



# Unified Path Following Guidance for Hybrid VTOLs

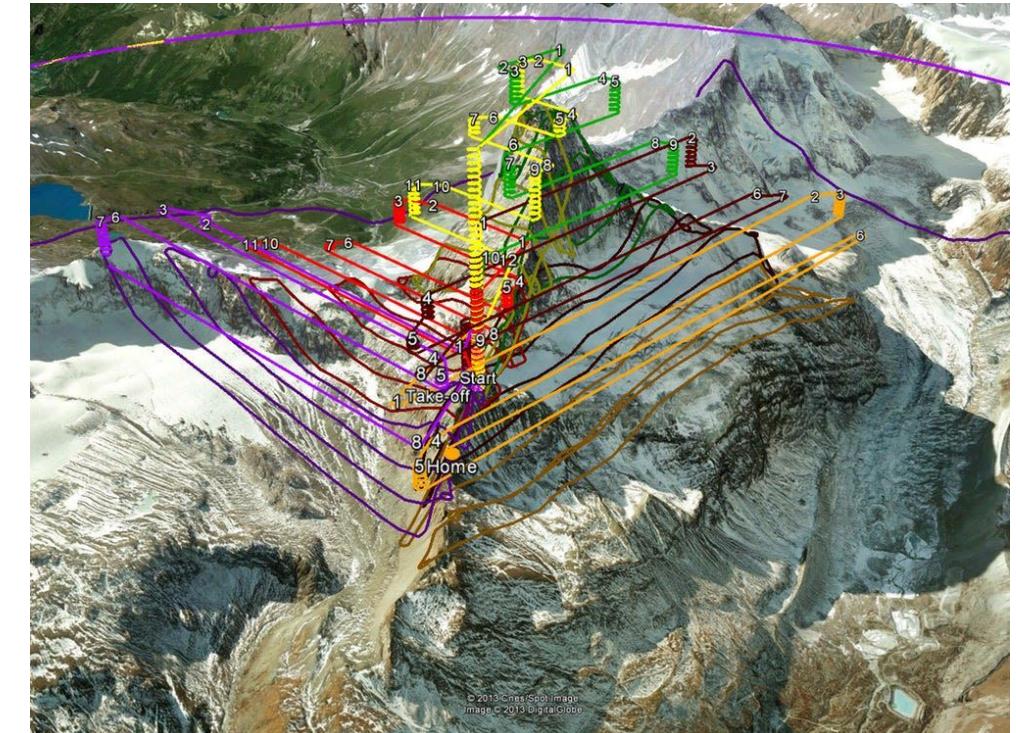
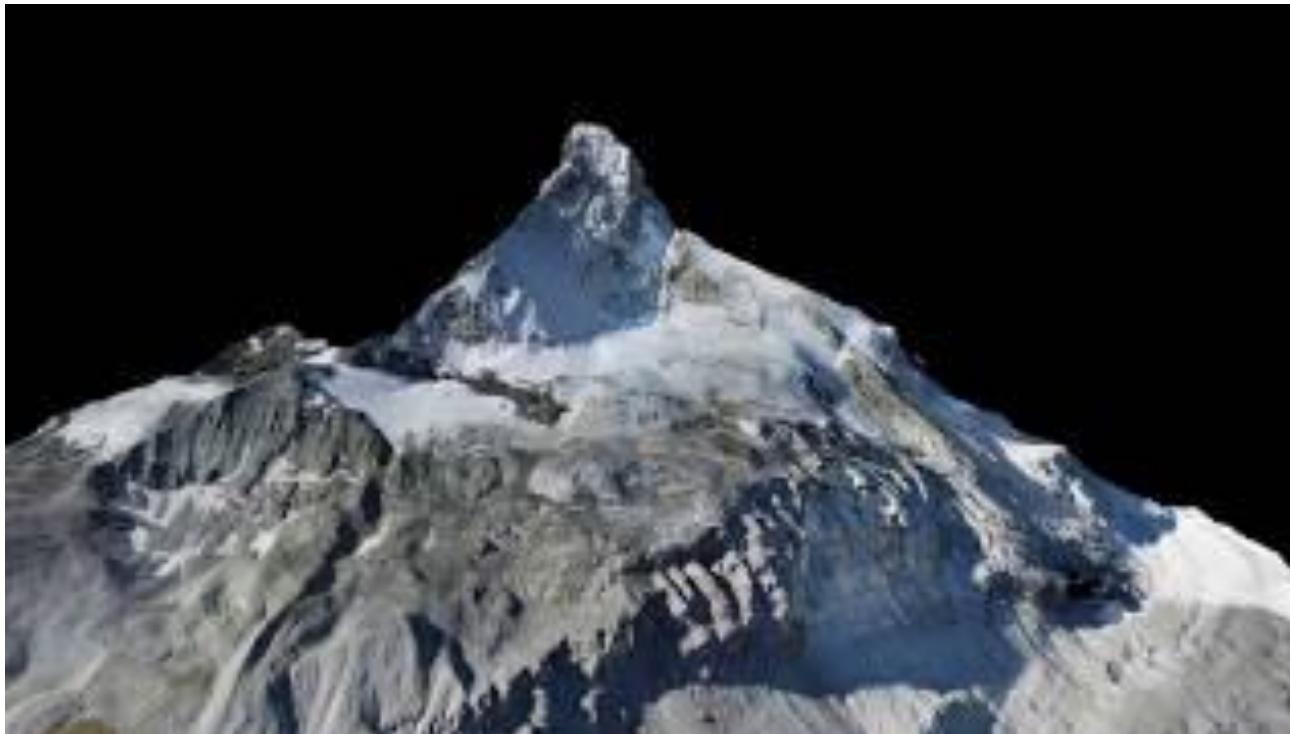
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Bachelor Thesis  
Autonomous Systems Lab, ETH Zurich

# Motivation

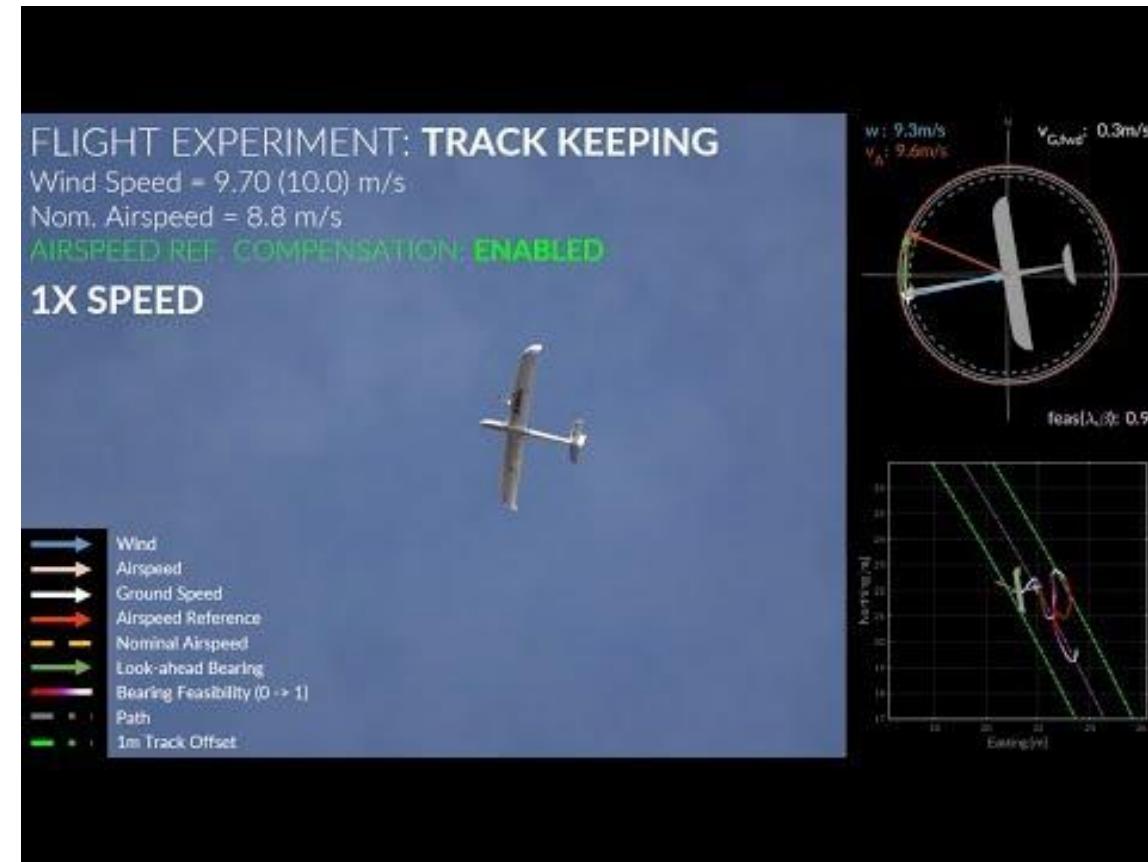
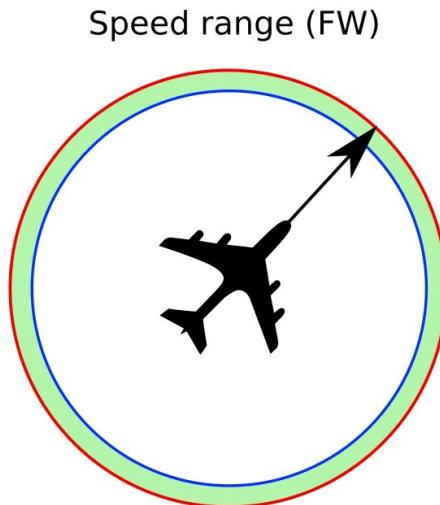
# Motivation



# Related Work

# Related Work: Path Following on Fixed Wing

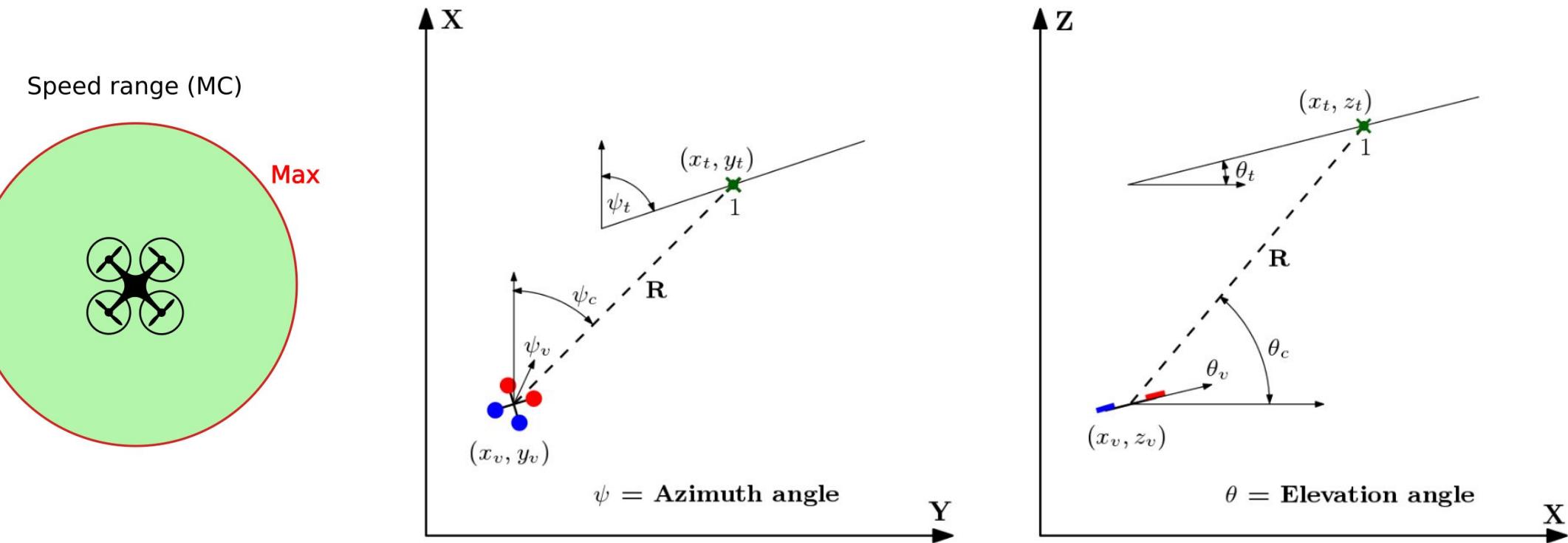
- Nonlinear Control [Stastny, IROS, 2019]



T. Stastny. "On Flying Backwards: Preventing Runaway of Small, Low-speed, Fixed-wing UAVs in Strong Winds". IROS, 2019

# Related Work: Path Following on Multirotor

- Virtual Target Pursuit [Manjunath, 2016]

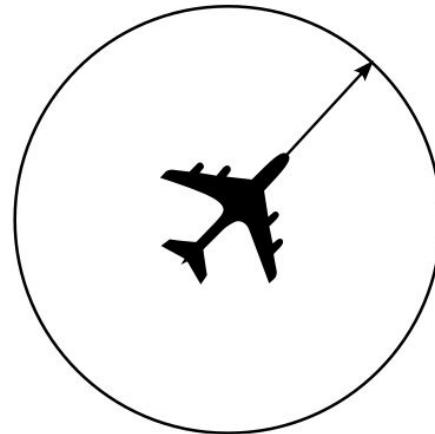


Manjunath, A. R.. "Path following by a quadrotor using virtual target pursuit guidance." (2016).

# Problem Definition

# Limitation of conventional Fixed Wing Path Following

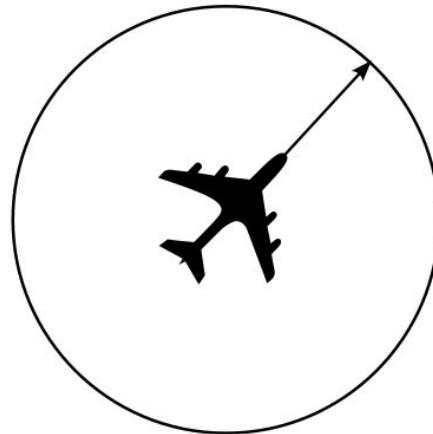
Nominal Speed (FW)



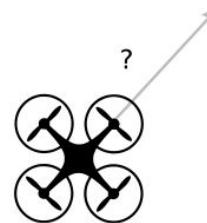
- Fixed Wing flies at a constant ‘Nominal speed’

# Limitation of conventional Fixed Wing Path Following

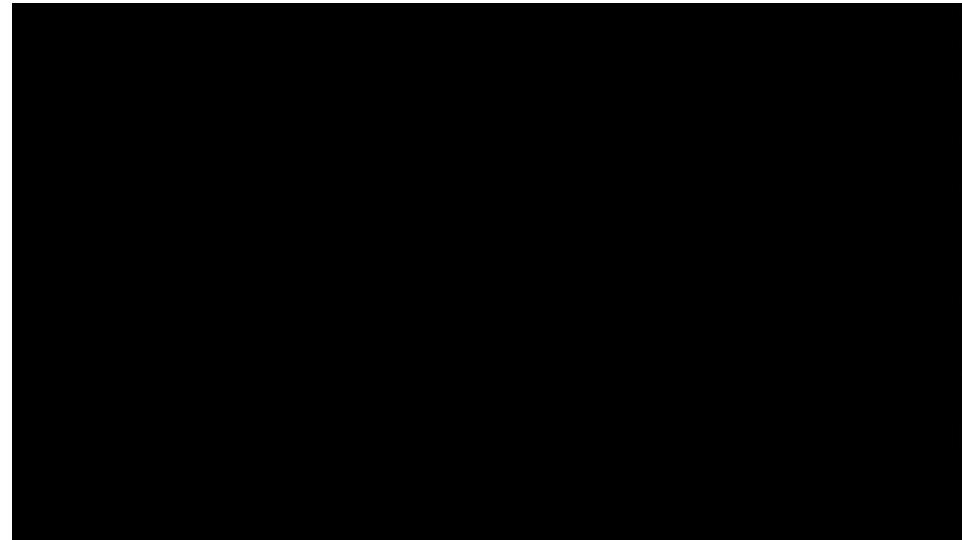
Nominal Speed (FW)



Nominal Speed = 0 (MC)

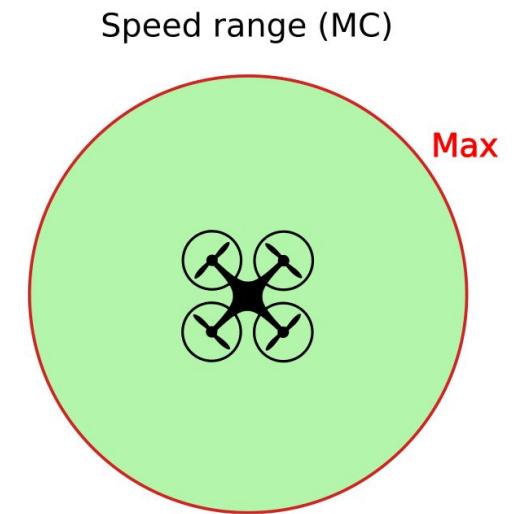
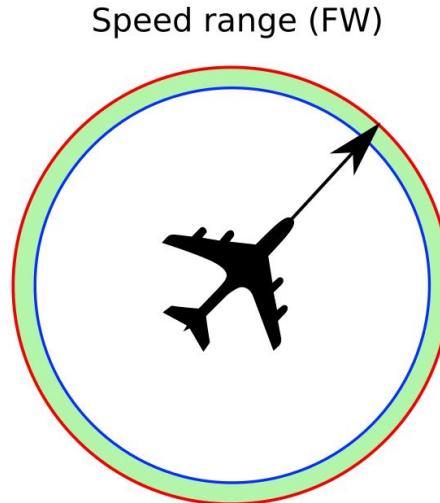


- **Fixed Wing** flies at a constant '**Nominal speed**'
- **Multirotors** can have a huge speed range, including '**stopping**'.
  - Using FW guidance on MC results in unintended approach path that isn't meant for the ground velocity profile



# Goal

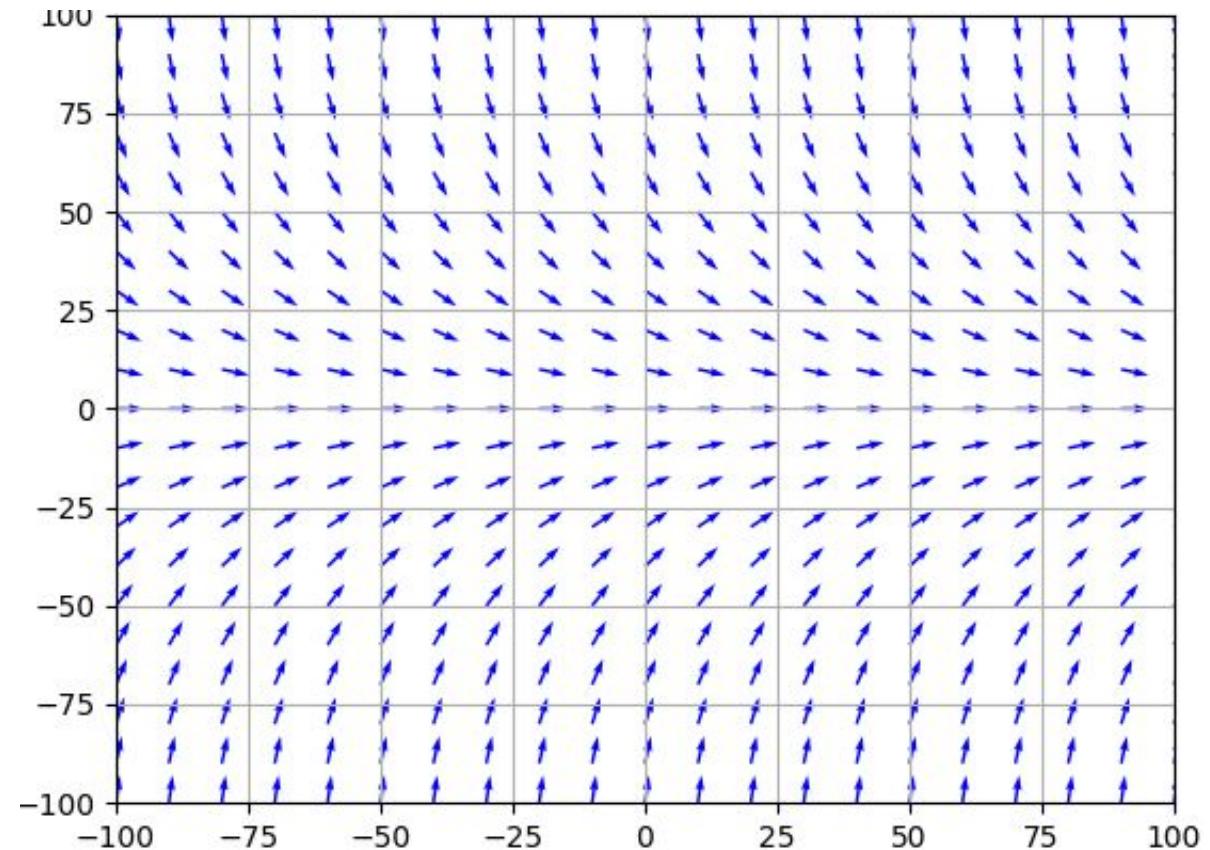
**“Unified Path Following Guidance that can be used by Fixed Wing, Multirotor, and Hybrid VTOL utilizing their full maneuverability envelope”**



