracies occur. In these regions the dynamical perturbations in equation (8) change the adiabatic states already in the zeroth order. These



changes represent the effects of rotational couplings in the new, modified representation. In the  $R \rightarrow 0$  limit the problem reduces to the mixing of states with different  $m$  within a given  $(N, l)$  manifold and can be solved by the close-coupling method (Grodzanov and Solov'ev 1982). In the region  $R \rightarrow \infty$ , the degeneracies can be removed completely only in the second-order perturbation theory in  $\omega$  (Grodzanov and Solov'ev 1991). We note, however, that in this order of the perturbation theory the dynamical adiabatic wavefunctions are obtained exactly and their expansion over the spherical hydrogen-like states can be carried out analytically.

Knowing the elementary transition probabilities  $p_{\alpha\beta}$  at each branching point  $R_c$ , equations (1)–(3), one can easily construct the adiabatic evolution matrix by a multiplicative procedure assuming that the interference effects between different reaction paths can be neglected (see e.g. Janev and Krstić 1992). The neglect of these effects can be justified in the total channel cross sections if the collision velocity is sufficiently small (Richter and Solov'ev 1993). The construction of the adiabatic evolution matrix includes also transformation of the separated atom spherical states into Stark states, the rotational transitions between the Stark states in both the entrance and exit channels and the rotational transitions in the united atom limit within each  $(N, l)$  manifold. In the present calculations, the rotational transitions at large internuclear distances have been calculated in the second-order perturbation theory with respect to the parameter  $\omega$ , while the rotational transitions at small internuclear distances have been calculated by numerical solution of the corresponding close-coupled equations (Grodzanov and Solov'ev 1982). The evolution matrix also includes the ionization probabilities along the  $S$ - and  $Q$ -superseries. The cross sections of different reaction channels are calculated by integration of channel probabilities over the impact parameters. The determination of adiabatic energy branching points  $R_c$ , the calculation of the values of corresponding Massey parameters, the construction of the evolution matrix for a given basis set  $\{N\}$  and the calculation of the channel and total cross sections for excitation, ionization and electron capture processes in the  $\text{Li}^{3+} + \text{H}$  system with  $N \leq 10$  has been performed by the computer program package ARSENY (see e.g. Solov'ev (1991) and Richter and Solov'ev (1993)). The results of cross section calculations are presented in the next two sections.

