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```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%
% Computational Problem Set, Enviro I, Problem 3
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%
% Last Edit Date: Nov 8, 2022
%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

## set directories

```
clear; clc;

cd '/Users/zachkuloszewski/Dropbox/My Mac (Zachs-MBP.lan)/Documents/';
cd 'GitHub/phd_psets/year2/environmental';
addpath(genpath('figures'));
addpath(genpath('functions'));
```

## Problem 3

Drilling and Real Options

### Part 3a - Set up the state space

```
% init parameters
D = 3e6;
X = 100000;

r      = 0.05;
delta = 1/(1+r);

Pmin = 0;
Pmax = 80;
N     = 81;

% define state space
P = linspace(Pmin,Pmax,N);

% define profits across the state space
```

---

```
profit = P*X - D;
```

## Part 3b - state transition matrix with uncertainty

```
% shock parameters ~N(P_{t-1}, 16)
mu      = 0;
sigma   = 4;

% init T
T = nan(N,N);

% bin upper bounds
P_bins_UB = P + 0.5;
P_bins_UB(end) = inf;

for i=1:N
    Tcdf = normcdf(P_bins_UB, P(i)+mu, sigma);

    T(i,1) = Tcdf(1);

    for j=2:numel(Tcdf)
        T(i,j) = Tcdf(j) - Tcdf(j-1);
    end
end
```

## Part 3c - value function iteration once again

```
% init parameters
error      = 1e12;
error_tol  = 1e-8;

% init value and optim choice
V_hist = nan(N,1000);
C_hist = nan(N,1000);

% iteration counter
n_iter = 0;

V      = repelem(0,N)';
Vnext = nan(N,N);

while error > error_tol

    % count number iterations
    n_iter = n_iter + 1;
    Vold = V;

    Vnext = T * V;

    % grab optimized value and action column
```

---

```
V = max((P*X - D)', delta .* Vnext);  
C = (V==(P*X - D)');  
  
% store values and choices  
V_hist(:,n_iter) = V;  
C_hist(:,n_iter) = C;  
  
error = max(abs(V-Vold));
```

```
end
```

## Part 3d - plot the value function

```
close all;  
figure;  
plot(V);  
xlabel('State');  
ylabel('Value');  
title('Converged Estimate of Value Function');  
  
saveas(gcf, 'figures/part3d.png')
```

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