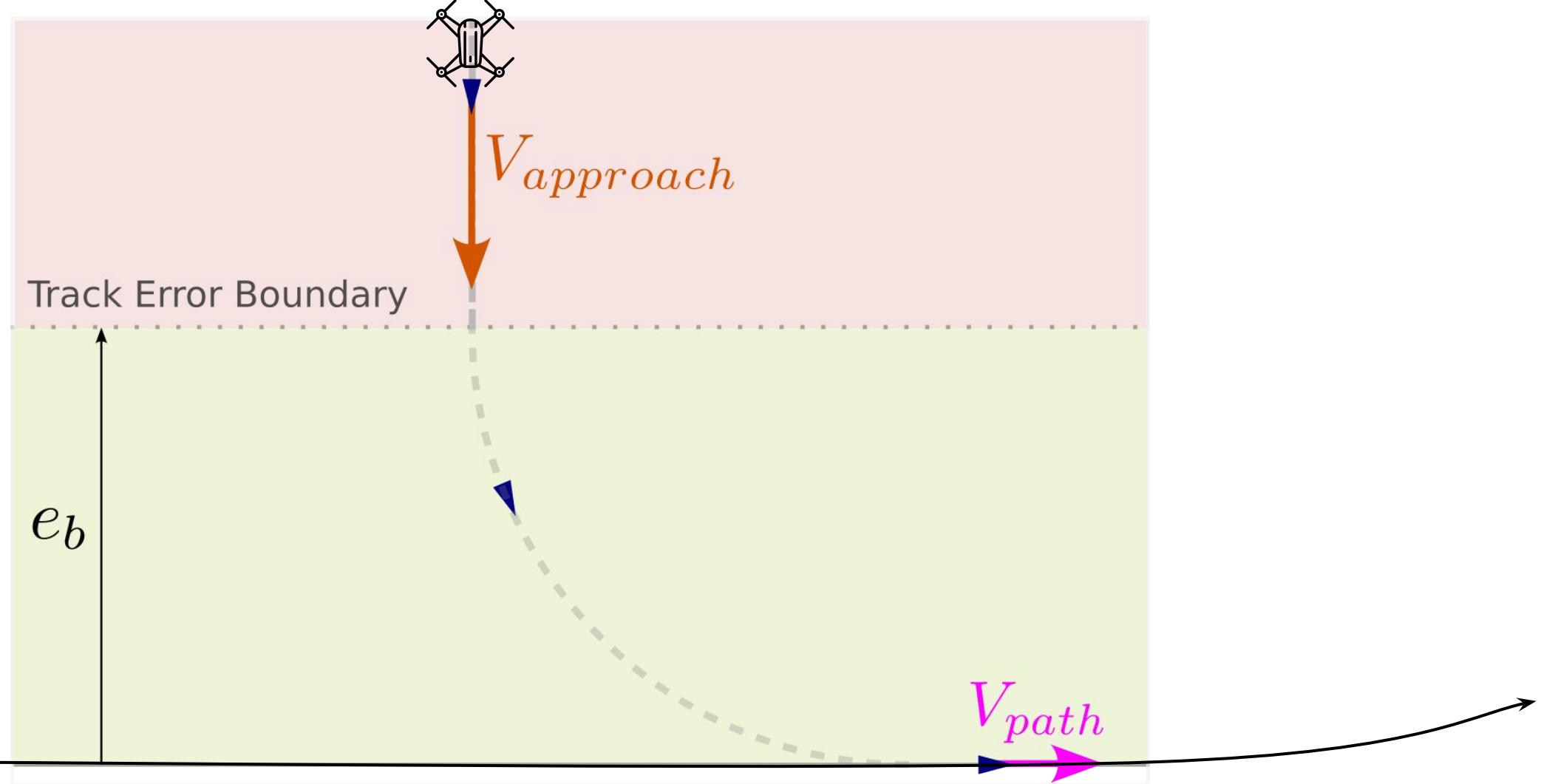
# Approach

- **Vector Field Method**
    - If vector is followed, converges to path
    - Desired course setpoint is generated
1. Geometric: more **generic**
  2. Can be followed by **any** vehicle type!

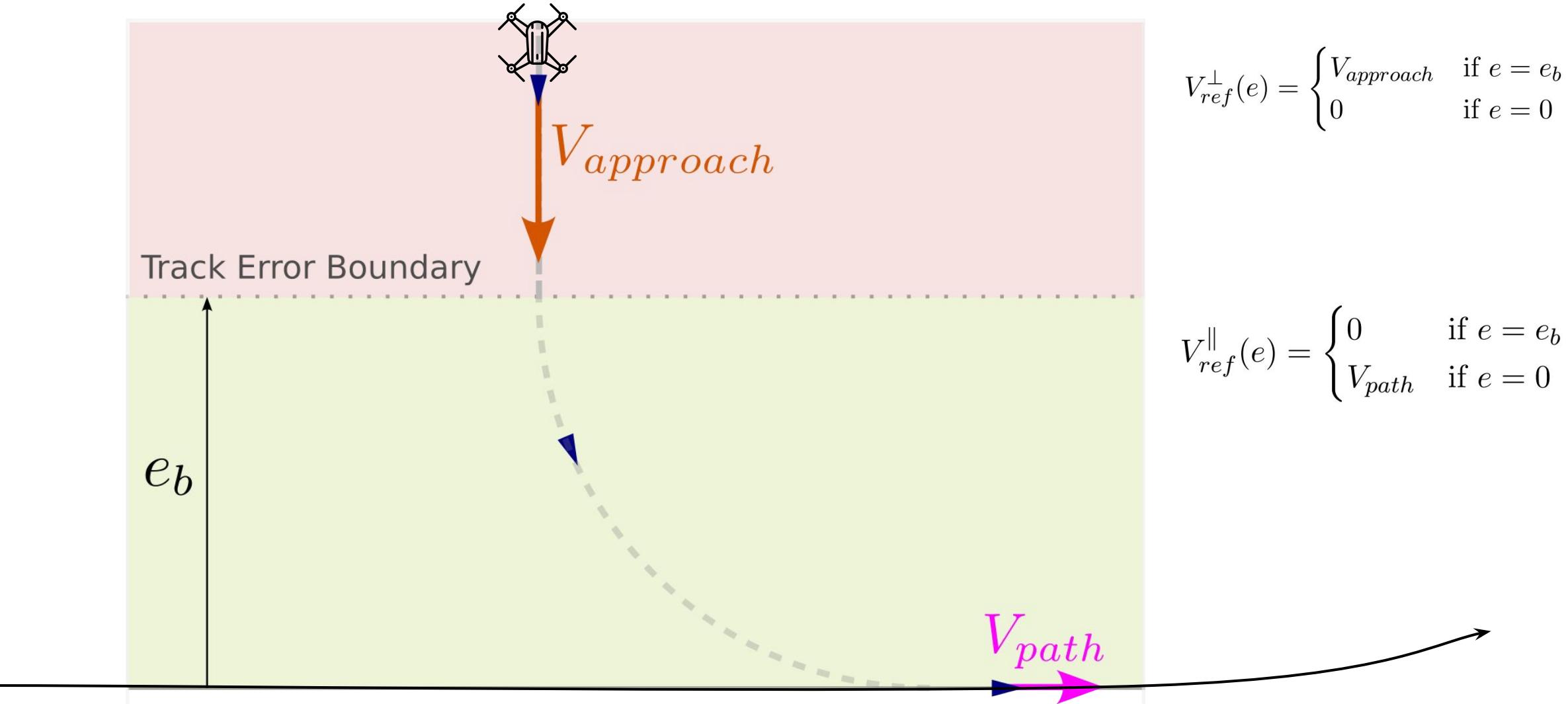
Other methods: Optimal control, etc.



# Approach: Overview



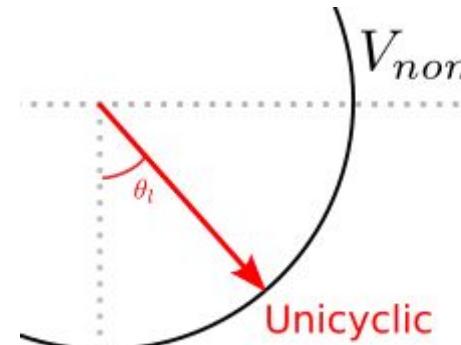
# Approach: Problem Definition



# Methods

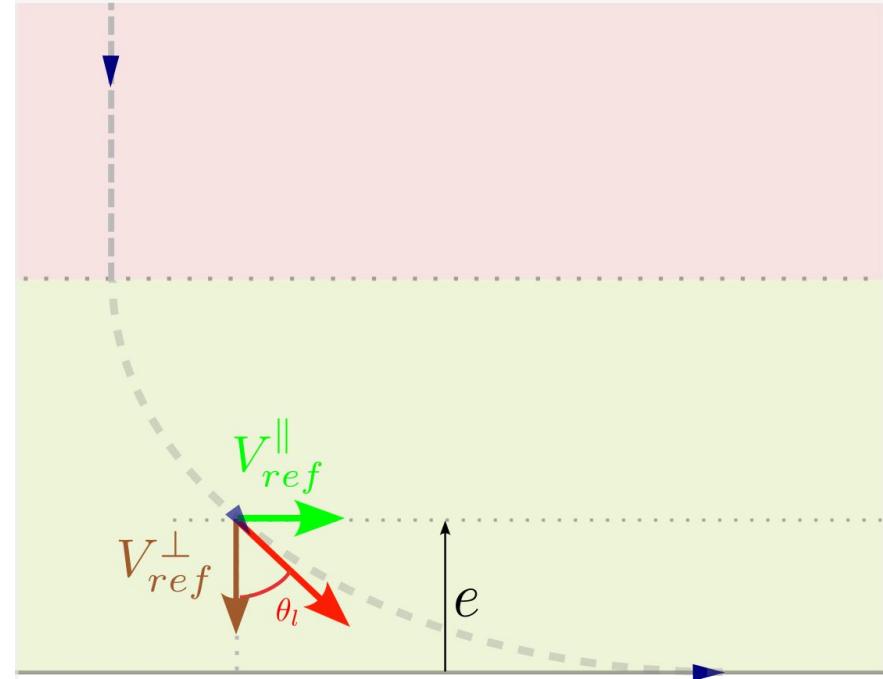
# Methods

## Unicyclic (Original)



$$V_g^{\parallel} = V_{nom} * \sin(\theta_l)$$

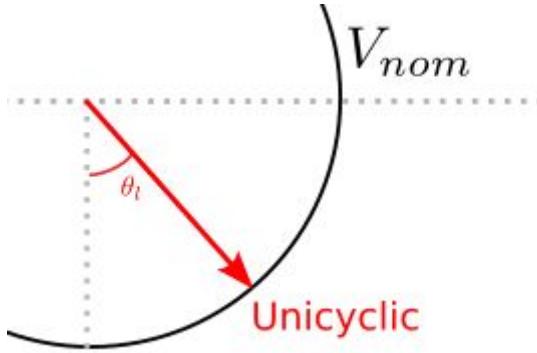
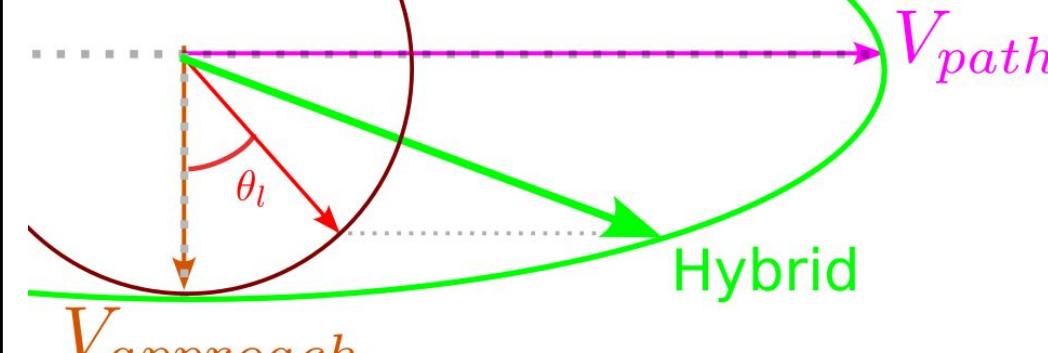
$$V_g^{\perp} = V_{nom} * \cos(\theta_l)$$



$$\bar{e} = \frac{e}{e_b}$$

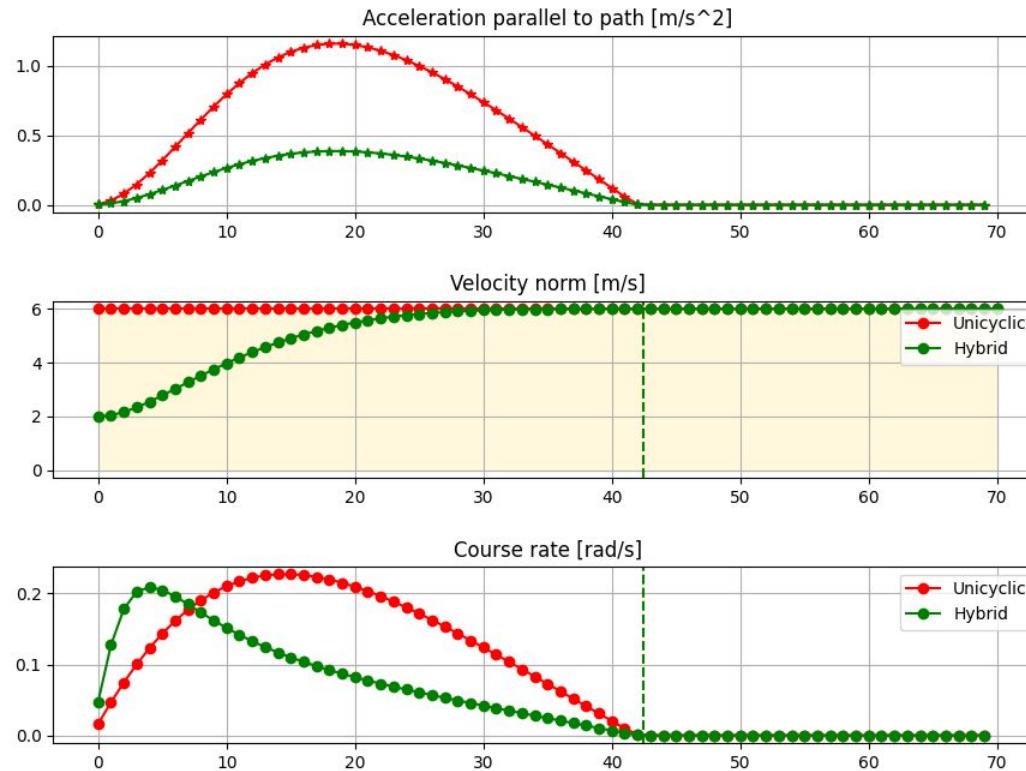
$$\theta_l = constrain\left(\frac{\pi}{2}(1 - \bar{e})^2, 0, \frac{\pi}{2}\right)$$

# Methods

Unicyclic (Original)	Hybrid (Proposed)
 <p>Unicyclic</p>	 <p>Hybrid</p>
$V_g^{\parallel} = \boxed{V_{nom}} * \sin(\theta_l)$ $V_g^{\perp} = \boxed{V_{nom}} * \cos(\theta_l)$	$V_g^{\parallel} = \boxed{V_{path}} * \sin(\theta_l)$ $V_g^{\perp} = \boxed{V_{approach}} * \cos(\theta_l)$

# Evaluation

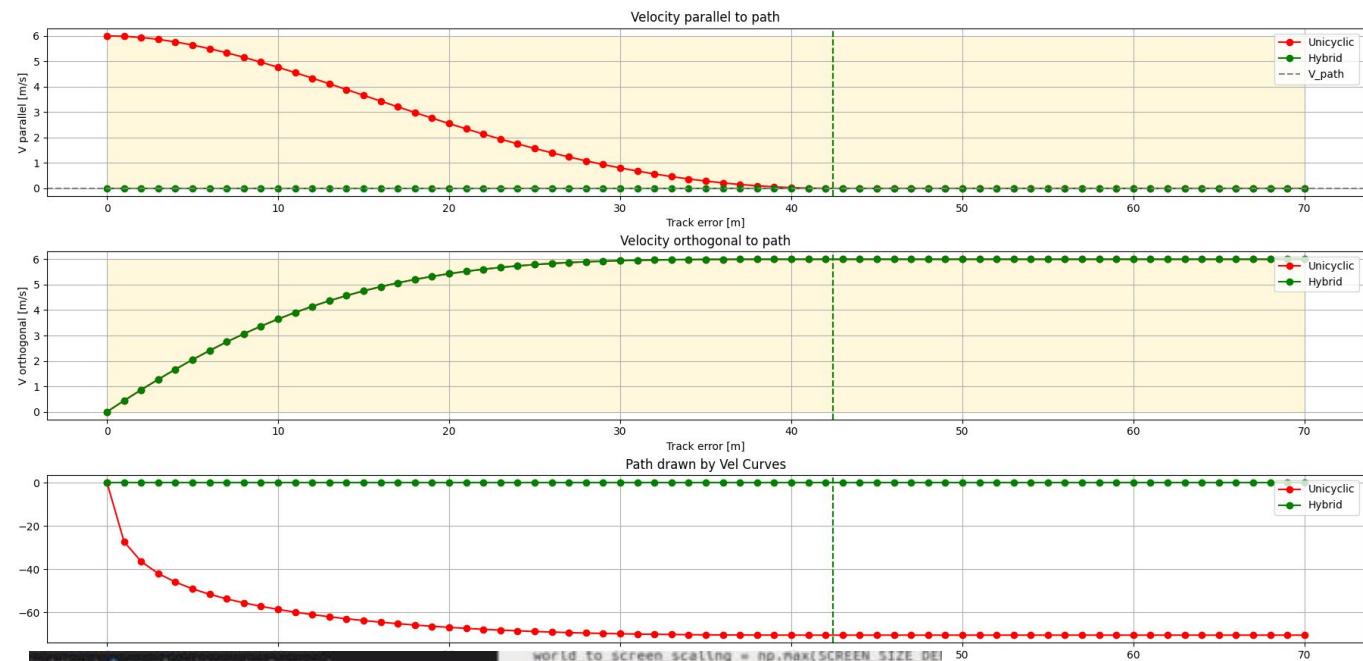
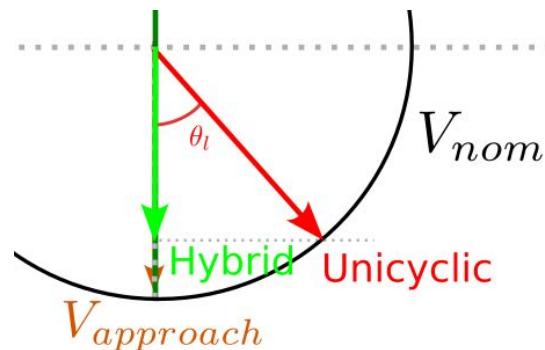
# Evaluation Criteria



- **Approach speed:** Does it approach at required speed?
- **Path speed:** Does it reach the speed on path?
- **Monotonicity:** Monotonic ground speed profile
- **Acceleration:** Doesn't exceed vehicle's limit
- **Course rate:** Doesn't exceed vehicle's yaw rate limit (FW)