#### 4. Cross section results for $\text{Li}^{3+} + \text{H}(1s)$ collisions

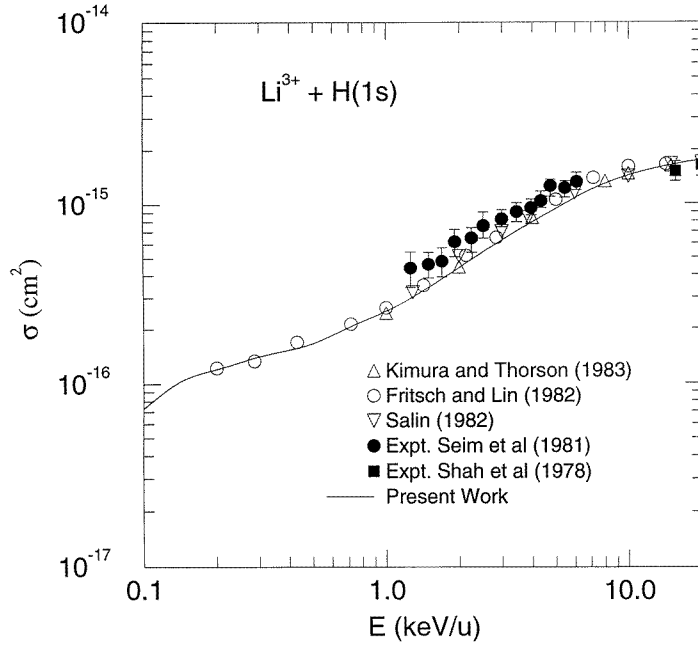
##### 4.1. Electron capture

In the adopted molecular basis for the  $\text{Li}^{3+} + \text{H}$  system containing all the states with  $N \leq 10$  ( $l \leq N-1$ ,  $m \leq l$ ) we have found 24  $S$ -superseries with more than 70 branch points, and 30  $Q$ -superseries with more than 100 branch points. Only a part of these superseries is shown in tables 1 and 2 and in figures 2 and 3. Besides, six isolated Landau–Zener pseudo-crossings were found in the considered system of molecular states (denoted by an asterisk in table 2). When two adiabatic states are coupled by both a  $Q$ -type and an isolated branching point, the transition probability between the coupled states is calculated only with the (smaller) Massey parameter of the isolated branching point, since, in the spirit of the theory of asymptotic expansions, the inclusion of the contribution from the  $Q$ -branching point would mean in this case an overestimation of the accuracy of the method. The separated atom states which are included in the adopted molecular basis have principal quantum numbers  $n \leq 3$  for the  $\text{H}^+$  centre and  $n \leq 9$  for the  $\text{Li}^{3+}$  centre. We should point out, however, that not all the molecular states (namely those with  $N > 10$ ) which correlate with  $n = 3$  states on  $\text{H}^+$  and  $n = 9$  states on  $\text{Li}^{3+}$  are present in our basis. Therefore, the excitation transitions to

$H(n = 3)$  and electron capture transitions to  $Li^{2+}(n = 9)$  cannot be fully accounted for by the present calculations.

The initial molecular state of  $Li^{3+} + H(1s)$  system is  $3d\sigma$  and, as can be seen from table 2, it is strongly coupled with the  $2p\sigma$  state, which asymptotically correlates with the  $Li^{2+}(n = 2)$  manifold and with the  $4f\sigma$  state, which asymptotically correlates with the  $Li^{2+}(n = 3)$  manifold. Although the strength of the  $3d\sigma$ – $2p\sigma$  coupling is stronger than that of the  $3d\sigma$ – $4f\sigma$  coupling (see the corresponding  $\Delta_0$  values in table 2), the cross section for population of the  $4f\sigma$  state at low energies is still larger than that for population of  $2p\sigma$ , since the  $3d\sigma$ – $4f\sigma$  coupling occurs at larger internuclear distances ( $ReR_c \simeq 7$ ). The population of  $Li^{2+}(1s)$  electron capture channel is strongly inhibited by the large value of Massey parameter for the  $2p\sigma$ – $1s\sigma$  transition ( $\Delta_0 = 2.7856$ ) and the small value of characteristic distance for this transition ( $ReR_c \simeq 0.6$ ). The population of  $L^{2+}(n \geq 4)$  states requires a sequence of successive transitions along the  $Q_{1s\sigma}$  superseries during the outgoing stage of the collision ( $3d\sigma \rightarrow 4f\sigma \rightarrow 5g\sigma$  for  $Li^{2+}(n = 4)$ ,  $3d\sigma \rightarrow 4f\sigma \rightarrow 5g\sigma \rightarrow 6h\sigma$  for  $Li^{2+}(n = 5)$ , etc) and, therefore, the population probabilities for these states are correspondingly smaller than those for the  $L^{2+}(n = 2, 3)$  states. Additional reaction paths for population of  $Li^{2+}(n = 2, 3)$  manifolds are opened via the  $2p\sigma$ – $2p\pi$  (for  $Li^{2+}(n = 2)$ ) and  $3d\sigma \rightarrow 3d\pi \rightarrow 3d\delta$  (for  $Li^{3+}(n = 3)$ ) rotational couplings at small internuclear distances. The  $Q_{2p\pi}$ ,  $Q_{3d\pi}$  and  $Q_{3d\delta}$  superseries, initiated by these rotational transitions, provide a mechanism for population of the  $\pi$ - and  $\delta$ -states of  $Li^{2+}(n \geq 4)$  manifolds. The transitions at the lower  $S$ -branching points can also activate  $Q$ -superseries for population of higher  $n$  capture states. Thus, the  $3d\sigma$ – $4d\sigma$   $S$ -transition at  $ReR_c \simeq 1.5$  activates the  $Q_{4d\sigma}$ -superseries (a sub-series of  $Q_{2s\sigma}$ ), which populates the  $n \geq 4$  manifolds of  $Li^{2+}$ . Obviously, the branching of probability flux in the transition region of any type ( $S$ - or  $Q$ -branching point, or rotational coupling at small  $R$ ), creates a large number of reaction paths for population of a specific exit reaction channel. Generally speaking, however, only those reaction paths which include a small number of couplings give significant contribution to the cross section of a particular reaction channel. The contributing role of different couplings to the cross section may, of course, change when varying the collision velocity. Figure 4 shows the total electron capture cross section for  $Li^{3+} + H(1s)$  collisions in the energy range 0.1–20 keV/u. The results of present calculations are in good agreement with those of the previous extensive AO- or MO-based close-coupling calculations mentioned in the introduction, but lie below the experimental data of Seim *et al* (1981) by 10–20% in the overlapping energy range. The reason for this disagreement could be either the neglected interference effects in the present treatment, or the neglect of rotational transitions in the united atom region for internuclear distances larger than the ‘radii’ of the  $S$ -superseries. In the region around 20 keV/u, the present results agree well with the cross section measurements of Shah *et al* (1978).

In figure 5 we present the calculated cross section for electron capture to specific  $n$ -shells of  $Li^{2+}$  ion. The partial cross sections for population of  $n = 2$  and  $n = 3$  shell are compared with the 24+ AO close-coupling results of Fritsch and Lin (1982). We note that the charge-exchange states with  $Li^{2+}(n \geq 4)$  were not included in the AO-basis of Fritsch and Lin. The agreement of the two sets of calculations is quite good, except for the  $n = 2$  case in the energy region below 1 keV/u. This fact is understandable in view of the small values of the cross sections for capture to  $n \geq 4$  states. Both calculations show that in the region below approximately 1 keV/u, the dominant electron capture channel is  $n = 3$ . As mentioned at the beginning of this section, this is a consequence of the strong coupling between  $3d\sigma$  and  $4f\sigma$  molecular states in the region  $ReR \simeq 7$ . In table 3 we give the calculated cross sections for electron capture to specific  $nl_a$ -subshells of the  $Li^{2+}$

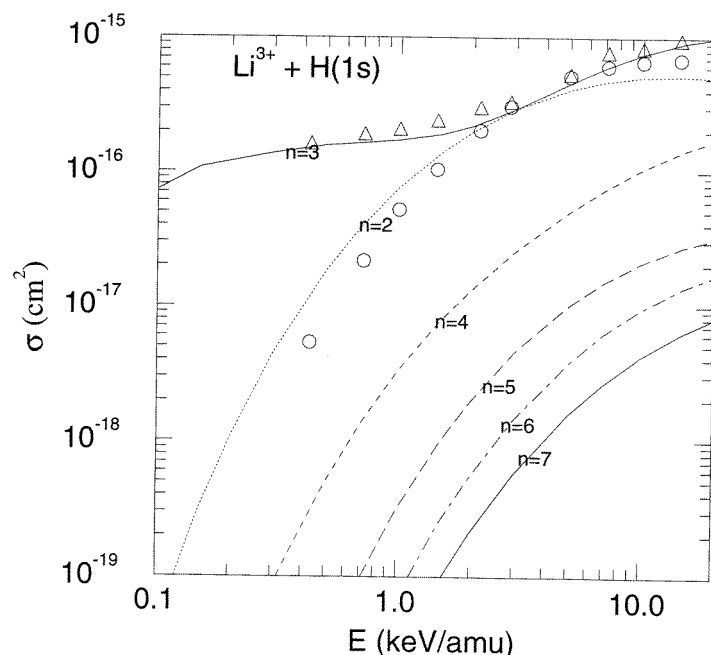


**Figure 4.** Total electron capture cross section in  $\text{Li}^{3+} + \text{H}(1s)$  collisions. The full curve represents the results of present calculations. The experimental data are indicated by closed symbols. The triangles and inverted triangles are the results of 10 MO and 24 MO close-coupling calculations, respectively, and the open circles are the results of 24 AO+ close-coupling calculations.

ion ( $n = 2-5$ ) for a number of collision energies between 1 keV/u and 15 keV/u. ( $l_a$  designates the angular momentum quantum number of the atomic state). For  $n = 2, 3$  and  $E = 1, 5, 10$  keV/u the results of Fritsch and Lin (1982) are also shown in this table. There are significant differences between the two sets of cross section values, particularly for the energy of 1 keV/u. It is difficult to accurately trace the origin of these differences given the different character and size of the bases used in the two calculations. We note that the  $l_a$ -distribution of captured electrons within a given  $n$ -shell is dominantly determined by the rotational coupling of molecular states at large internuclear distances.

#### 4.2. Excitation and ionization

The molecular states of  $\text{Li}^{3+}\text{-H}$  system, which in the separated atom limit go over to the  $\text{H}(n = 2)$  manifold, are the  $7i\sigma$ ,  $6g\sigma$  and  $6h\pi$  states. The  $7i\sigma$  state can be populated by the  $Q_{1s\sigma}$  superseries on the outgoing stage of the collision via the following sequence of transitions:  $3d\sigma \rightarrow 4f\sigma \rightarrow 5g\sigma \rightarrow 6h\sigma \rightarrow 7i\sigma$ . As seen from table 2 the last step of this sequence of transitions is due to an isolated (Landau-Zener) branch point at  $\text{Re}R_x \simeq 34.5$  and it is, therefore, particularly strong ( $\Delta_0 = 0.00145$ ). The  $6g\sigma$  state can be populated by a  $3d\sigma \rightarrow 4d\sigma$   $S$ -type transition during the incoming part of the trajectory, followed by the sequence of  $Q$ -type transitions  $4d\sigma \rightarrow 5f\sigma \rightarrow 6g\sigma$  along the  $Q_{2s\sigma}$  superseries during the outgoing stage of the collision. Finally, the  $6h\pi$  state is populated by the rotational  $3d\sigma \rightarrow 3d\pi$  transition in the united atom region, followed by the  $3d\pi \rightarrow 4f\pi \rightarrow 5g\pi \rightarrow 6h\pi$  sequence of transitions along the  $Q_{2p\pi}$  superseries. Again, the last transition in this sequence