# Evaluation: Zero speed on path

Parameter	Value
$V_{nom}$	6
$V_{approach}$	6
$V_{path}$	0



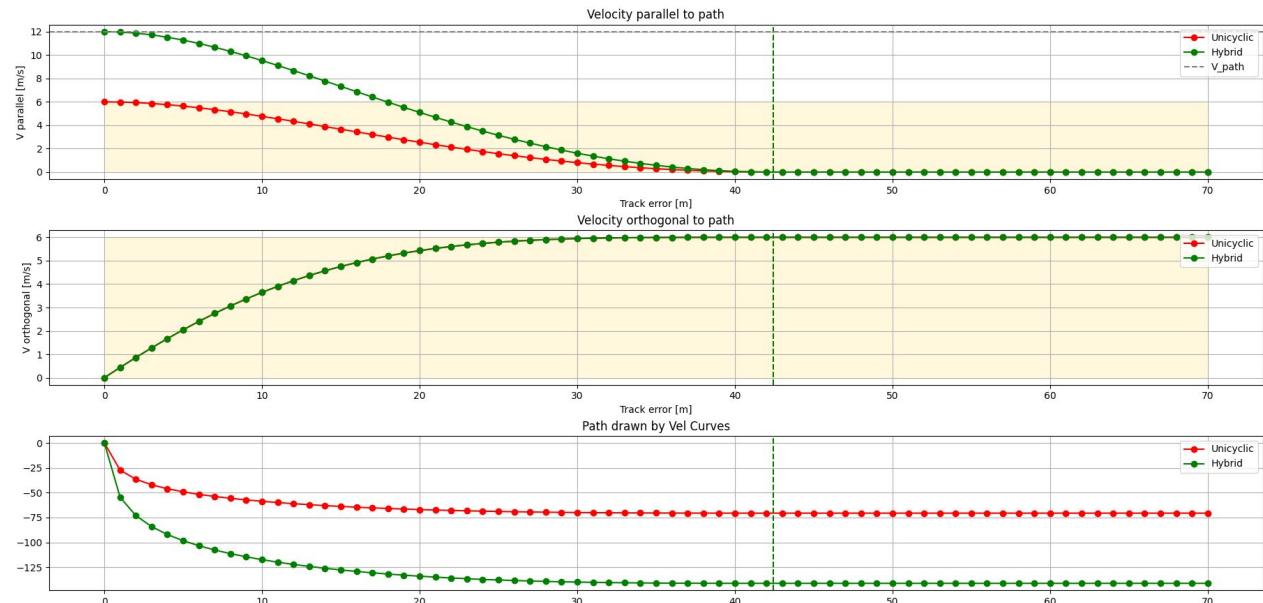
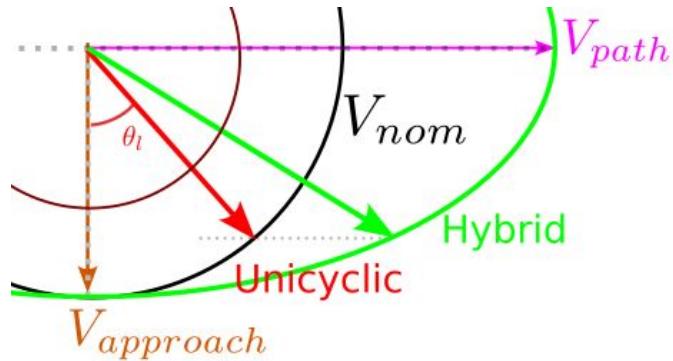
```

simulations > mc_npig_pointmass_twoCurves.py ...
  9  inputs = pybullet
10  import gym
11
12  import matplotlib.pyplot as plt
13
14  from Windywings.envs import MCPointMass
15
16  from theories.velocity.reference_algorithms import *
17
18  # Curve visualization aid
19  # from theories.acc.course_rates_of_vel_curves import *
20
21  # Rendering
22  SCREEN_SIZE_DEFAULT: tuple[Literal[1000], Literal[1000]] = (1000, 1000)
23  MULTICOPTER_CIRCLE_RADIUS: Literal[10] = 10 # radius of the multicopter
24
25  UNICYCLIC_COLOR: Literal['red'] = 'red'
26  HYBRID_UNICYCLIC_COLOR: Literal['green'] = 'green'
27  MAX_ACCEL_COLOR: Literal['brown'] = 'brown'
28  HYBRID_UNICYCLIC_UNIFORM_COLOR: Literal['orange'] =
29
30  # Vehicle constraints
31  MIN_VELOCITY: float = 0.0
32  NOM_VELOCITY: float = 6.0
33  MAX_VELOCITY: float = 15.0
34  VEL_RANGE: ndarray[Any, dtype] = np.array([MIN_VELOC
35  MAX_ACCELERATION: float = 7.0 # [m/s^2] Max Accel in

```

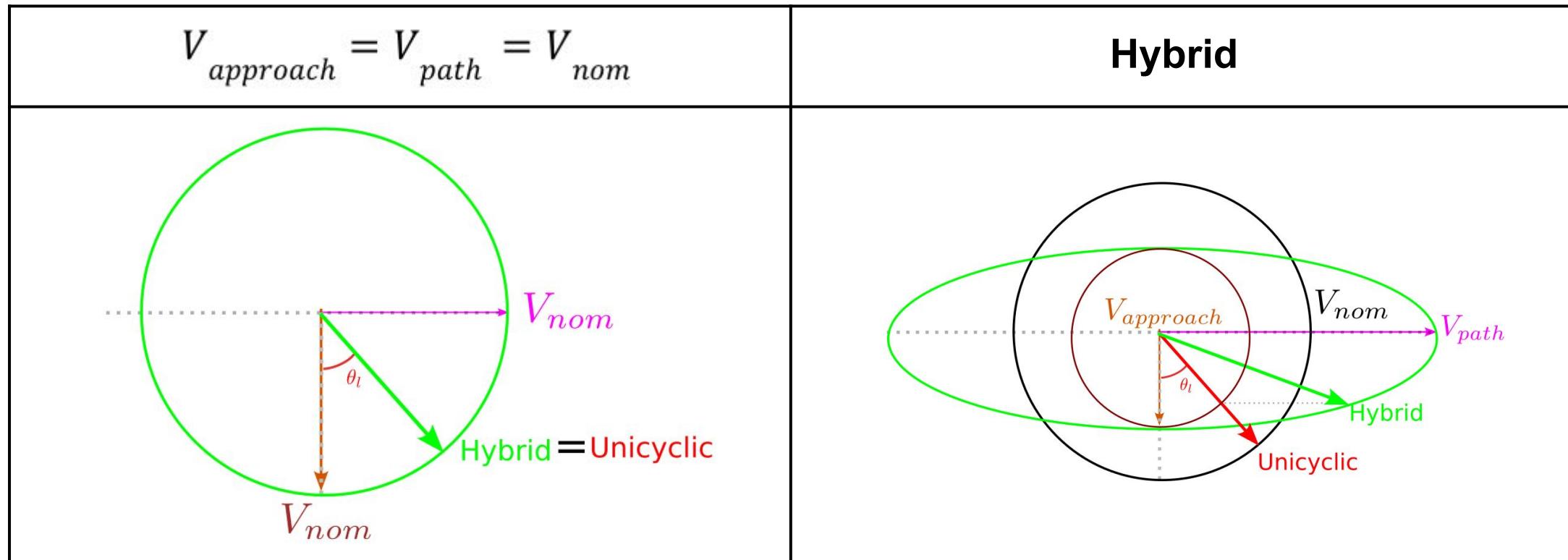
# Evaluation: High speed on path

Parameter	Value
$V_{nom}$	6
$V_{approach}$	6
$V_{path}$	<b>12</b>



# Evaluation: Is the FW case still supported?

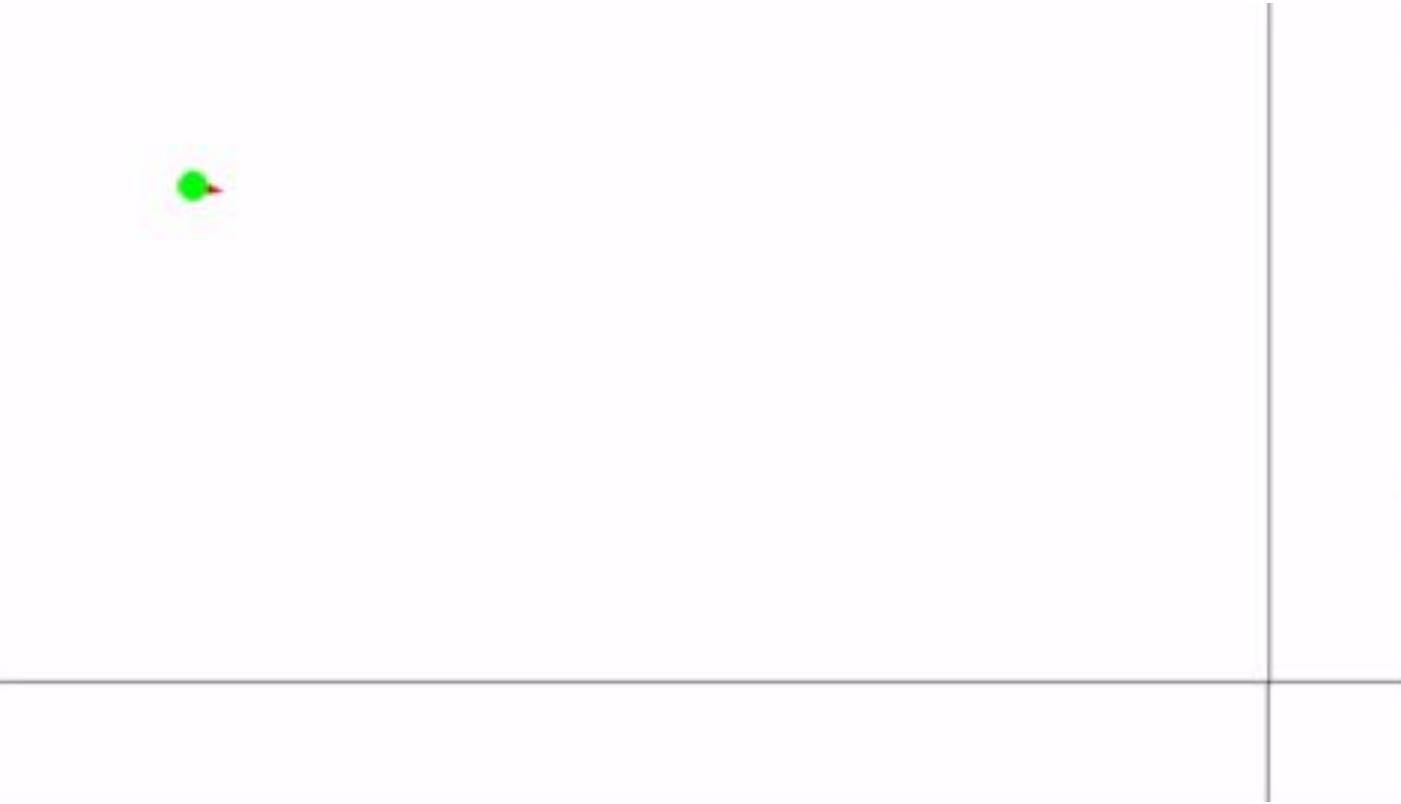
- Fixed Wing (Unicyclic) is just a **special case** where:  $V_{approach} = V_{path} = V_{nom}$



# Result: Simulation

**Unicyclic:** 10 m/s nominal speed

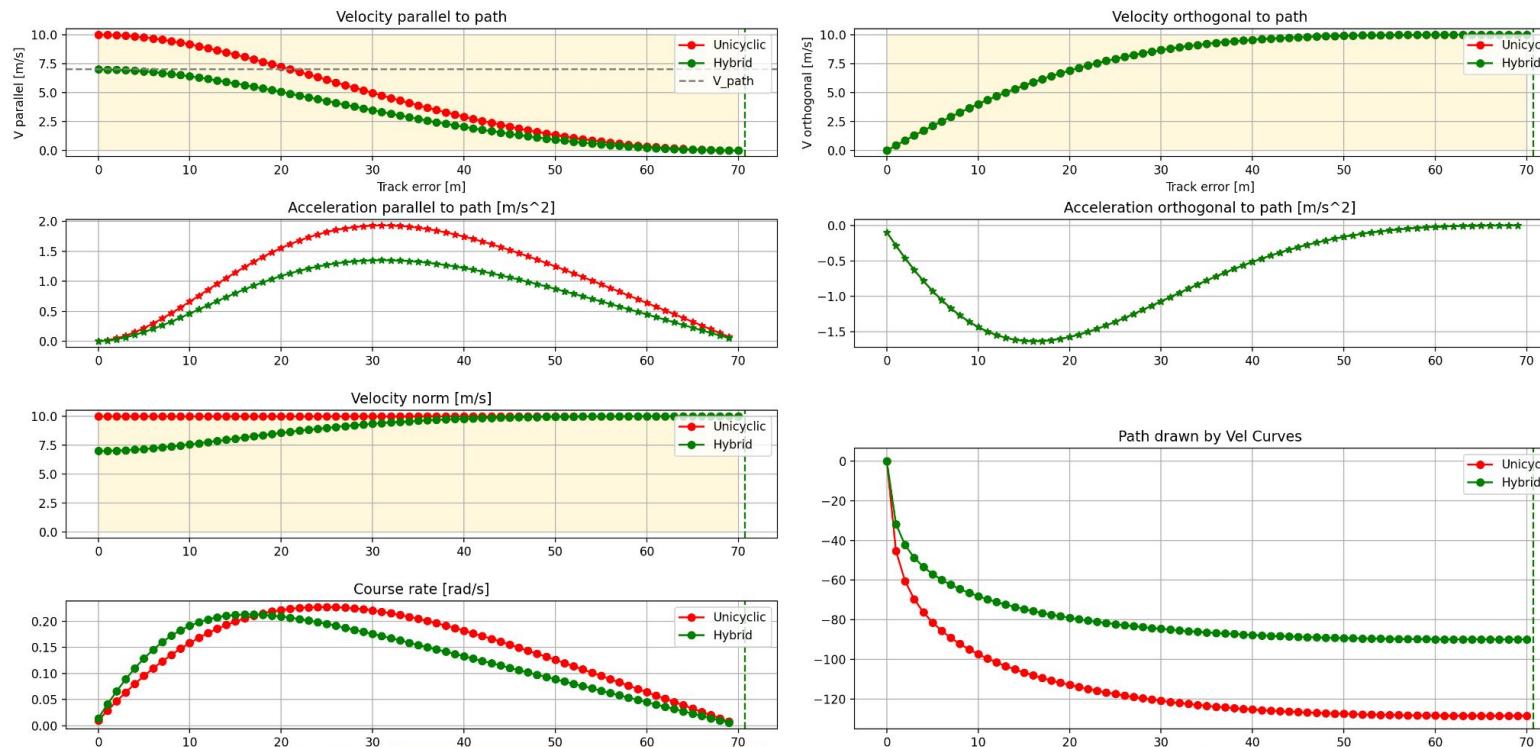
**Hybrid:** 10 m/s approach & 7 m/s path speed



# Result: Simulation

**Fixed Wing:** 10 m/s nominal speed

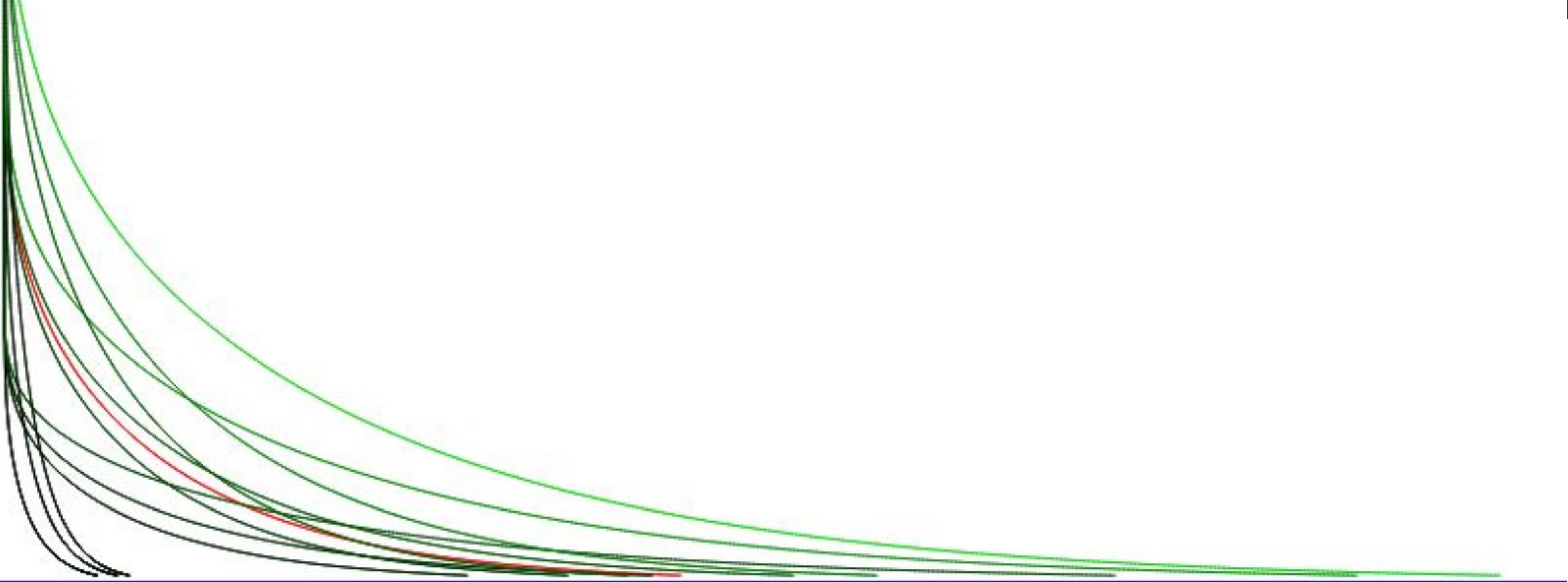
**Multirotor:** 10 m/s approach & 7 m/s path speed



- **Monotonicity:** Guaranteed (Ellipsoidal velocity)
- **Acceleration limit** is within Fixed wing's limit (feasible for MC)

# Discussion and Outlook

- Achievements 🎉
  - **Unified Path Following** formulation applicable to both multirotor and fixed wing
- Limitations 🙄
  - **Dynamic constraints** hasn't been considered (Acceleration / Jerk)
- Future Work 💪
  - Implementation & Testing on a **real** Hybrid VTOL
  - Incorporating **wind** into guidance (air velocity profile)



Thank you 

Special thanks to: Jay, Florian, David, and Thomas

# QnA Backup slides

# Path Following Evaluation Criteria

Criteria	Description	Evaluation
<b>Time to convergence</b> on a path [s]	Time required by the vehicle to converge to the path when following the ground velocity vector field with no error $t_{conv} = - \int_{e_b}^0 \frac{1}{V_g^\perp} de = e_b \cdot \int_0^1 \frac{1}{V_g^\perp} d\hat{e} \text{ (when } e_b \text{ is constant)}$	Smaller the better
<b>Track error boundary length</b> [m]	$e_b$	Smaller the better
<b>Converging path parallel distance</b> [m]	Path-parallel distance travelled to converge to path when following ground velocity vector field with no error $d_{conv} = - \int_{e_b}^0 V_g^\parallel \cdot \frac{e}{V_g^\perp} de = e_b \cdot \int_0^1 V_g^\parallel \cdot \frac{\hat{e}}{V_g^\perp} d\hat{e} \text{ (when } e_b \text{ is constant)}$	Smaller the better
<b>Velocity on Path fulfilled</b> [bool]	$V_g^\parallel = V_{path}$ when $\hat{e} = 0$	Needs to be True
<b>Speed monotonicity</b> [bool]	Whether the magnitude of velocity grows or decreases consistently throughout track error boundary $\text{Monotonicity} = \left\{ \begin{array}{l} \frac{d}{de} \ V_g(e)\  \geq 0 \mid \text{for all } e \in [0, e_b] \\ \text{Or} \\ \frac{d}{de} \ V_g(e)\  \leq 0 \mid \text{for all } e \in [0, e_b] \end{array} \right\}$ This can be compared via: $V_g^\perp (\frac{d}{de} V_g^\perp) + V_g^\parallel (\frac{d}{de} V_g^\parallel)$	Needs to be True
<b>Total acceleration RMS</b> [m/s <sup>2</sup> ]	Root-Mean-Square value of acceleration $acc_{rms} = \frac{1}{e_b} * \sqrt{- \int_{e_b}^0 (\  \frac{d}{dt} V_g(e) \ ^2) de} = \sqrt{\int_0^1 (\  \frac{d}{dt} V_g(\hat{e}) \ ^2) d\hat{e}} \text{ (when } e_b \text{ is constant)}$ $= \frac{1}{e_b} \sqrt{\int_0^1 (\  V_g^\perp \cdot \frac{d}{de} V_g(\hat{e}) \ ^2) d\hat{e}} = \frac{1}{e_b} \sqrt{\int_0^1 ([ (V_g^\perp)^2 \cdot ((\frac{d}{de} V_g^\perp)^2 + (\frac{d}{de} V_g^\parallel)^2) ]) d\hat{e}}$	Smaller the better
<b>Maximum acceleration total</b> [m/s <sup>2</sup> ]	Maximum total acceleration $acc_{max} = \max\{ \frac{d}{dt} V_g(e) \mid e \in [0, e_b] \} = \frac{1}{e_b} \cdot \max\{ V_g^\perp \cdot \sqrt{(\frac{d}{de} V_g^\perp)^2 + (\frac{d}{de} V_g^\parallel)^2} \mid \hat{e} \in [0, 1] \} \text{ (when } e_b \text{ is constant)}$	Smaller the better