**Figure 5.** Cross section for electron capture into specific  $\text{Li}^{2+}(n)$ -shells in  $\text{Li}^{3+} + \text{H}(1s)$  collisions. The lines represent the results of present calculations. The symbols are the results of 24 AO+ close-coupling calculations of Fritsch and Lin (1982) for capture to  $n = 2$  and  $n = 3$  shells.

is an isolated branching point and is, therefore, very strong ( $\Delta_0 = 0.093$ ; see table 2). The fact that all intermediate states in the above transition sequences are connected with the  $\text{Li}^{2+}(n = 3, 4, 5)$  electron capture channels makes the excitation of the  $\text{H}(n = 2)$  manifold a weak process. On the other hand, the strong  $6h\sigma \rightarrow 7i\sigma$  and  $5g\pi \rightarrow 6h\pi$  transitions prevent a considerable population of the  $\text{Li}^{2+}(n = 5)$  charge exchange states.

As has been mentioned in section 3, our  $N \leq 10$  molecular basis includes the  $9i\sigma$ ,  $9j\pi$ ,  $9k\delta$ ,  $10k\sigma$  and  $10l\pi$  states which asymptotically correlate with the  $\text{H}(n = 3)$  manifold, but does not include the state  $11m\sigma$  which also correlates to the same manifold. The  $n = 3$  excitation state  $11m\sigma$  can be reached by continuing the evolution along the  $Q_{1s\sigma}$  superseries from the  $7i\sigma$   $n = 2$  excitation state. Since in the excitation of  $11m\sigma$ ,  $10l\pi$  and  $10k\sigma$  states four successive transitions are needed (e.g.  $7i\sigma \rightarrow 8j\sigma \rightarrow 9k\sigma \rightarrow 10l\sigma \rightarrow 11m\sigma$ , in the case of the  $Q_{1s\sigma}$  superseries), it can be expected that the population of these excited states would be considerably smaller than that of  $7i\sigma$ ,  $6h\pi$  and  $6g\sigma$   $n = 2$  excited states. The population of the other three molecular states,  $9i\sigma$ ,  $9j\pi$  and  $9k\delta$ , which in the separated atom limit correlate with the  $\text{H}(n = 3)$  manifold, also includes sequences of a large number of transitions. For instance, the  $9i\sigma$  state can be populated by making the  $3d\sigma \rightarrow 4d\sigma \rightarrow 5d\sigma$  S-type transitions during the incoming part of the trajectory and the  $5d\sigma \rightarrow 6f\sigma \rightarrow 7g\sigma \rightarrow 8h\sigma \rightarrow 9i\sigma$  Q-type transitions during the outgoing part of the trajectory. Therefore, these  $n = 3$  excitation channels are also expected to be weak.

In table 4 we give the calculated cross sections for excitation of 2s and 2p states of hydrogen atom in the energy range 1–20 keV/u. For a number of collision energies the present cross sections are compared with those of 24 AO close-coupling calculations of

**Table 3.** Cross sections (in units of  $10^{-16} \text{ cm}^2$ ) for the  $\text{Li}^{3+} + \text{H}(1s) \rightarrow \text{Li}^{2+}(nl_a) + \text{H}^+$  reaction ( $n = 2-5$ ). (The values in square brackets are the results of Fritsch and Lin (1982).)

$n$	$nl_a$	$E$				
		1 keV/u	2 keV/u	5 keV/u	10 keV/u	15 keV/u
2	2s	1.91(−1) <sup>a</sup> [2.46(−1)]	5.03(−1)	1.04 [2.32]	1.29 [2.01]	1.32
	2p	5.68(−1) [2.76(−1)]	1.49	3.08 [2.81]	3.82 [4.59]	3.88
3	3s	4.00(−1) [2.08(−1)]	4.16(−1)	5.45(−1) [8.13(−1)]	7.40(−1) 2.69	8.50(−1)
	3p	2.99(−1) [8.37(−1)]	5.09(−1)	1.49 [1.94]	4.14	3.33
	3d	1.03 [1.05]	1.28	2.54 [2.61]		5.01
4	4s	3.42(−3)	1.36(−2)	4.37(−2)	7.56(−2)	9.40(−2)
	4p	6.61(−3)	2.39(−2)	7.92(−2)	1.64(−1)	2.31(−1)
	4d	8.89(−3)	3.54(−2)	1.52(−1)	3.60(−1)	5.24(−1)
	4f	1.42(−2)	5.69(−2)	2.26(−1)	4.56(−1)	6.08(−1)
5	5s	2.71(−4)	1.57(−3)	7.19(−3)	1.45(−2)	1.90(−2)
	5p	6.37(−4)	3.71(−3)	1.53(−2)	2.72(−2)	3.30(−2)
	5d	7.52(−4)	4.33(−3)	1.95(−2)	4.00(−2)	5.39(−2)
	5f	8.48(−4)	5.48(−3)	2.83(−2)	6.02(−2)	8.00(−2)
	5g	6.27(−4)	4.78(−3)	2.99(−2)	6.81(−2)	9.14(−2)

<sup>a</sup>  $a(-x) = a \times 10^{-x}$ .**Table 4.** Excitation and ionization cross sections (in units of  $10^{-16} \text{ cm}^2$ ) for  $\text{Li}^{3+} + \text{H}(1s)$  collisions. (The values in square brackets are the results of Bransden and Noble (1982).)

$E$ (keV/amu)	$\sigma_{\text{ex}}(2s)$	$\sigma_{\text{ex}}(2p)$	$\sigma_{\text{ion}}$
1.0	1.51(−3) <sup>a</sup>	2.26(−3)	3.70(−4)
1.5	4.93(−3) [2.0(−2)]	6.90(−3) [5.5(−2)]	1.90(−3)
2.0	1.01(−2)	1.42(−2)	5.14(−3)
3.0	2.47(−2)	3.74(−2)	1.75(−2)
5.0	6.74(−2) [1.8(−1)]	1.25(−1) [2.2(−1)]	6.31(−2)
7.0	1.24(−1)	2.64(−1)	1.29(−1)
10.0	2.27(−1) [1.6(−1)]	5.43(−1) [3.0(−1)]	2.48(−1)
15.0	4.17(−1)	1.09	4.65(−1)
20.0	6.06(−1)	1.65	6.81(−1)

<sup>a</sup>  $a(-x) = a \times 10^{-x}$ .

Bransden and Noble (1982). The differences between the two sets of data, particularly for  $E = 1.5 \text{ keV/u}$  and  $E = 5 \text{ keV/u}$ , are considerable. The application of the AO close-coupling model at these low energies is, however, not expected to be justifiable. It should be noted that in the region above approximately  $7 \text{ keV/u}$ , the  $2s$  and  $2p$  excitation cross sections calculated by the present method are larger than those of Bransden and Noble

(1982). (For  $E \leq 7$  keV/u the opposite is true.) This is a consequence of the fact that the atomic basis used in the calculations of Bransden and Noble includes all the  $n = 3$  states (and, therefore, a larger part of the excitation flux is transmitted from  $n = 2$  to  $n = 3$  states), which is not the case with the basis used in the present calculations.

In table 4 we also give the results for ionization of H(1s) by  $\text{Li}^{3+}$  ions in the same energy range. The main contribution to the ionization cross section at energies below approximately 5 keV/u give the  $S_{p\sigma}$ ,  $S_{d\sigma}$  and  $S_{f\sigma}$  superseries, while for higher energies the ionization via the  $Q_{1s\sigma}$ ,  $Q_{2s\sigma}$  and  $Q_{2p\pi}$  superseries also becomes important. In the upper part of this energy range, the ionization cross section becomes less reliable since it may include a significant fraction of the excitation and charge exchange channels to states with  $N \geq 11$ , treated here as lying in the continuum.