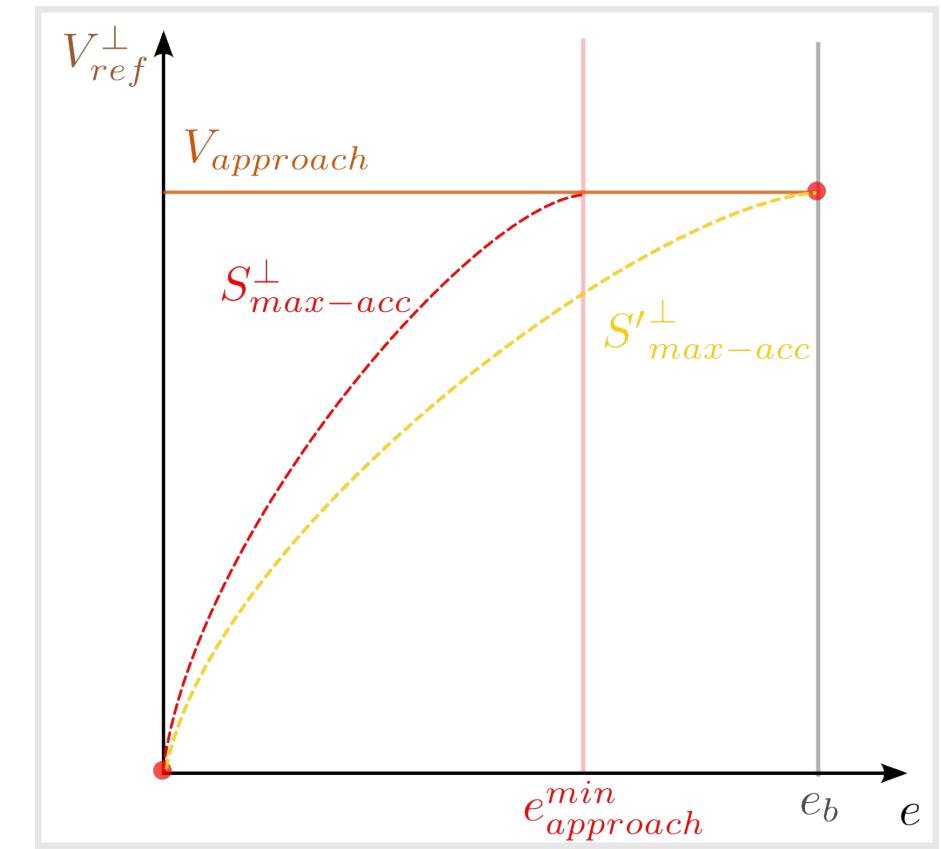
# Maximum Acceleration Method: Orthogonal Velocity

$$e_{approach}^{min} = \frac{V_{approach}^2}{2a_{max}^\perp}$$

With  $e_b = \frac{V_{approach}^2}{2a_{max}^\perp}$

$$S_{max-acc}^\perp(e) = \begin{cases} \sqrt{2a_{max}^\perp} * \sqrt{e} & \text{if } e < e_b \\ V_{approach} & \text{if } e \geq e_b \end{cases}$$

$$\begin{aligned} S'_{max-acc}^\perp(e) &= S_{max-acc}^\perp\left(\frac{e_{approach}^{min}}{e_b} * e\right) \\ &= \begin{cases} \sqrt{\frac{2a_{max}^\perp e_{approach}^{min}}{e_b}} * \sqrt{e} & \text{if } e < e_b \\ V_{approach} & \text{if } e \geq e_b \end{cases} \\ &= \begin{cases} V_{approach} * \sqrt{\frac{e}{e_b}} & \text{if } e < e_b \\ V_{approach} & \text{if } e \geq e_b \end{cases} \end{aligned}$$



$$V_{ref}^\perp(e) = \begin{cases} V_{approach} & \text{if } e = e_b \\ 0 & \text{if } e = 0 \end{cases}$$

# Maximum Acceleration Method: Parallel Velocity

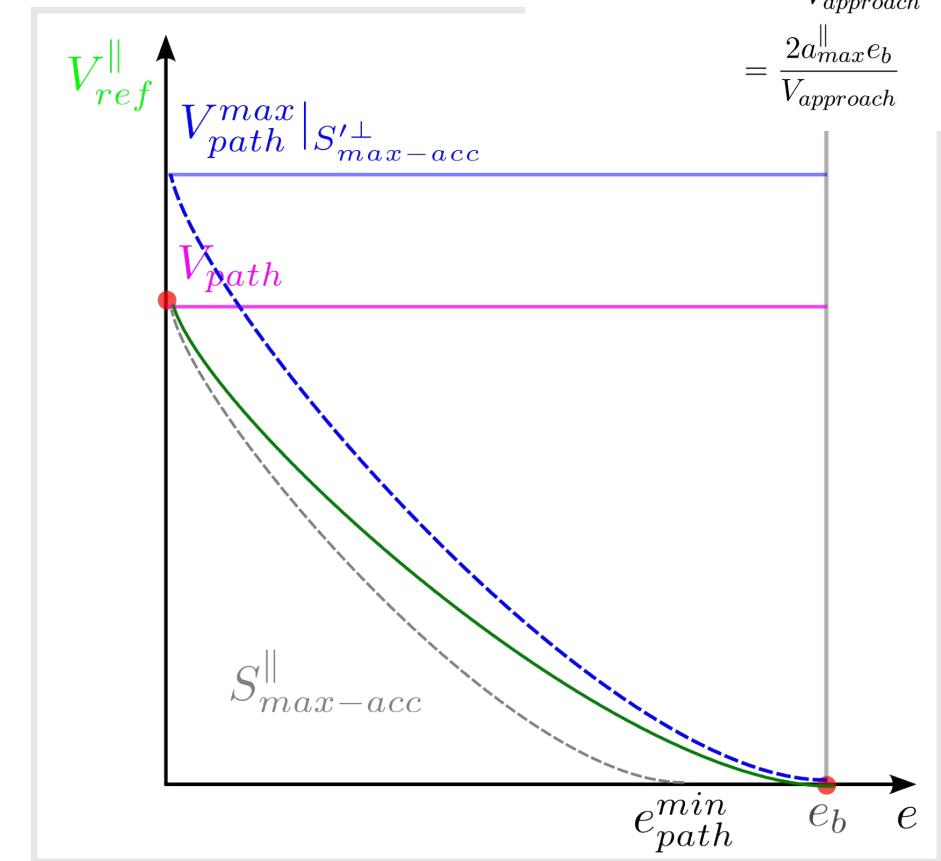
$$\begin{aligned}\frac{d}{de} V_{ref}^{\parallel}(e) &\geq -\frac{a_{max}^{\parallel}}{S'^{\perp}_{max-acc}(e)} \\ &= \begin{cases} -\frac{a_{max}^{\parallel}}{V_{approach}} * \sqrt{\frac{e_b}{e}} & \text{if } e < e_b \\ -\frac{a_{max}^{\parallel}}{V_{approach}} & \text{if } e \geq e_b \end{cases}\end{aligned}$$

Since  $V_{path} = \int_{e_{path}^{min}}^0 -\frac{a_{max}^{\parallel}}{V_{approach}} \sqrt{\frac{e_b}{e}} de$ ,

$$= -\frac{a_{max}^{\parallel} \sqrt{e_b}}{V_{approach}} * [2\sqrt{e}]_{e_{path}^{min}}^0,$$

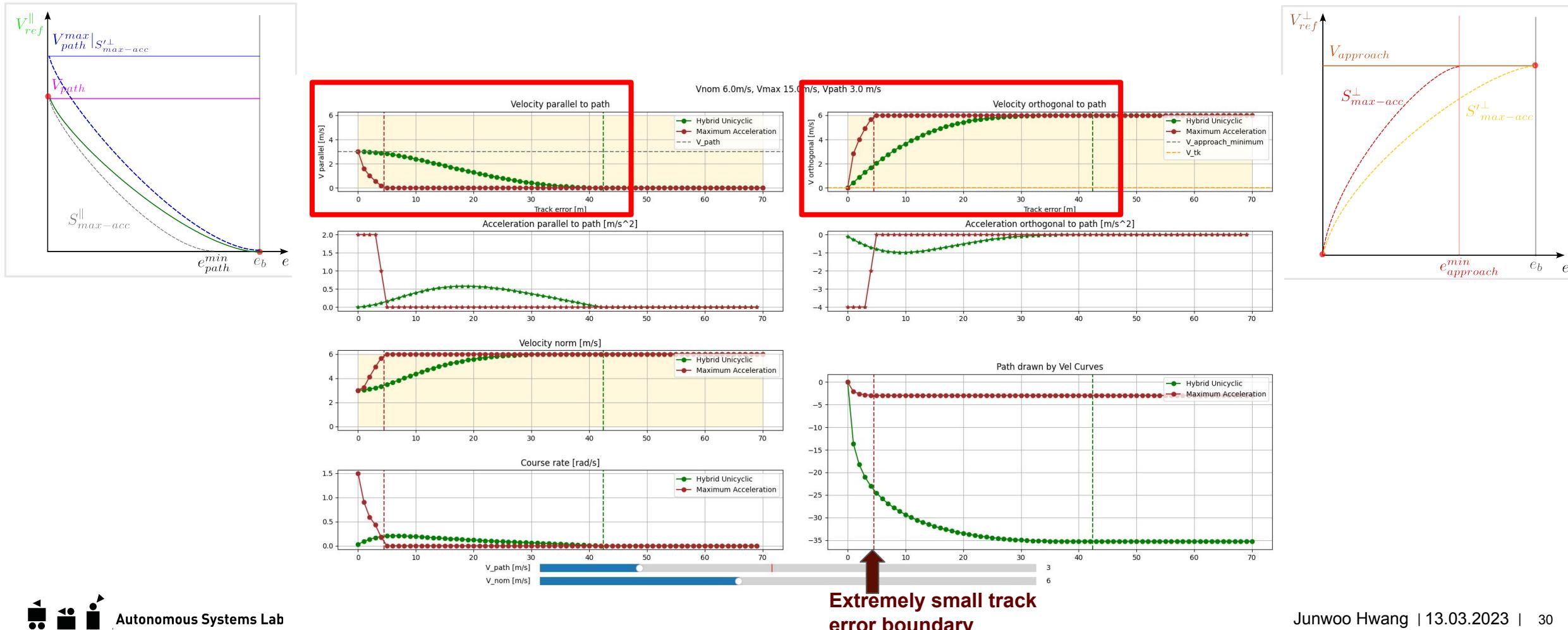
Therefore,  $e_{path}^{min}|_{S'^{\perp}_{max-acc}} = [\frac{V_{path} V_{approach}}{2a_{max}^{\parallel}}]^2 * \frac{1}{e_b}$

$$\begin{aligned}S'^{\parallel}_{max-acc}(e) &= S_{max-acc}^{\parallel} \left( \frac{e_{path}^{min}|_{S'^{\perp}_{max-acc}}}{e_b} * e \right) \\ &= \begin{cases} V_{path} - \frac{2a_{max}^{\parallel} \sqrt{e_b}}{V_{approach}} * \sqrt{\frac{e_{path}^{min}|_{S'^{\perp}_{max-acc}}}{e_b} * e} & \text{if } e < e_b \\ 0 & \text{if } e \geq e_b \end{cases} \\ &= \begin{cases} V_{path} * (1 - \sqrt{\frac{e}{e_b}}) & \text{if } e < e_b \\ 0 & \text{if } e \geq e_b \end{cases}\end{aligned}$$

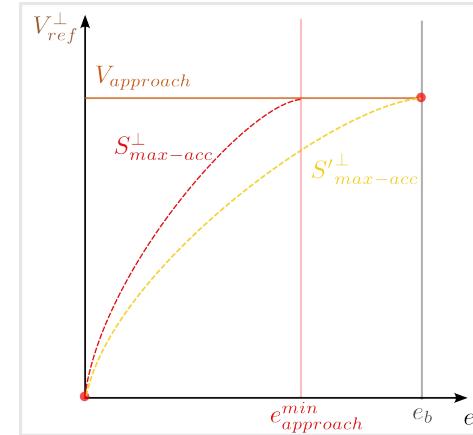
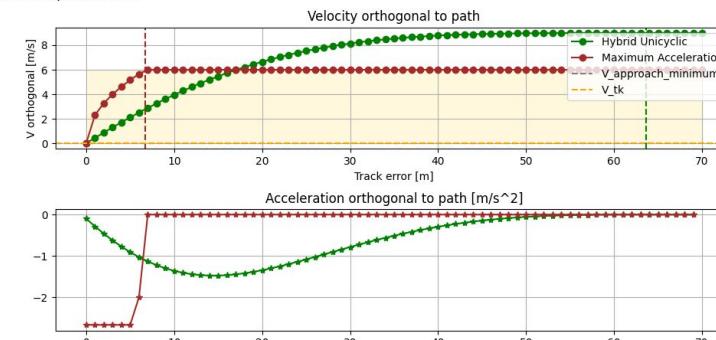
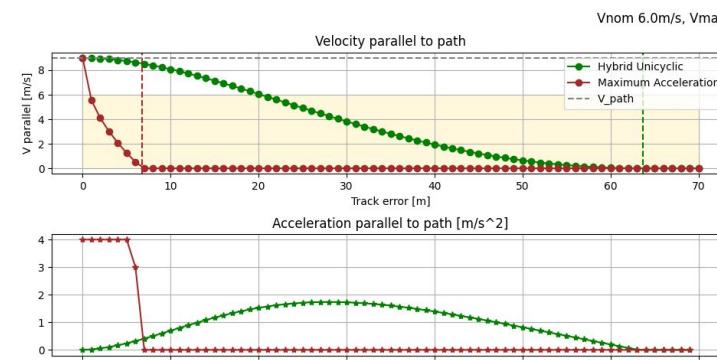
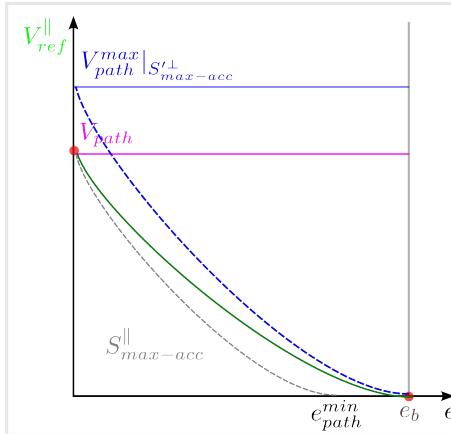


$$V_{ref}^{\parallel}(e) = \begin{cases} 0 & \text{if } e = e_b \\ V_{path} & \text{if } e = 0 \end{cases}$$

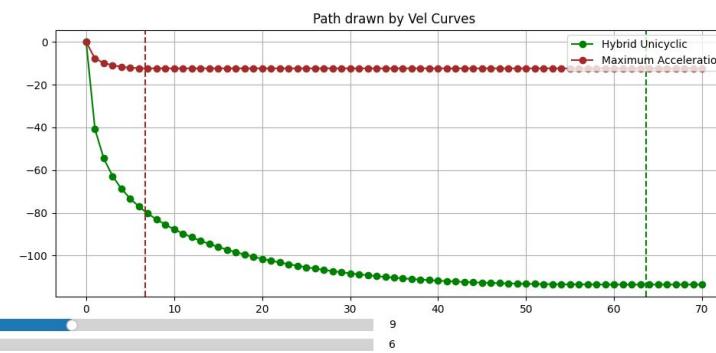
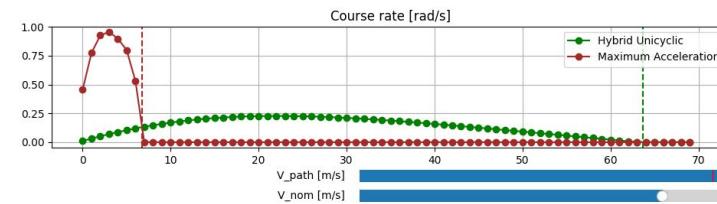
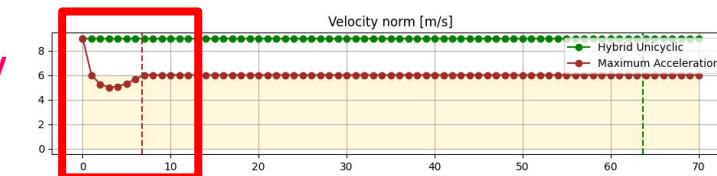
# Maximum Acceleration method



# Maximum Acceleration method



Monotonicity  
not satisfied



# Maximum Acceleration Formulation

$e$  = Current cross track error to path

$t_{const}$  = Track error boundary calculation time constant

$e_b$  = Track error boundary

$\hat{e}$  = Normalized track error boundary ( $= \frac{e}{e_b}$ )

$V_{nom}$  = Nominal speed of the vehicle (cruise)

$\Theta_{la}$  = Look ahead angle (away from orthogonal component to the path)

$V_g^\perp$  = Orthogonal ground reference velocity (towards the path)

$V_g^{\parallel}$  = Parallel ground reference velocity (along the path)

$e_{approach}^{\min}$  = Minimum track error boundary to satisfy approaching velocity constraint

$e_{path}^{\min}$  = Minimum track error boundary to satisfy on path velocity constraint

$a_{max}^\perp$  = Maximum orthogonal (to path) acceleration limit

$a_{max}^{\parallel}$  = Maximum parallel (to path) acceleration limit

$j_{max}$  = Maximum jerk limit

$$V_{approach} = \max(V_{nom}, V_{path})$$

$$e_{approach}^{\min} = \frac{[V_{approach}]^2}{2a_{max}^\perp}$$

$$e_{path}^{\min} = \left[ \frac{V_{path} V_{approach}}{2a_{max}^{\parallel}} \right]^2 * \frac{1}{e_{approach}^{\min}} = \left[ \frac{V_{path}}{a_{max}^{\parallel}} \right]^2 * \frac{a_{max}^\perp}{2}$$

$$\text{if}(e_{approach}^{\min} < e_{path}^{\min})$$

$$e_{approach}^{\min} = e_{path}^{\min} = \left[ \frac{V_{path} V_{approach}}{2a_{max}^{\parallel}} \right]$$

$$e_b = \max(e_{approach}^{\min}, e_{path}^{\min})$$

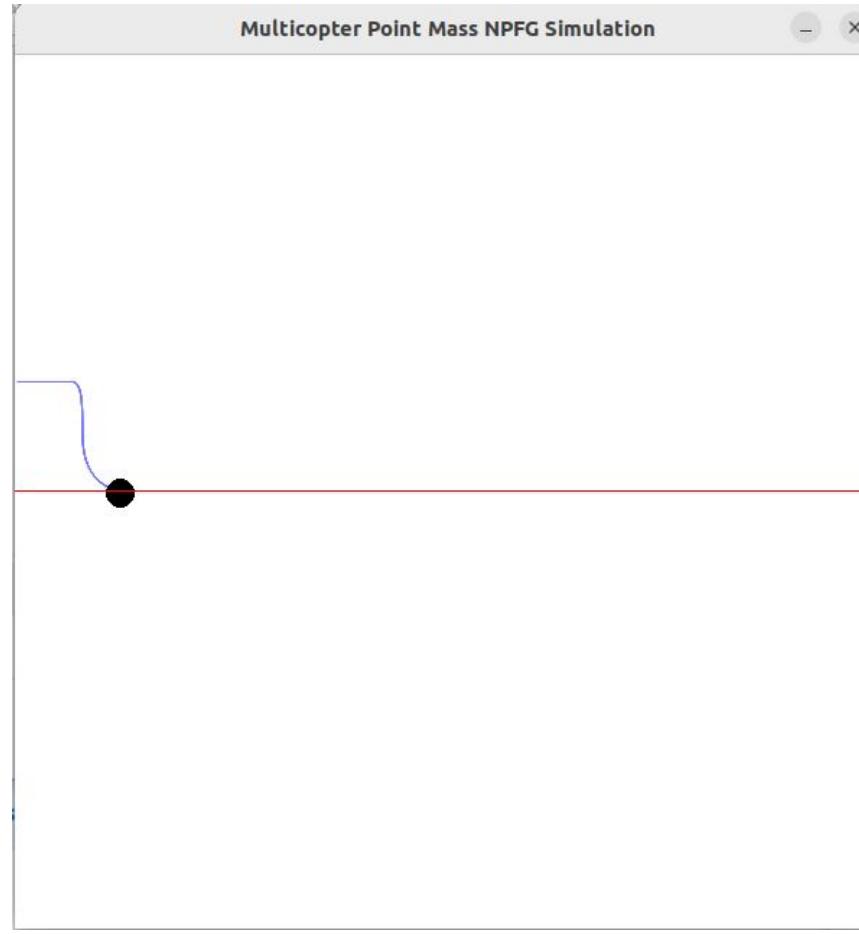
$$V_g^{\parallel} = V_{path} * (1 - \sqrt{\hat{e}})$$

$$V_g^\perp = V_{approach} * \sqrt{\hat{e}}$$

$$\text{return } [V_g^{\parallel}, V_g^\perp]$$



# Limitation of the unicyclic path following algorithm



What do we do when we want to go **slower** on the path?

- Unicyclic Path Following assumes that vehicle maintains the ‘nominal airspeed’, so **it can never stop**.
- Reducing nominal airspeed produces **weird artifacts**

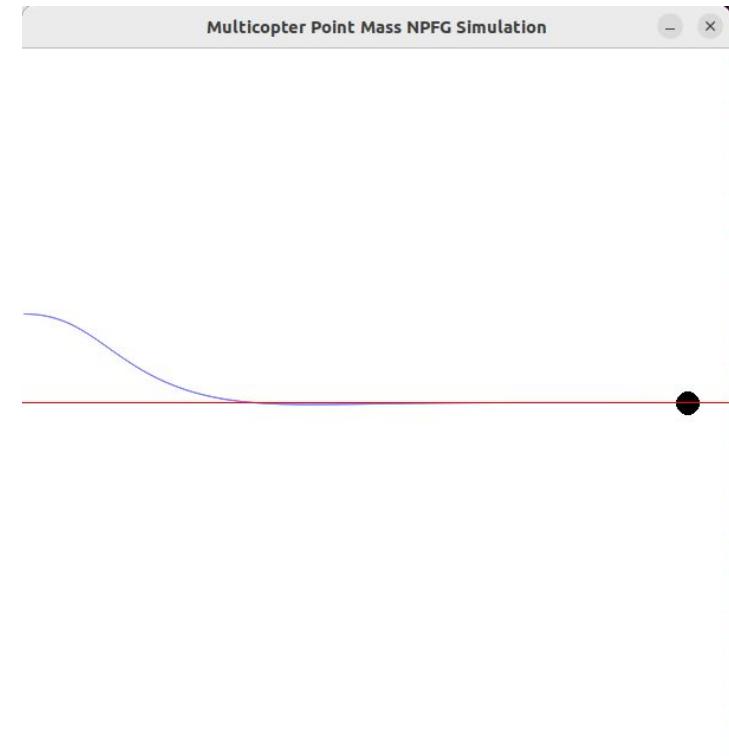
What about going **faster**?

- We can set nominal airspeed to a higher value, but it **alters the definition of ‘cruise speed’** (energy optimal speed)

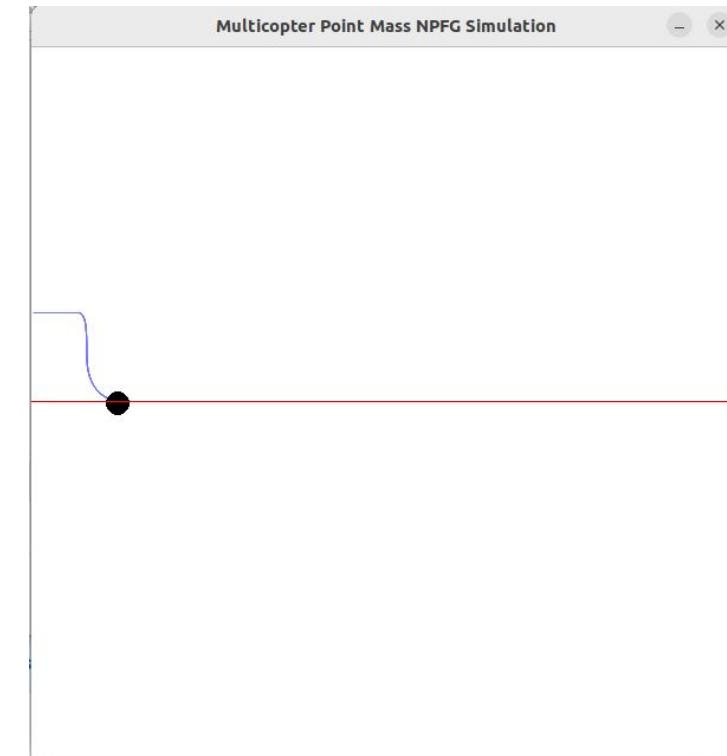


# Track-keeping

User-set minimum ground speed = 5.0 m/s



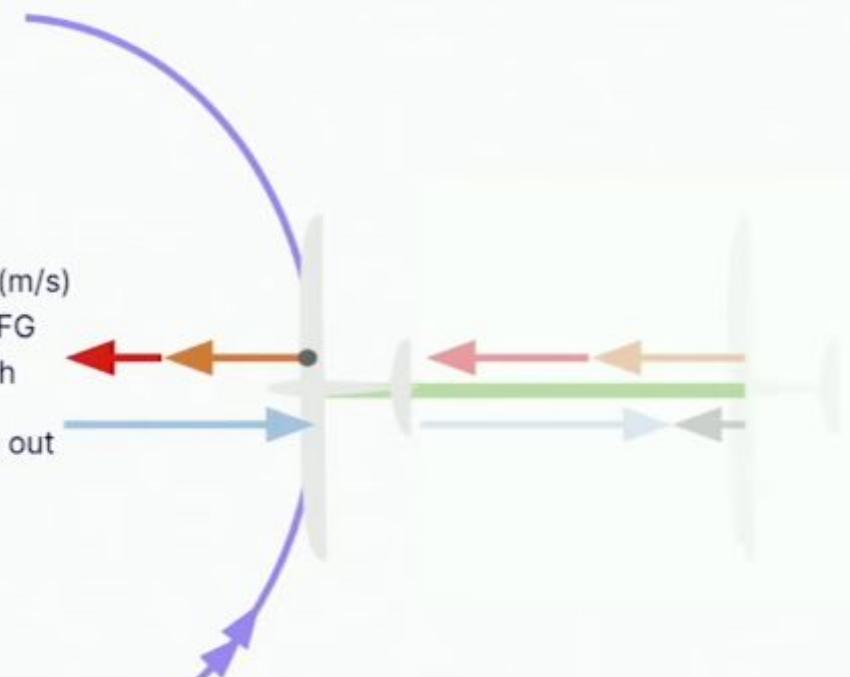
User-set minimum ground speed = 0.0 m/s



# Limitations of NPFG Track-keeping feature

## Track keeping

- Enable: `NPFG_TRACK_KEEP=1`
- Set `FW_GND_SPD_MIN=0`
- Far away from the track, `NPFG_GSP_MAX_TK` (m/s) is the maximum **forward** ground speed NPFG will command in its effort to return to the path
- The commanded ground speed aid is **zeroed** out once safely on the path



# Limitations of NPFG Track-keeping feature

```
327 float NPFG::minGroundSpeed(const float normalized_track_error, const float feas)
328 {
329     // minimum ground speed demand from track keeping logic
330     min_gsp_track_keeping_ = 0.0f;
331
332     if (en_track_keeping_ && en_wind_excess_regulation_) {
333         // zero out track keeping speed increment when bearing is feasible
334         // maximum track keeping speed increment is applied until we are within
335         // a user defined fraction of the normalized track error
336         min_gsp_track_keeping_ = (1.0f - feas) * min_gsp_track_keeping_max_ * math::constrain(
337             normalized_track_error / NTE_FRACTION, 0.0f,
338             1.0f);
339     }
340
341     // minimum ground speed demand from minimum forward ground speed user setting
342     float min_gsp_desired = 0.0f;
343
344     if (en_min_ground_speed_ && en_wind_excess_regulation_) {
345         min_gsp_desired = min_gsp_desired_;
346     }
347
348     return math::max(min_gsp_track_keeping_, min_gsp_desired);
349 } // minGroundSpeed
```



# Bearing Feasibility

Minimum  
Ground Speed

=

1 - feasibility

X

Minimum  
Ground Speed  
Track-Keeping

# Bearing Feasibility

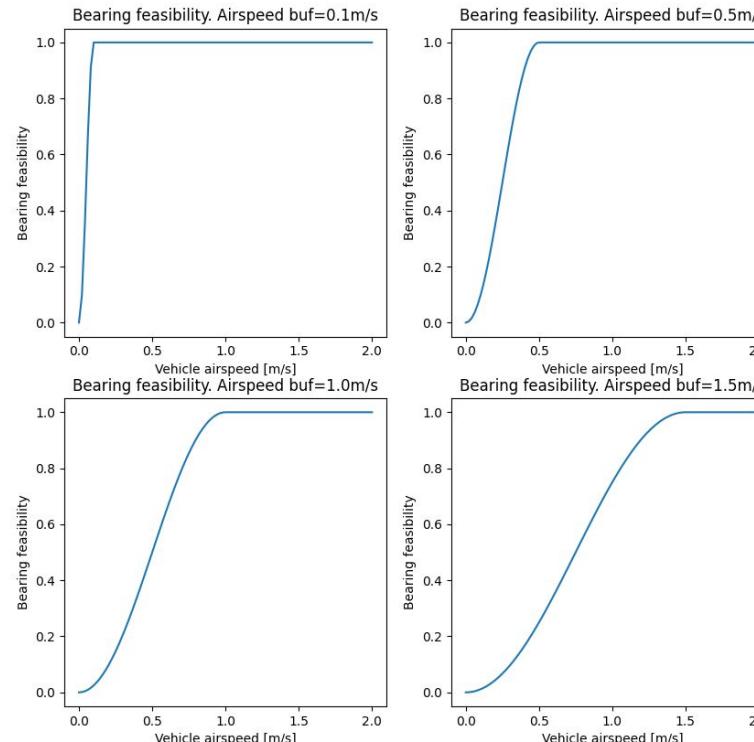
Minimum  
Ground Speed

=

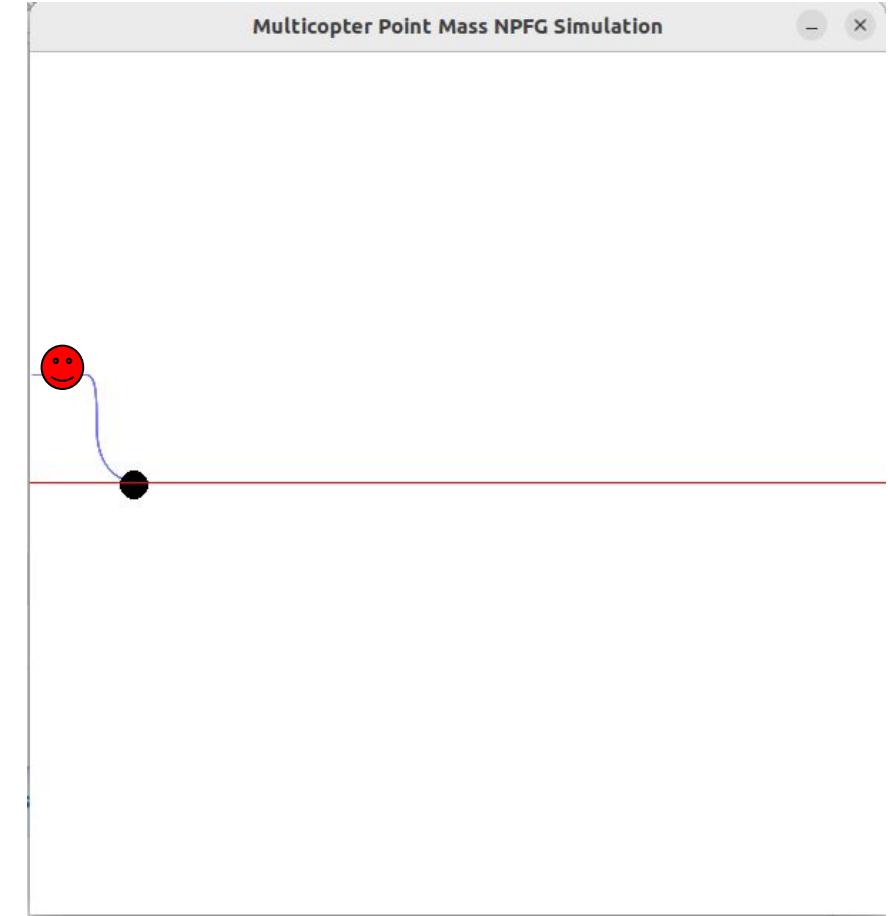
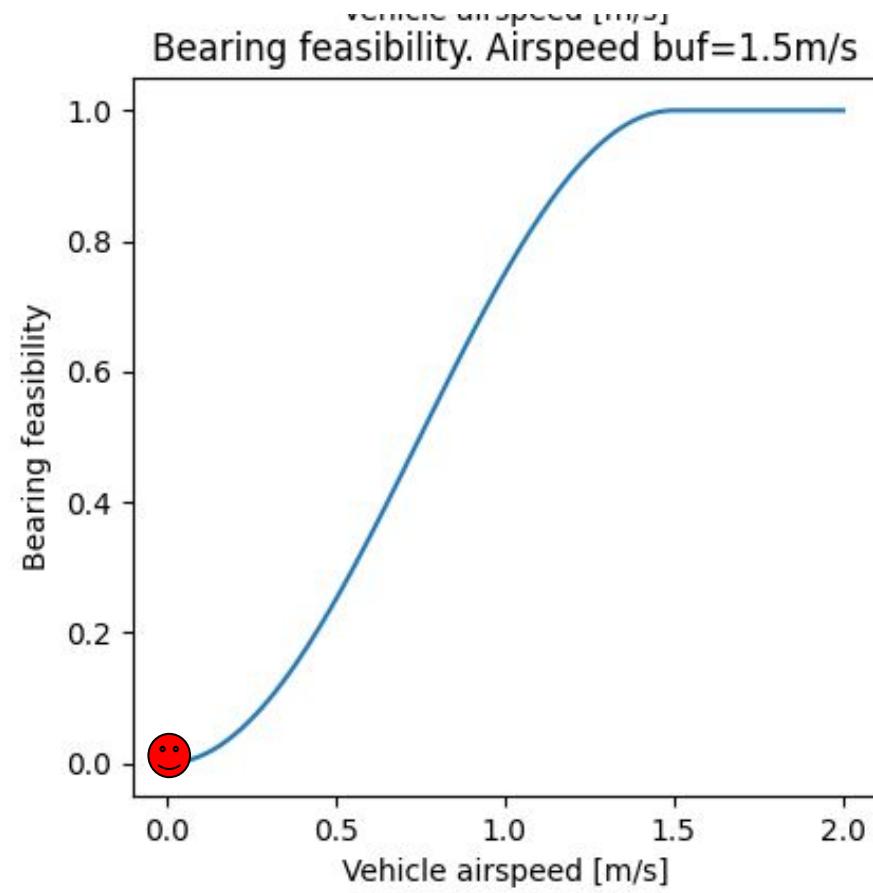
1 - feasibility

X

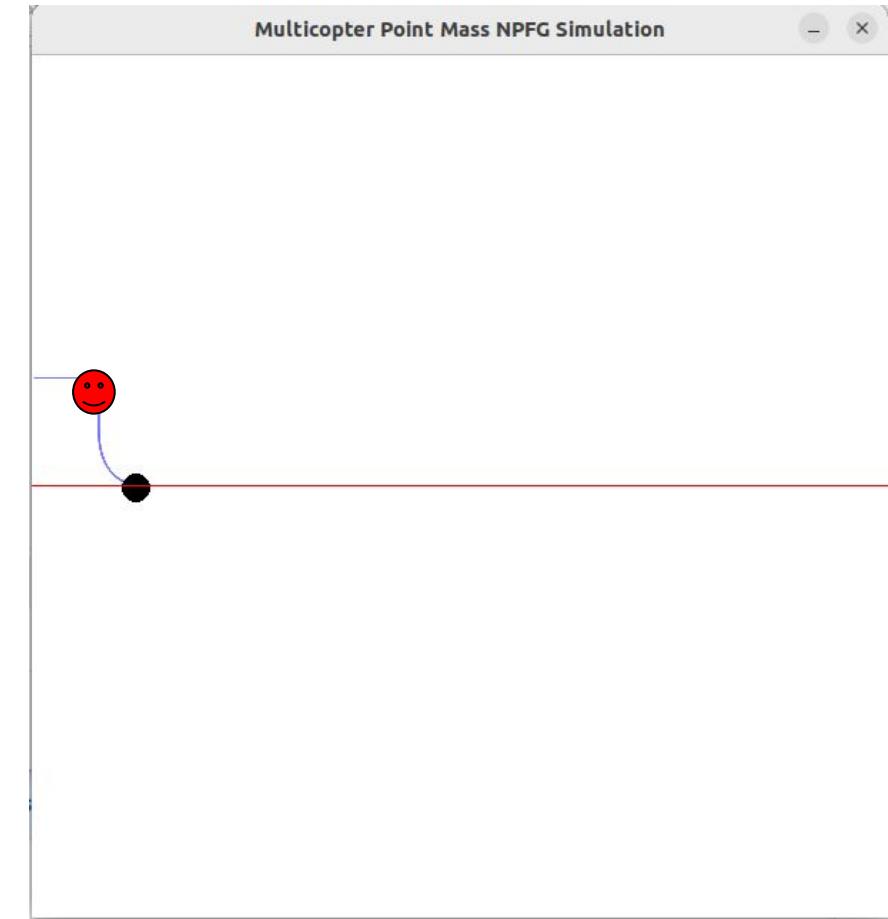
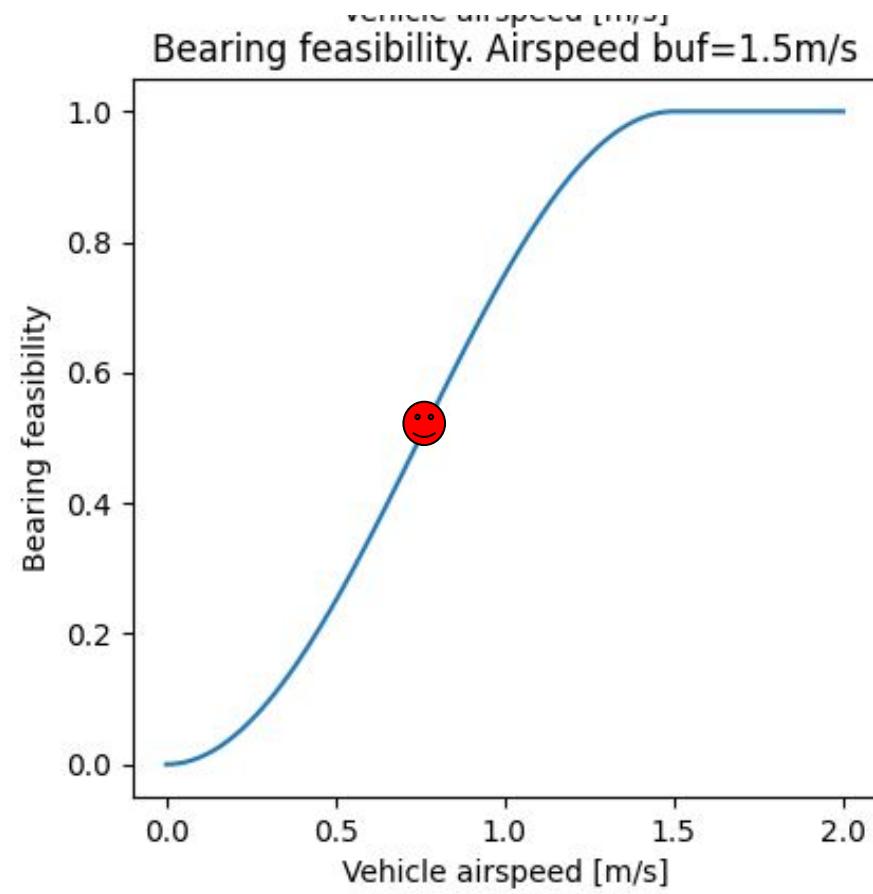
Minimum  
Ground Speed  
Track-Keeping