## 5. $\text{Li}^{3+} + \text{H}(2s)$ collisions

### 5.1. Charge exchange

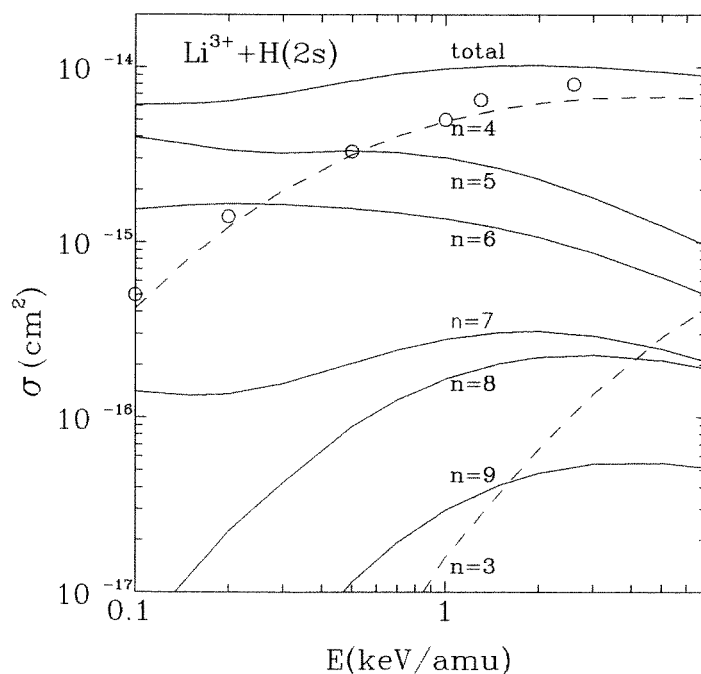
The initially occupied  $7i\sigma$  and  $6g\sigma$  molecular states of  $\text{Li}^{3+} + \text{H}(2s)$  system are rotationally coupled with the  $6h\pi$  state at large distances and, thus, the system enters the molecular collision region with three initial molecular states,  $7i\sigma$ ,  $6g\sigma$  and  $6h\pi$  (with well defined populations). These three states exhibit very strong couplings  $7i\sigma-6h\sigma$ ,  $6g\sigma-5f\sigma$ ,  $6h\pi-5g\pi$  with the  $\text{Li}^{2+}(n=5)$  charge exchange states already at large internuclear distances (at  $\text{Re}R_c \simeq 34.5$ ,  $\text{Re}R_c \simeq 17.2$  and  $\text{Re}R_c \simeq 23.3$ , respectively). The Massey parameter values of these couplings are 0.0014, 0.13 and 0.093, respectively (see table 2). In their turn, the  $6h\sigma$ ,  $5f\sigma$  and  $5g\pi$  molecular states also have strong couplings with the  $\text{Li}^{2+}(n=4)$   $5g\sigma$ ,  $4d\sigma$  and  $4f\pi$  charge exchange states, respectively, still at sufficiently large distances (see table 2). Therefore, most of the initial-state population is transferred to the  $\text{Li}^{2+}(n=4)$   $5g\sigma$ ,  $4d\sigma$  and  $4f\pi$  charge exchange states already in the incoming part of the collision. These circumstances lead to dominant population of the  $\text{Li}^{2+}(n=4, 5) + \text{H}^+$  charge exchange channels in slow  $\text{Li}^{3+} + \text{H}(2s)$  collisions.

The total and  $n$ -selective electron capture cross sections for  $\text{Li}^{3+} + \text{H}(2s)$  collisions, in the energy range 1–7 keV/u, are shown in figure 6. As argued above, the  $n = 4, 5$  shells are populated dominantly, with  $n = 4$  being the dominant channel for  $E > 0.5$  keV/u and  $n = 5$  dominating for  $E < 0.5$  keV/u. The open symbols in this figure are the results of Landau–Zener model calculations of Casaubon and Piacentini (1984) with the  $6h\sigma-5g\sigma$  and  $5f\sigma-4d\sigma$  radial couplings only (i.e. assuming that the  $7i\sigma-6h\sigma$  and  $6g\sigma-5f\sigma$  transitions in the incoming part of the trajectory have a unit probability). Since the  $5g\sigma$  and  $4d\sigma$  molecular states in the separated atom limit go over into the  $\text{Li}^{2+}(n=4)$  manifold of states, the cross sections of Casaubon and Piacentini are pertinent to the  $n = 4$  channel only. With this in mind, their agreement with our results for the  $n = 4$  channel can be considered quite satisfactory.

The cross sections for capture into specific  $\text{Li}^{2+}(nl_a)$  states for  $n = 4, 5, 6, 7$ , are given in table 5 for a number of collision energies between 0.2 and 3 keV/u. As in the  $\text{Li}^{3+} + \text{H}(1s)$  case, the  $l_a$ -distributions of captured electrons within a given  $n$ -shell are determined by the rotational mixing of corresponding Stark states at large internuclear distances.