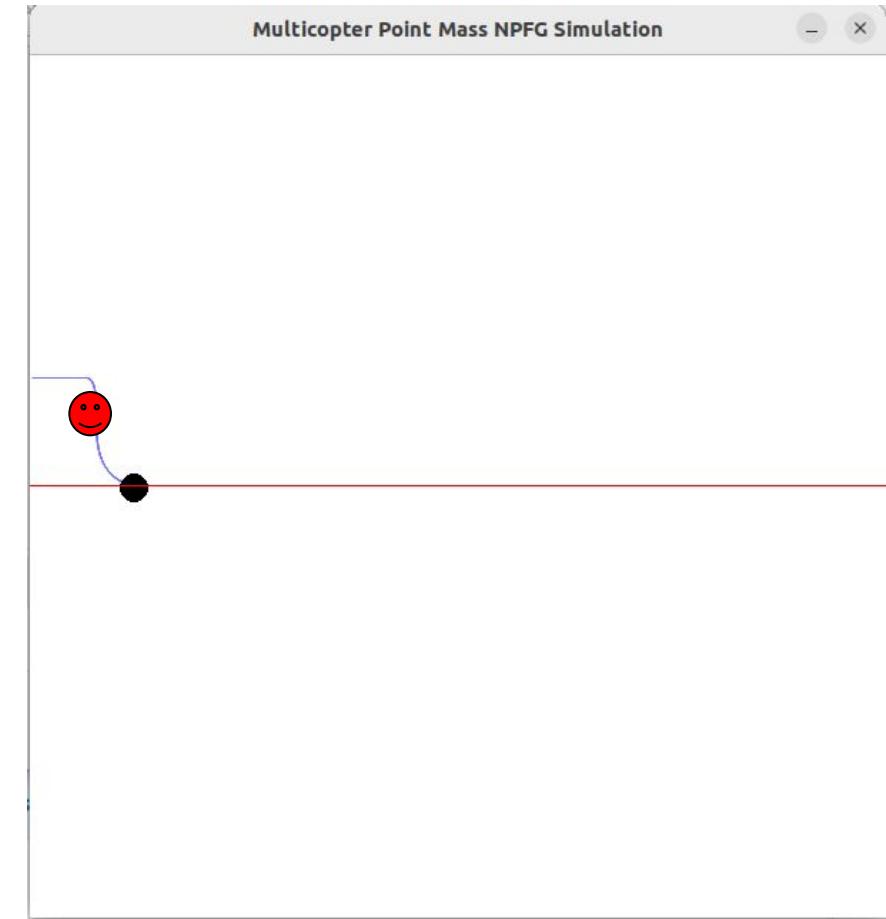
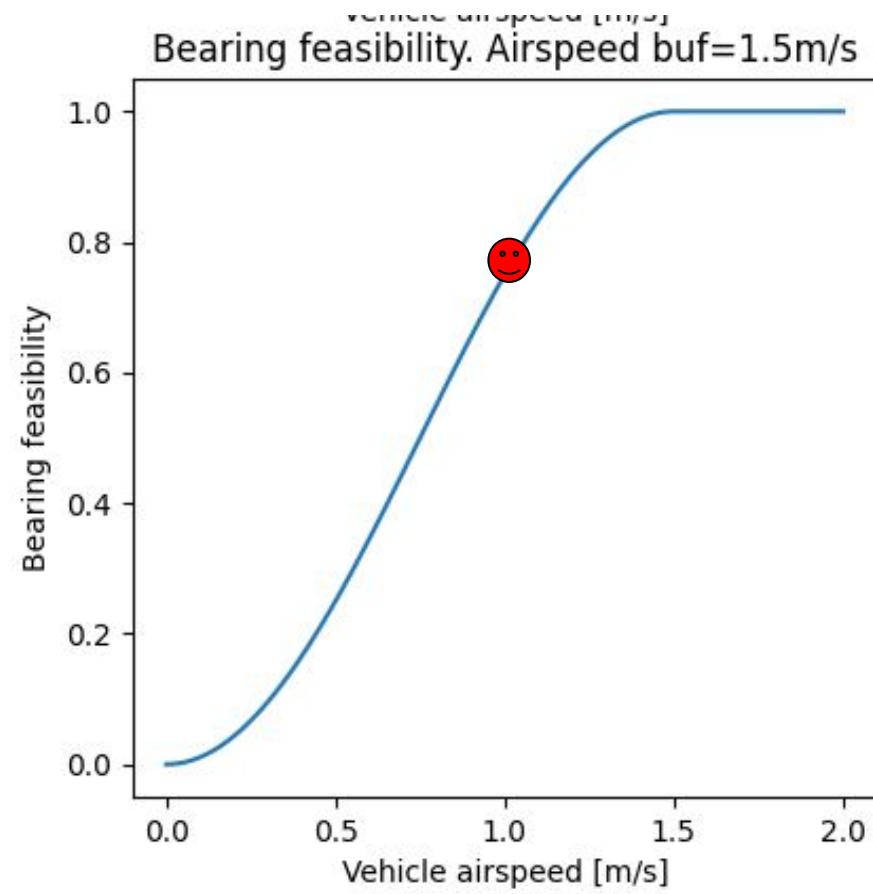
# Bearing Feasibility



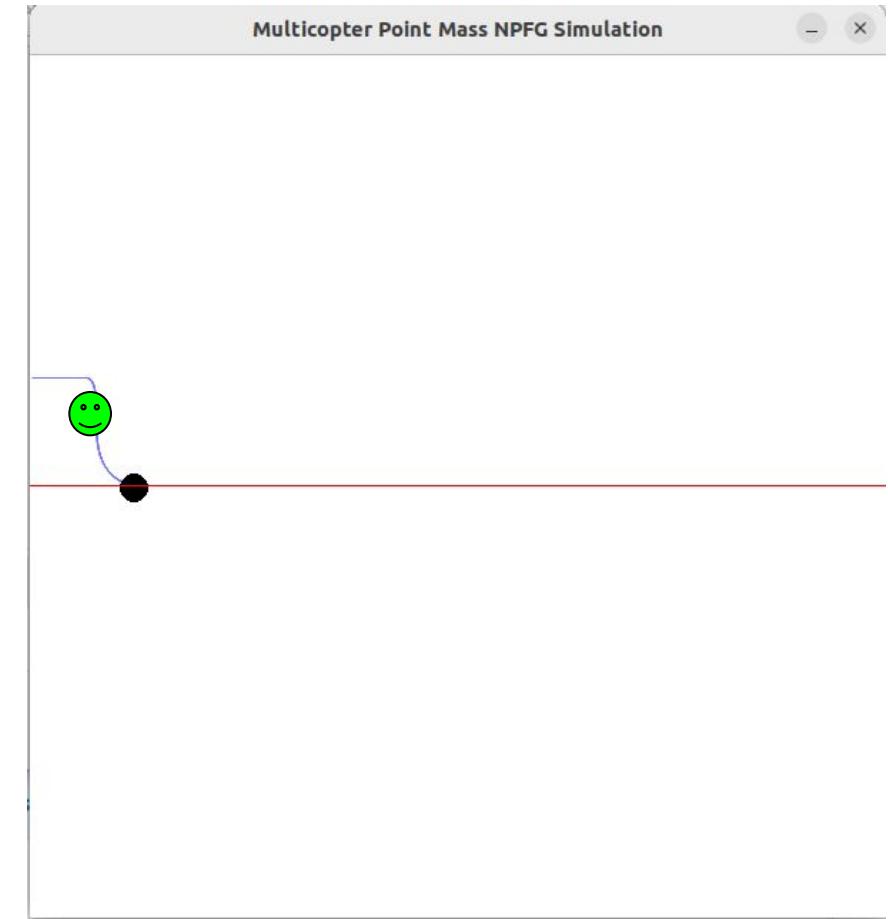
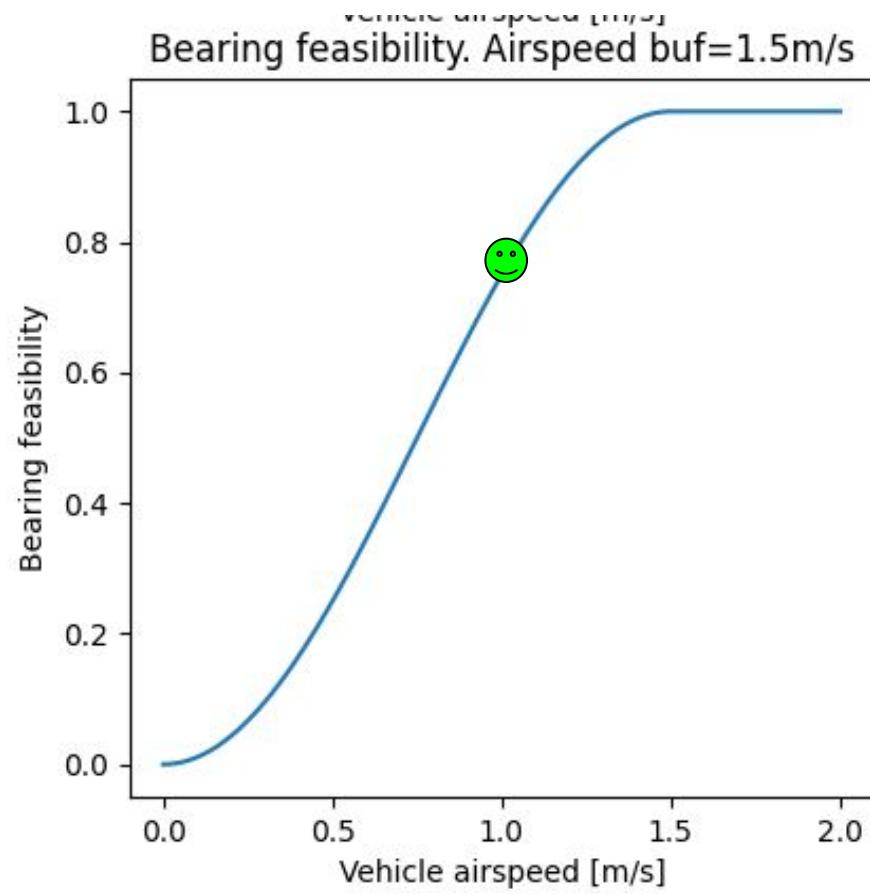
# Bearing Feasibility



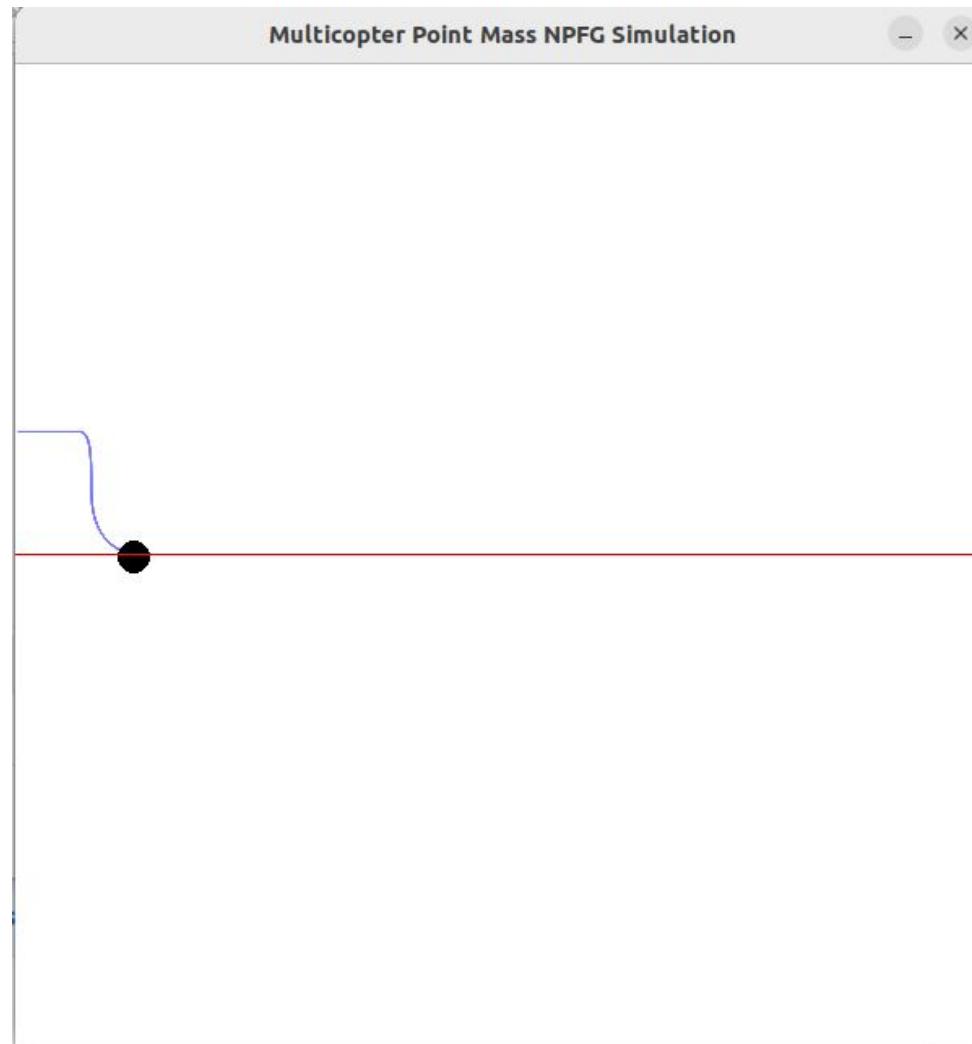
# Bearing Feasibility



# Bearing Feasibility



# Multicopter vs Fixed-wing dynamics



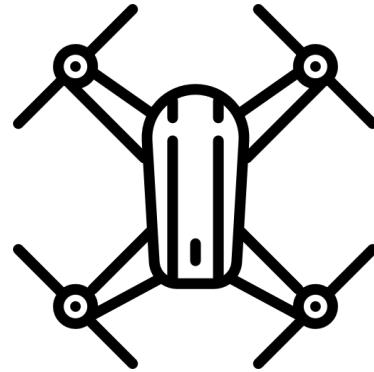
# Appendix

Slides that I won't be using





# Constraints of Multirotor and Fixed Wing System

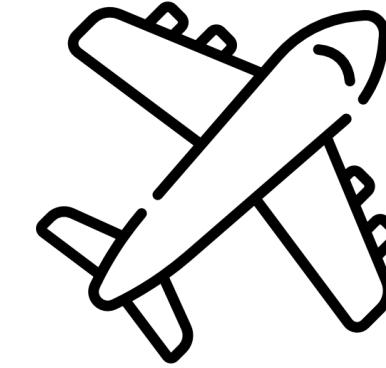


## Acceleration (Body Frame)

- Lateral
- Longitudinal

## Velocity

- Variable



## Acceleration

- Lateral (Yaw coupled)
- Longitudinal

## Velocity

- Constant

# Methods

## Look ahead angle

### Unicyclic

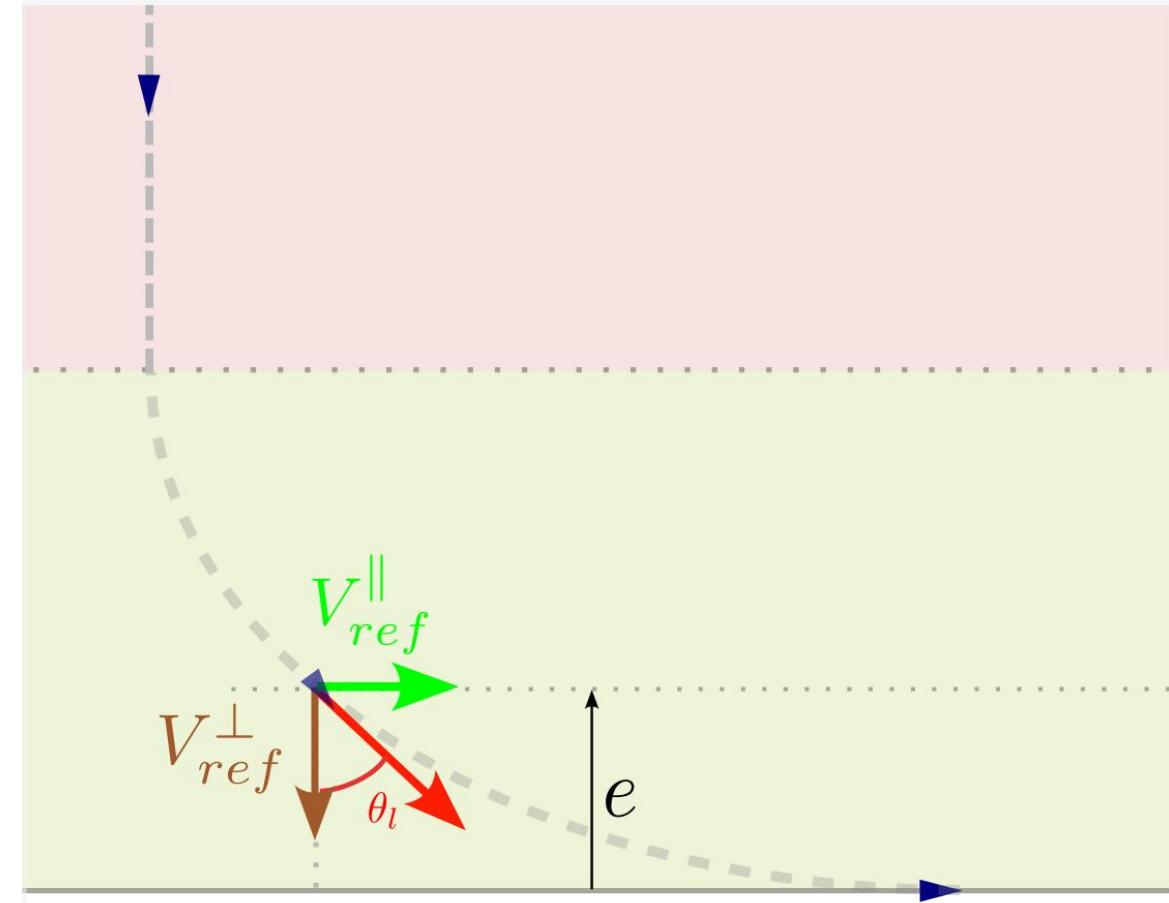
$$V_g^{\parallel} = V_{nom} * \sin(\theta_l)$$

$$V_g^{\perp} = V_{nom} * \cos(\theta_l)$$

### Hybrid Unicyclic

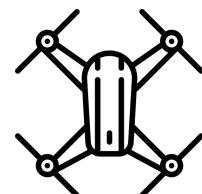
$$V_g^{\parallel} = V_{path} * \sin(\theta_l)$$

$$V_g^{\perp} = V_{approach} * \cos(\theta_l)$$

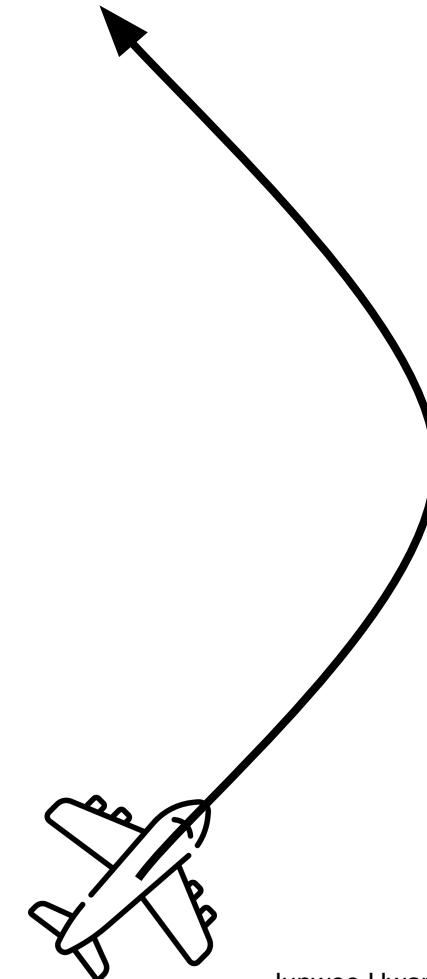


# Path Following for Multirotor / Fixed Wing

Holonomic

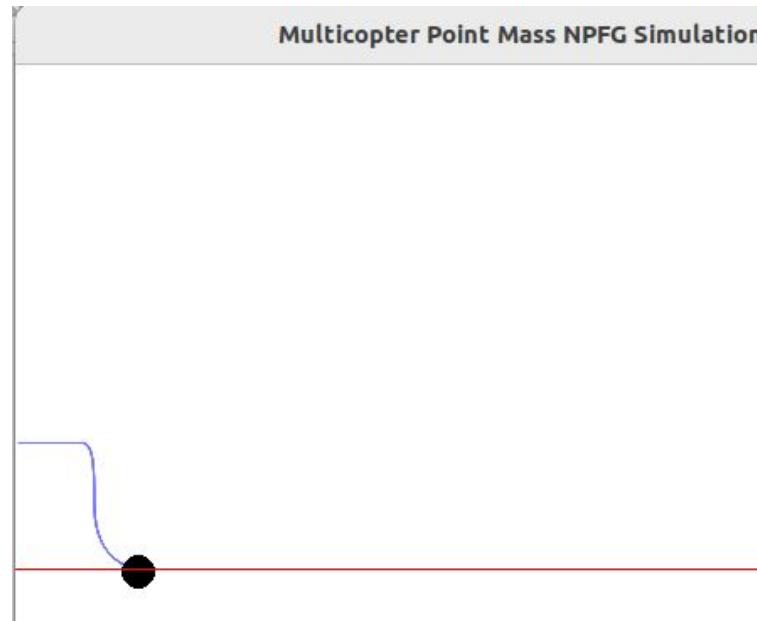


Non Holonomic



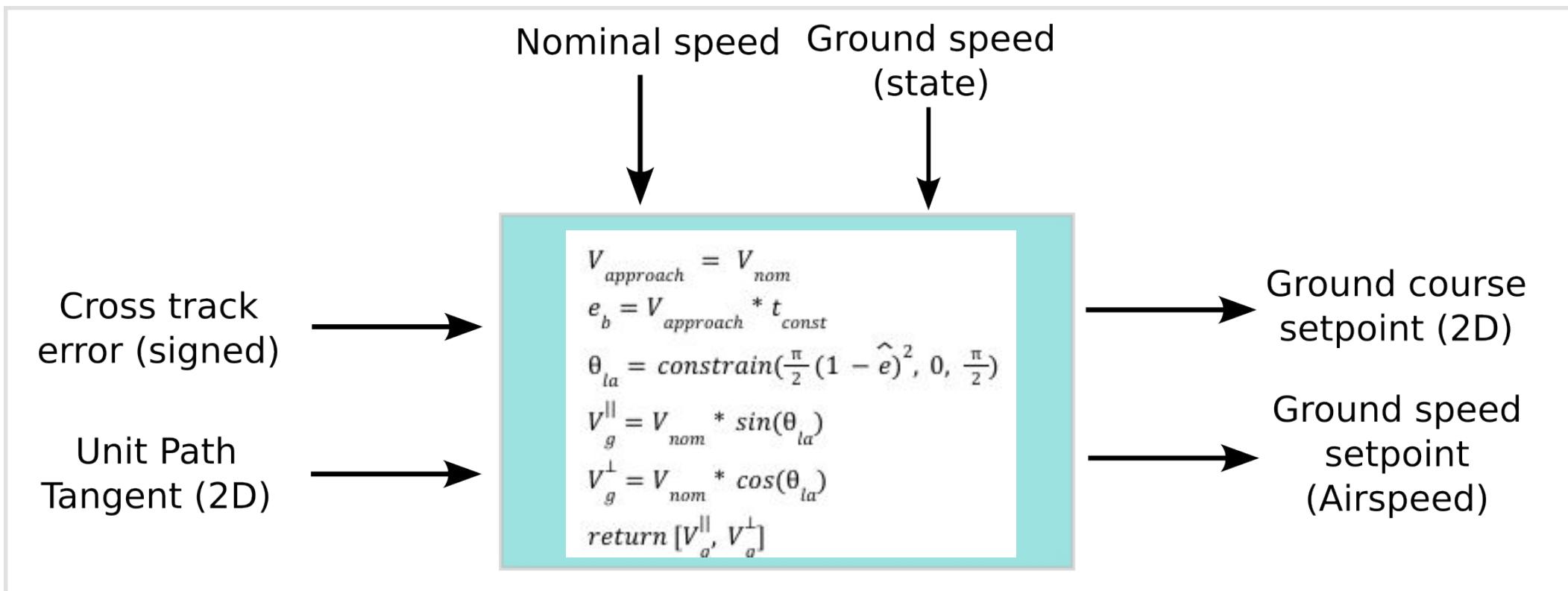
# Why do we need Unified Path Following?

- Fixed Wing Path Following doesn't work on Multirotor!



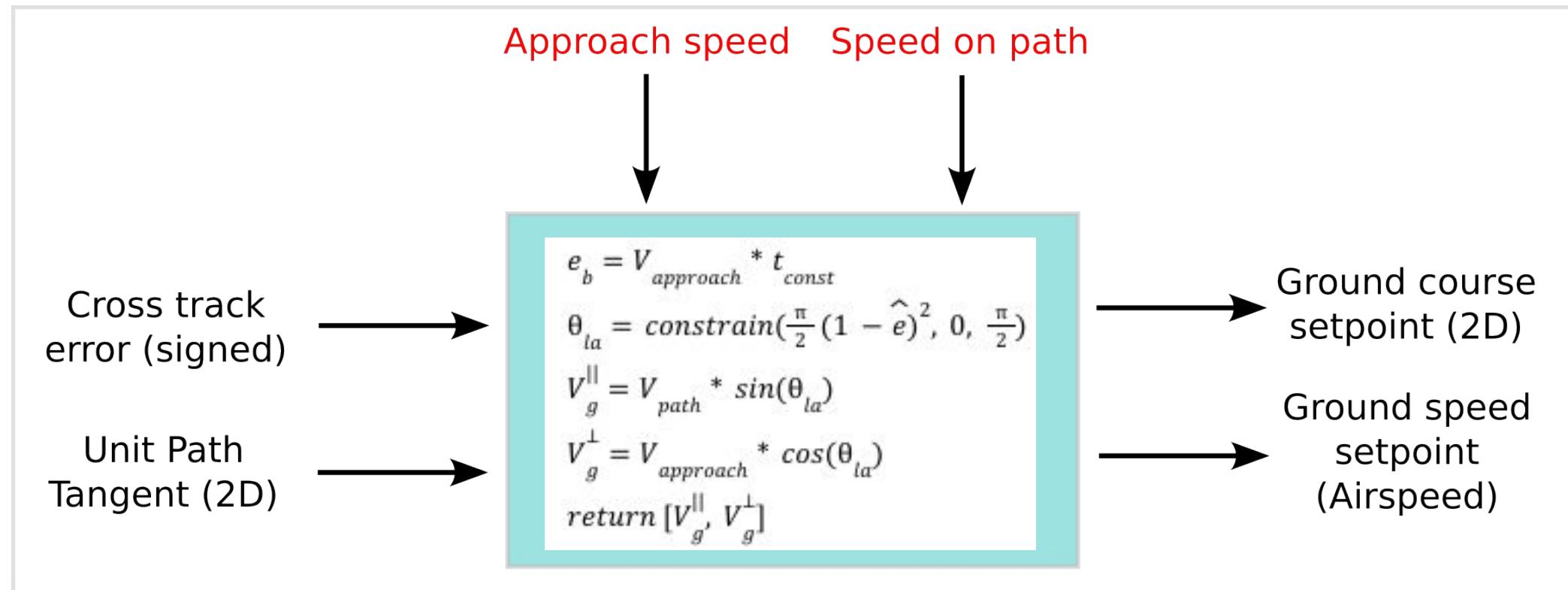
# Base Method

## Unicyclic Method [Stastny, IROS, 2019]



# Proposed Method

## Hybrid Unicyclic Method



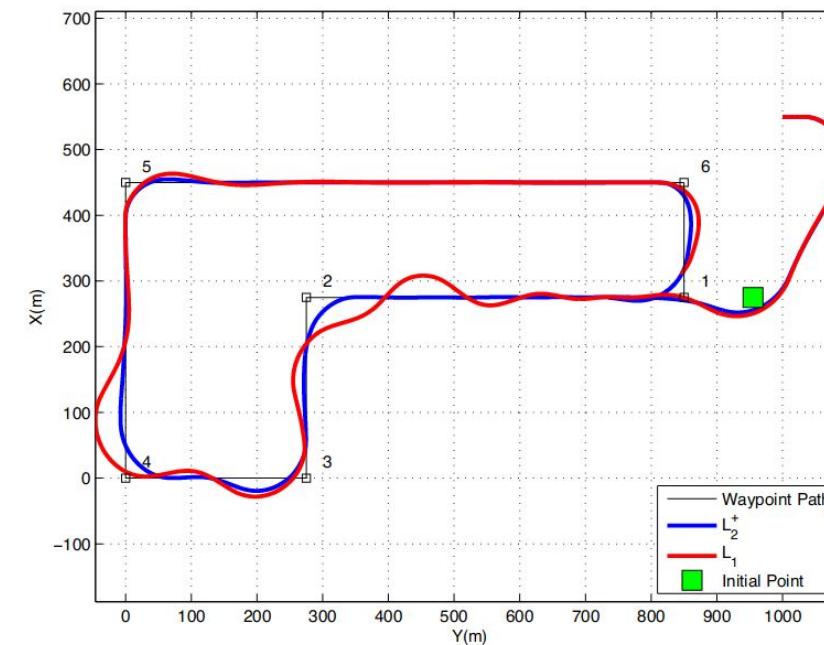
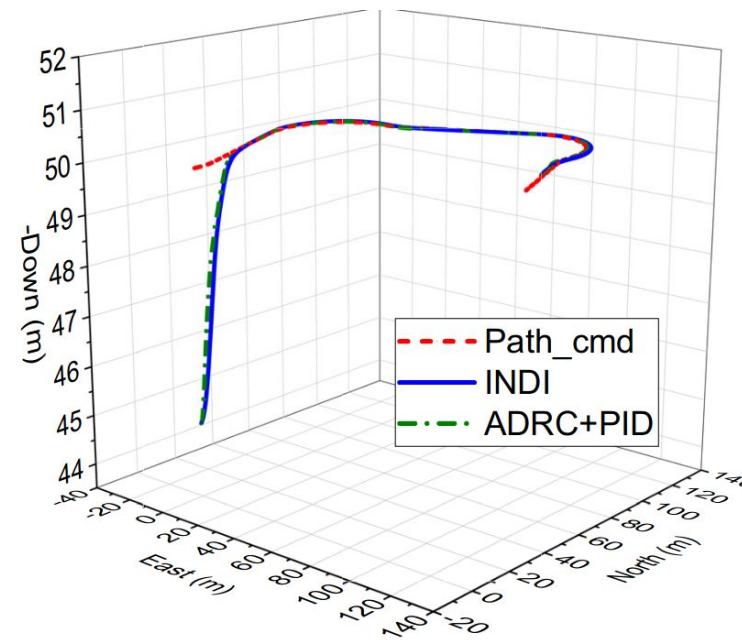
# Test Conditions

For evaluating the Ground Velocity curve:

- **No wind**
- **Track error boundary is fixed** (Only look-ahead angle & speed is varied)
- **Approach speed is fixed** (To allow consistent entry for comparison)
- Vehicle tracks ground velocity perfectly (first order system)

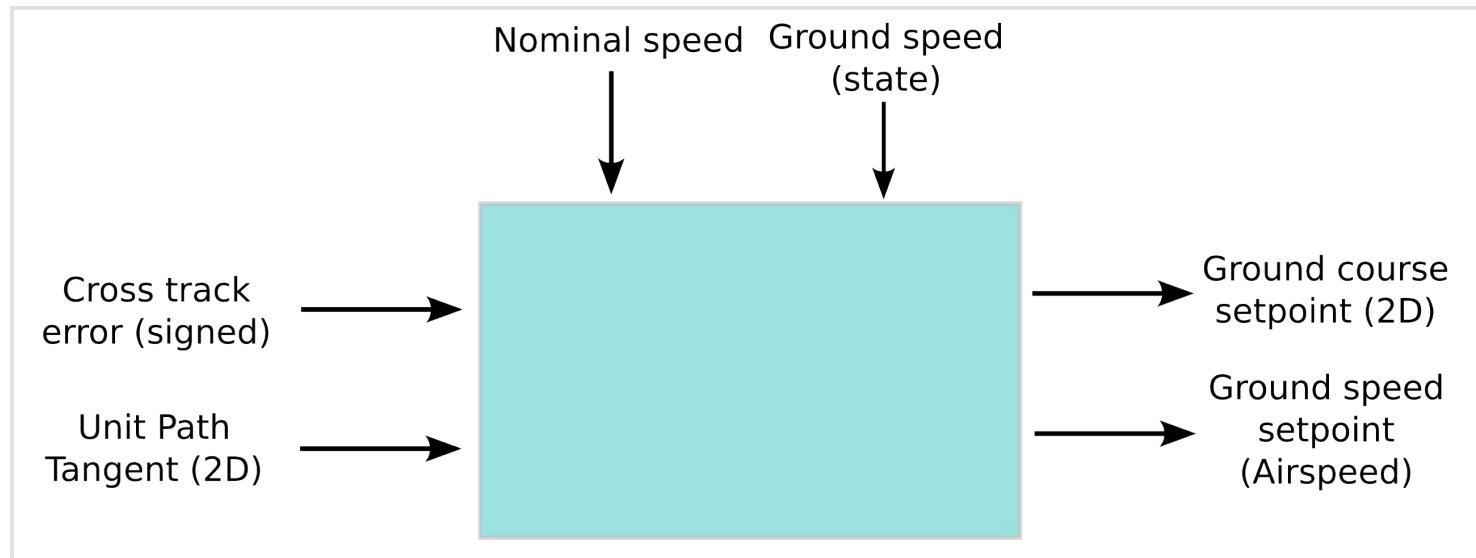
# Limitations

- Constant speed assumption for Multirotor (Limited maneuverability)
- No generic Path Following Guidance that suits both modes of operation