### 5.2. Excitation and ionization

As mentioned in section 4.2, the absence of the  $11m\sigma$  state in our molecular basis prevents us calculating the excitation to the  $\text{H}(n=3)$  states exactly. However, the flux reaching this



**Figure 6.** Total and shell-selective electron capture cross sections in  $\text{Li}^{3+} + \text{H}(2s)$  collisions. The lines represent the results of present calculations. The open circles are the results of two-channel Landau-Zener model calculations of Casaubon and Piacentini (1984).

state is expected to be small with respect to the total flux reaching the  $n = 3$  manifold (e.g. four intermediate transition steps along the  $Q_{1s\sigma}$  series are required to reach  $11m\sigma$  from  $7i\sigma$ ). In table 6 we give the cross section for excitation of the  $n = 3$  manifold (disregarding the contribution from the state  $11m\sigma$ ) in the energy range 0.1–7 keV/u. We note that for  $E \leq 2$  keV/u more than 90% of the cross section comes from the population of the 3d atomic state, and that for  $E = 7$  keV/u the 3d contribution to  $n = 3$  excitation amounts to 86%. The  $n = 3$  excitation cross section shows a maximum around  $E \simeq 0.7$  keV/u. The cross section for the  $2s \rightarrow 2p$  transition is also given in table 6. In the considered energy range, the  $2s \rightarrow 2p$  excitation cross section weakly depends on the energy and shows a broad maximum around 5 keV/u. The high cross section values for the  $2s \rightarrow 2p$  excitation are, of course, not surprising, because of the strong mixing of 2p-state Stark components with those of the initial state at large internuclear distances. It should, however, be noted that this mixing is not sufficiently strong to produce a statistical  $l_a$ -distribution within the final  $n = 2$  manifold: the 2p excitation cross section is only about a factor of two larger than the cross section of the elastic channel.

The cross section for ionization in  $\text{Li}^{3+} + \text{H}(2s)$  slow collisions is also given in the same table. In the upper part of the considered energy range ( $E \geq 2$  keV/u), the ionization cross section should be considered as less accurate because it includes a contribution from the excitation and electron capture transitions to asymptotic states which correlate with  $N \geq 11$  molecular states.

**Table 5.** Cross sections for capture into  $nl_a$ -states in  $\text{Li}^{3+} + \text{H}(2s)$  collisions (in units of  $10^{-16} \text{ cm}^2$ ).

$n$	$nl_a$	$E$					
		0.2 keV/u	0.5 keV/u	0.7 keV/u	1 keV/u	2 keV/u	3 keV/u
4	4s	1.36	3.37	4.39	5.33	5.66	4.83
	4p	3.22	8.81	1.12(+1) <sup>a</sup>	1.38(+1)	1.76(+1)	1.82(+1)
	4d	3.45	7.92	9.22	1.05(+1)	1.49(+1)	2.00(+1)
	4f	4.13	1.16(+1)	1.54(+1)	1.95(+1)	2.40(+1)	2.33(+1)
5	5s	1.16	1.86	2.45	2.84	2.34	1.67
	5p	5.65	5.46	5.34	5.12	4.32	3.48
	5d	9.19	8.86	8.10	6.60	3.68	2.74
	5f	9.21	6.79	6.68	6.85	6.47	5.43
	5g	8.31	1.04(+1)	1.01(+1)	9.05	6.20	4.72
6	6s	2.22(−1)	2.50(−1)	2.93(−1)	3.63(−1)	4.30(−1)	3.84(−1)
	6p	3.13(−1)	4.73(−1)	5.51(−1)	6.35(−1)	7.25(−1)	6.64(−1)
	6d	7.97(−1)	1.10	1.19	1.22	1.11	1.05
	6f	2.55	2.32	2.21	2.09	1.69	1.35
	6g	5.22	4.48	3.99	3.42	2.50	2.11
	6h	7.49	6.95	6.52	5.89	4.22	3.14
7	7s	1.40(−2)	3.34(−2)	4.66(−2)	6.51(−2)	8.87(−2)	8.40(−2)
	7p	2.11(−2)	5.68(−2)	7.16(−2)	8.29(−2)	1.01(−1)	1.11(−1)
	7d	5.16(−2)	1.27(−1)	1.68(−1)	2.11(−1)	2.58(−1)	2.57(−1)
	7f	1.20(−1)	2.10(−1)	2.53(−1)	2.95(−1)	3.47(−1)	3.38(−1)
	7g	2.32(−1)	3.62(−1)	4.36(−1)	5.02(−1)	5.24(−1)	4.79(−1)
	7h	3.87(−1)	5.10(−1)	5.89(−1)	6.67(−1)	7.34(−1)	6.98(−1)
	7i	5.35(−1)	7.39(−1)	8.64(−1)	9.83(−1)	1.05	9.70(−1)

<sup>a</sup>  $a(\pm x) = a \times 10^{\pm x}$ .

## 6. Concluding remarks

In the present paper we have studied the low-energy inelastic processes in  $\text{Li}^{3+} + \text{H}(1s)$  and  $\text{Li}^{3+} + \text{H}(2s)$  systems by using the advanced adiabatic method. The molecular basis used in the calculations ( $N \leq 10$ ) was sufficient to describe all electron capture channels up to  $n = 9$  on  $\text{Li}^{2+}$ , but insufficient to include the target excitation to  $n = 3$  state and above. The ionization channels were defined by transitions to states with  $N \geq 11$ .

In the case of  $\text{Li}^{3+} + \text{H}(1s)$  collisions, the calculated total electron capture cross section was found to agree well with the results of previous AO- and MO-large-base close-coupling calculations. The present results for the shell and subshell selective electron capture and excitation cross sections are also in general agreement with the AO-based close-coupling calculations, except in the region of below approximately 5 keV/u where the AO-models are expected to be less adequate for description of collisional dynamics.

The total electron capture cross section for  $\text{Li}^{3+} + \text{H}(2s)$  collisions in the energy range 0.1–7 keV/u was found to be significantly larger than the previous results of Casaubon and Piacentini (1984), based on a two-channel Landau–Zener model. However, since the two considered molecular charge exchange channels both contribute to the population of the  $\text{Li}^{2+}(n = 4)$  only, the electron capture cross section of Casaubon and Piacentini is consistent with the present results for the same channel. The excitation and ionization cross



**Table 6.** Excitation and ionization cross sections (in units of  $10^{-16} \text{ cm}^2$ ) in  $\text{Li}^{3+} + \text{H}(2s)$  collisions.

$E \text{ (keV/u)}$	$\sigma_{\text{ex}}(2s \rightarrow 2p)$	$\sigma_{\text{ex}}(2s \rightarrow n = 3)$	$\sigma_{\text{ion}}$
0.1	3.65(+1) <sup>a</sup>	4.72(−1)	2.67(−2)
0.15	3.79(+1)	5.71(−1)	6.24(−2)
0.2	3.97(+1)	7.27(−1)	1.21(−2)
0.3	4.45(+1)	9.30(−1)	3.17(−1)
0.5	5.43(+1)	1.07	9.43(−1)
0.7	6.14(+1)	1.08	1.82
1.0	6.88(+1)	1.03	3.34
1.5	7.62(+1)	9.00(−1)	5.94
2.0	8.04(+1)	7.86(−1)	8.29
3.0	8.43(+1)	6.28(−1)	1.20(+1)
5.0	8.42(+1)	4.62(−1)	1.65(+1)
7.0	8.16(+1)	3.77(−1)	1.87(+1)

<sup>a</sup>  $a(\pm x) = a \times 10^{\pm x}$ .

sections for  $\text{Li}^{3+}\text{--H}(1s)$ ,  $\text{H}(2s)$  collisions at the considered low energies, are considerably smaller compared with the electron capture cross sections, as should be expected.

The upper limit of the energy range of present calculations was determined on the basis of Massey adiabatic criterion  $v \lesssim \Delta_{\text{eff}}$ , where  $\Delta_{\text{eff}}$  is a certain effective Massey parameter for a considered reaction channel. In practice, this criterion limits the validity of cross section results for a particular channel to collision energies where the cross section takes its maximum. The lower limit of the energy range for our calculations was determined by the estimated limit of validity of the adopted straightline trajectory approximation for the nuclear motion.

The adiabatic method used in the present calculations is expected to provide increasingly more accurate results with decreasing collision velocity. The main source of uncertainty at larger collision velocities is the neglect of the  $v$ -dependence of the Massey parameter,  $\Delta = \Delta_0 + O(v^2)$ , and the quantum interference effects, the magnitude of which in the total cross sections is also of the order of  $O(v^2)$ . Within these limitations, the advanced adiabatic method based on the dynamical adiabatic molecular states and analytical properties of adiabatic energy surfaces in the complex  $R$ -plane provides a transparent picture of the collision dynamics in one-electron ion–atom(ion) collision systems. It should be mentioned that the advanced adiabatic approach conceptually is not limited to one-electron two-Coulomb centre problems. Both of its essential ingredients, namely the introduction of the dynamical adiabatic basis and the analytical continuation of the potential energies in the complex  $R$ -plane, are independent of the number of electrons in the collision system and are only related to the Born–Oppenheimer separation of nuclear and electronic motions. The method can also be generalized to multi-centre collision systems. The first generalizations of the method along these lines have just begun (Krstić 1995).

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