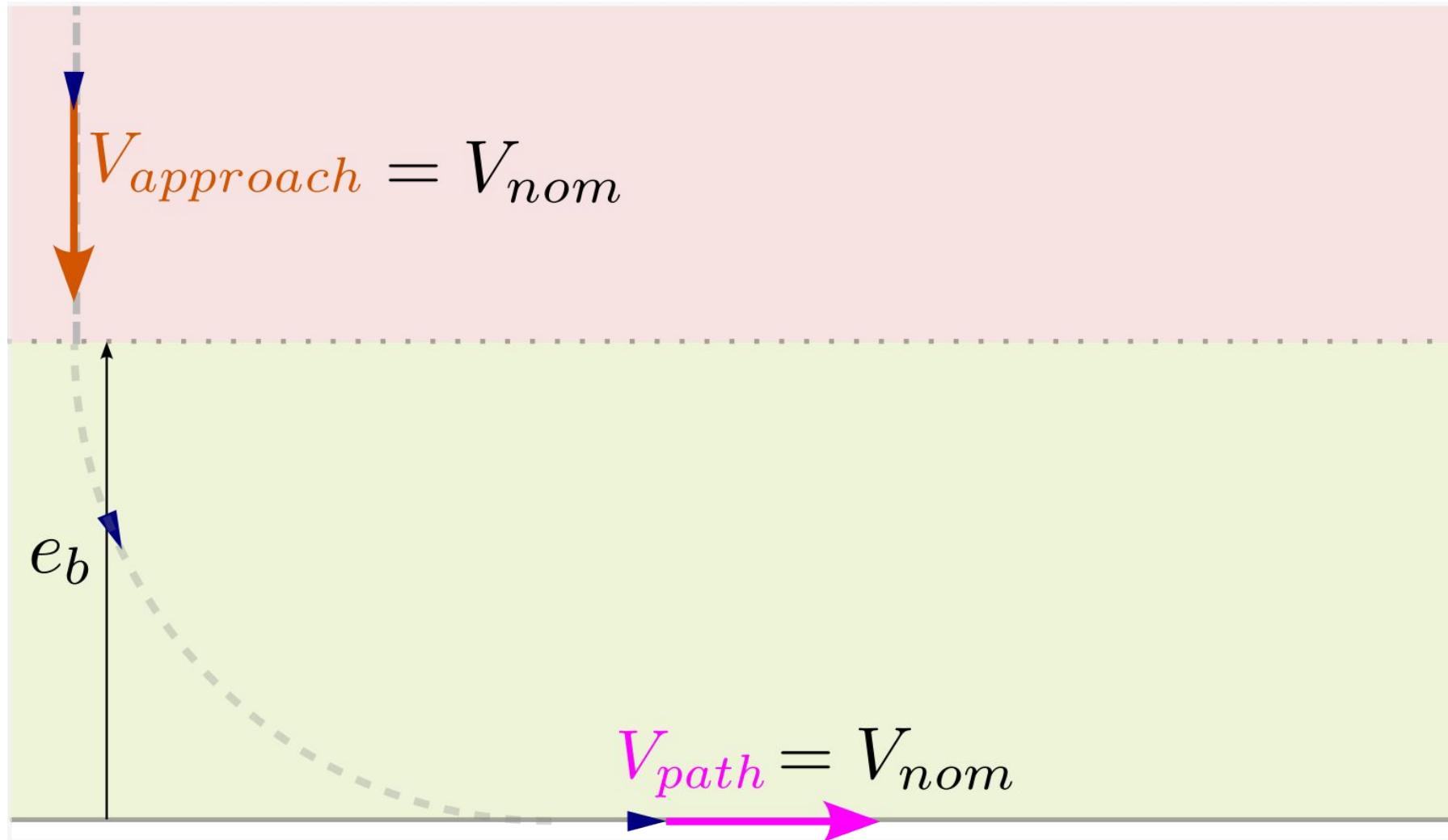


# Base Method

## Unicyclic Method [Stastny, IROS, 2019]

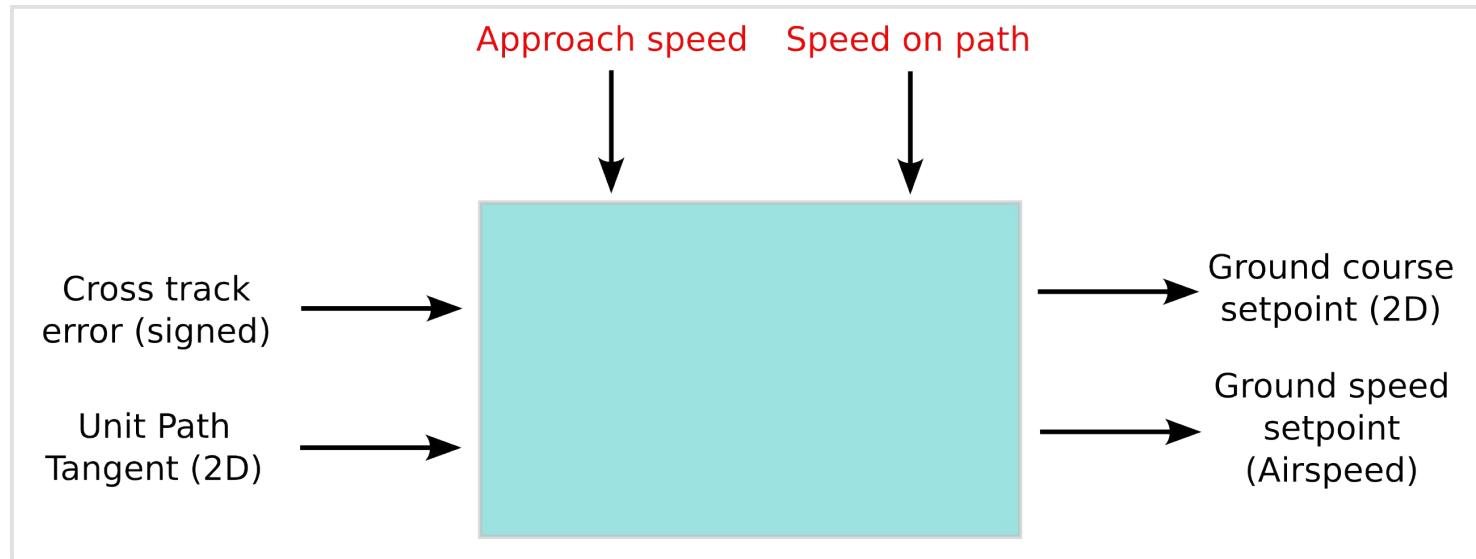


# Base Method

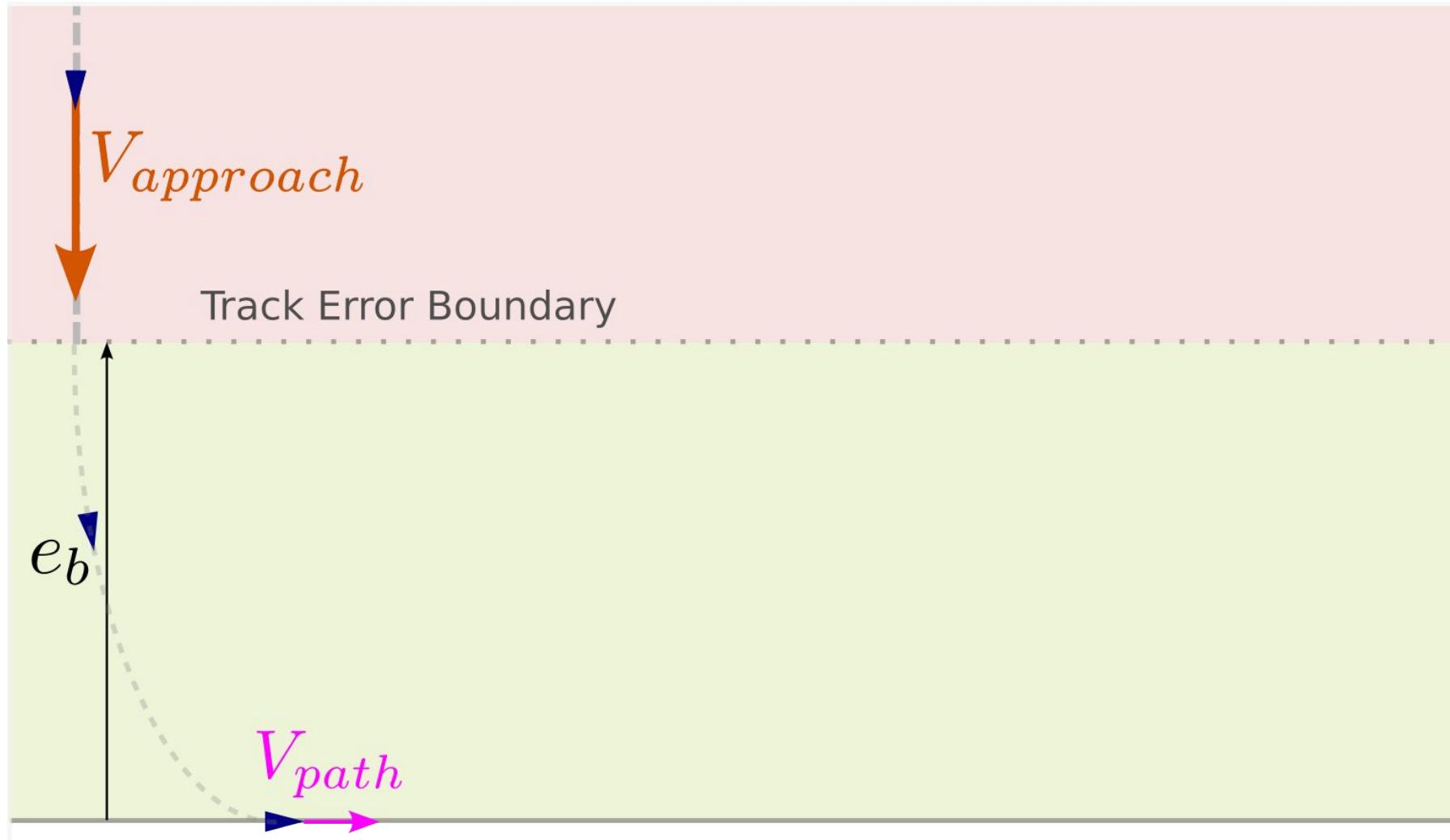


# Proposed Method

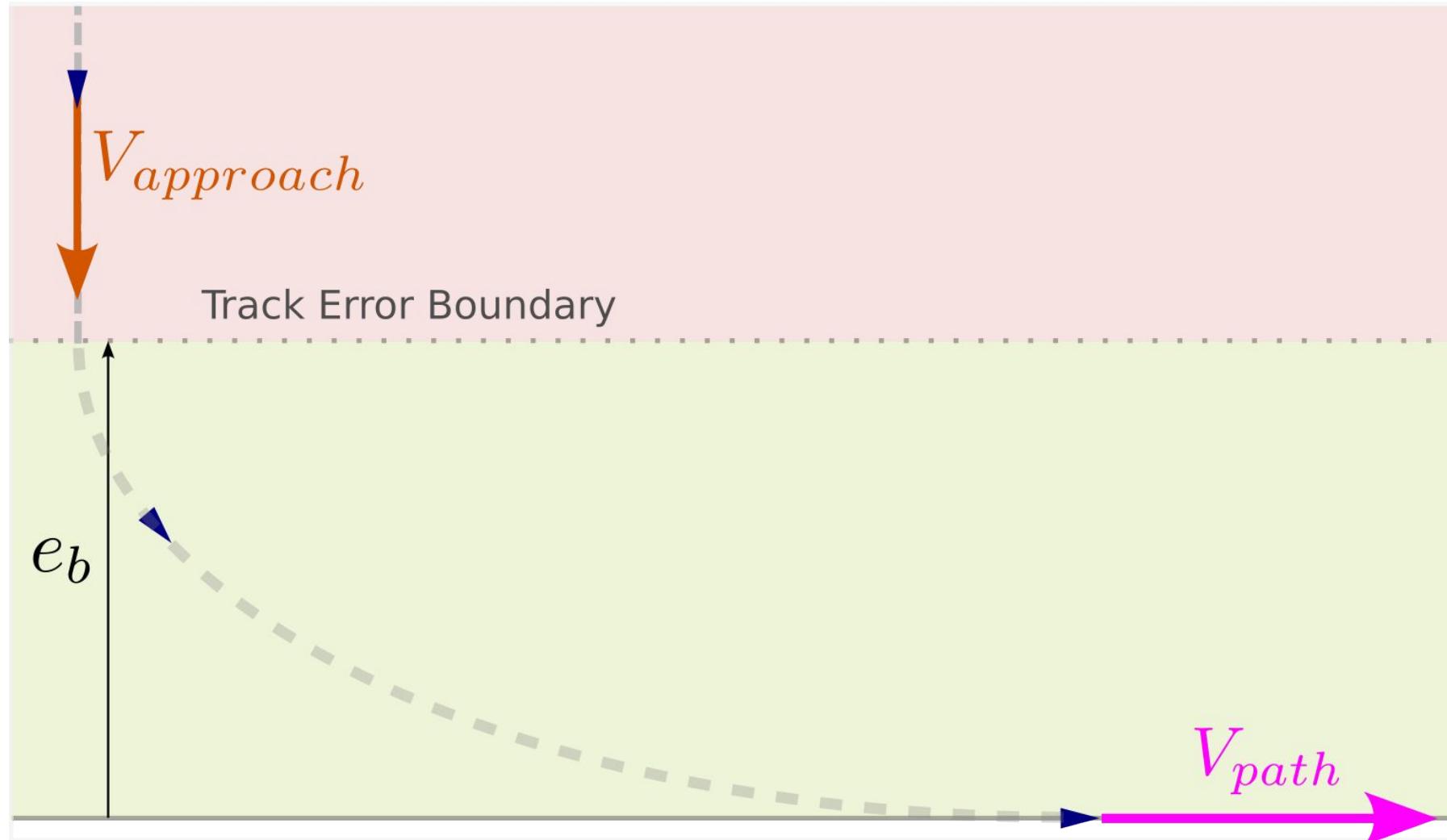
## Hybrid Unicyclic Method



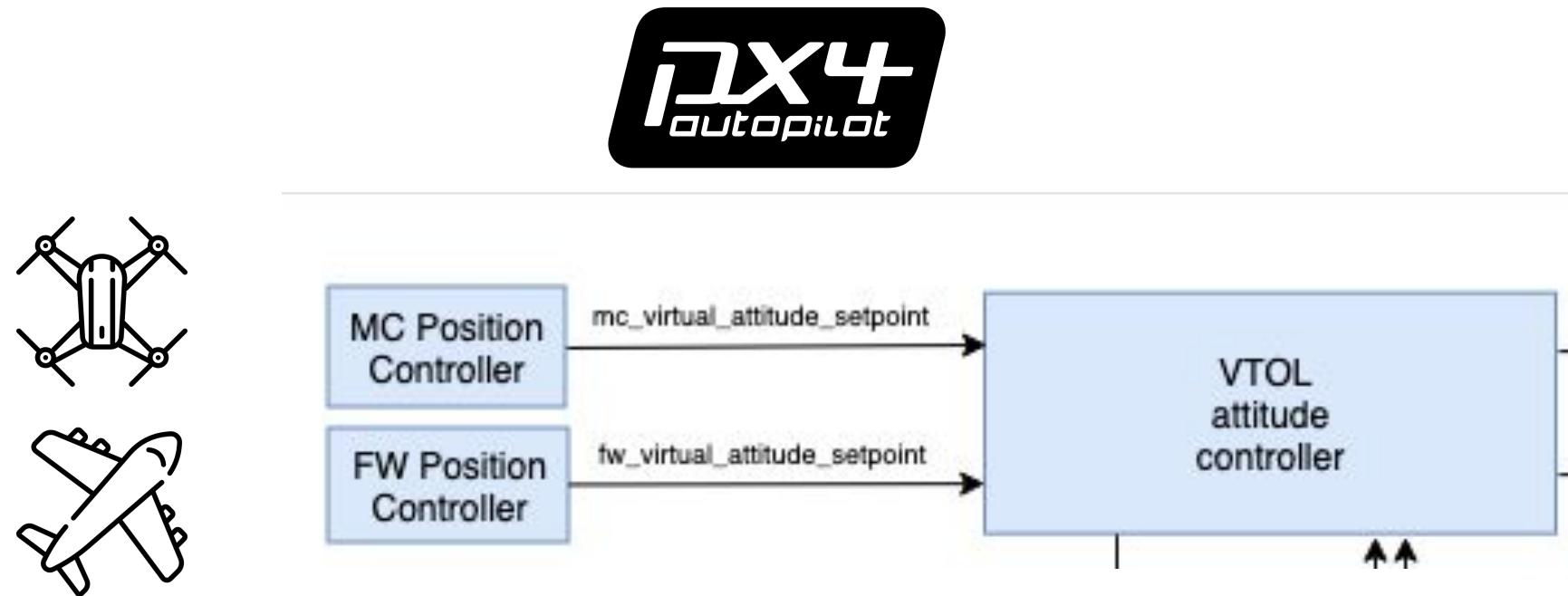
# Proposed Method: Low speed on Path (Aggressive turning)



# Proposed Method: High speed on Path (Smoother turning)



# Path Following for VTOL: Current Status



**Decoupled** between MC / FW

# What is Path Following?

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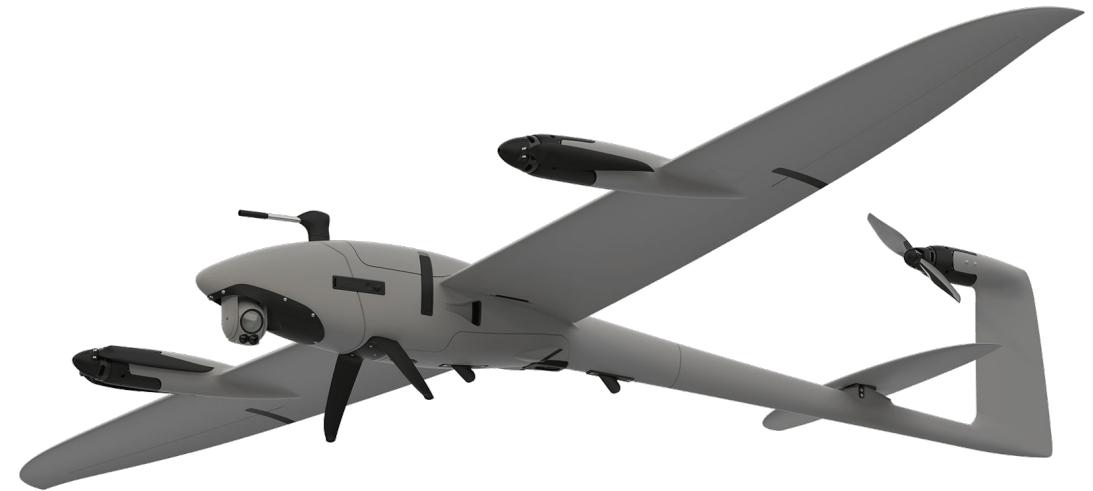
who cares lol



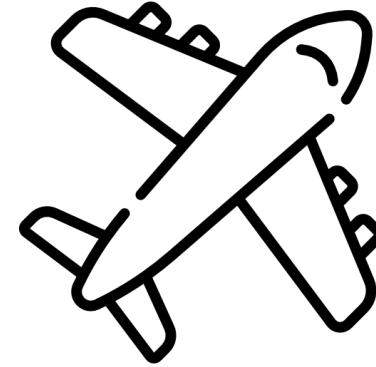
# What is a Hybrid VTOL?



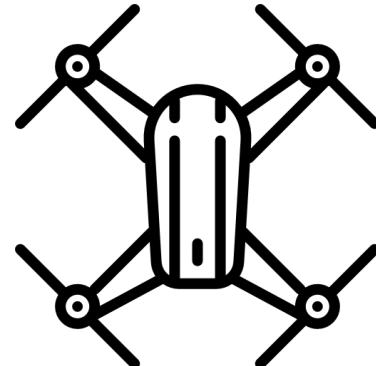
# Modes of operation of Hybrid VTOL



# Modes of operation of Hybrid VTOL



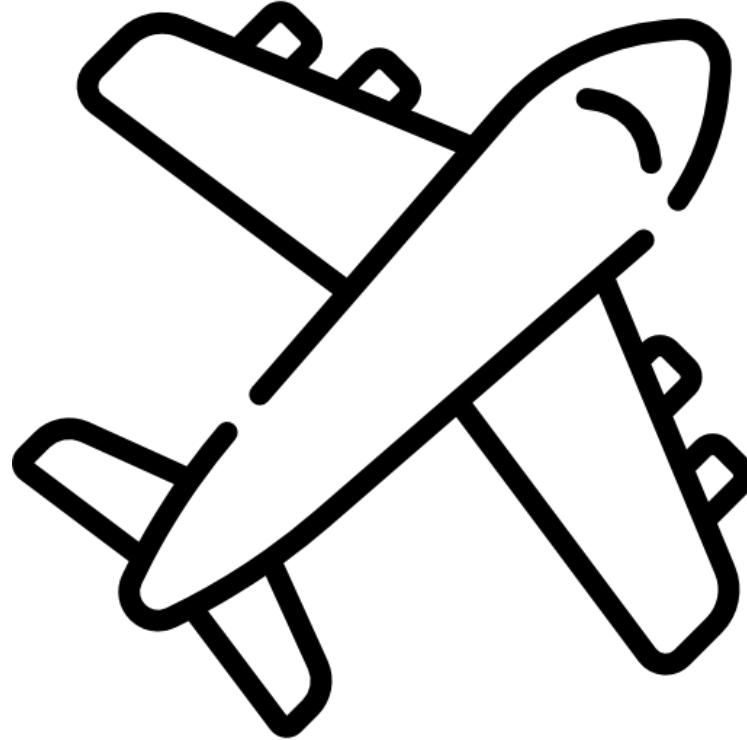
**Fixed Wing**



**Multirotor**



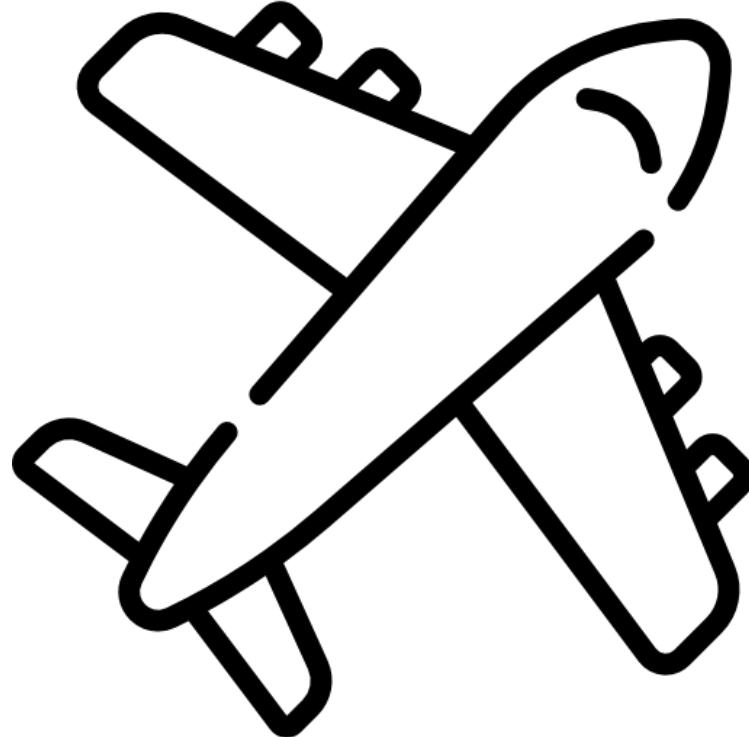
# Modes of operation of Hybrid VTOL



Fixed Wing



# Modes of operation of Hybrid VTOL



Fixed Wing

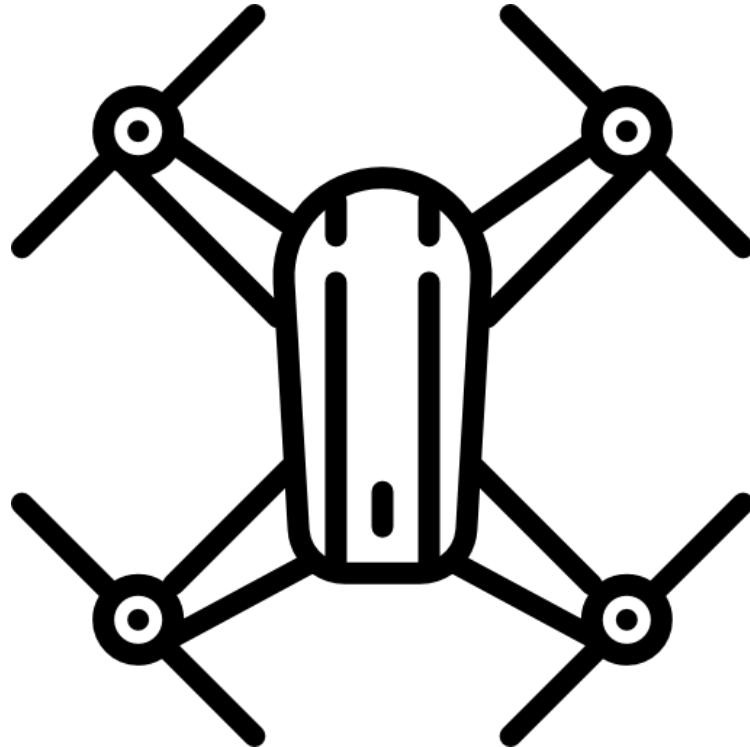
## Acceleration

- Lateral (Rolling): Coupled with yaw
- Longitudinal: (almost) None
- Vertical (Pitching): Flexible

## Velocity

- Airspeed: (almost) Constant

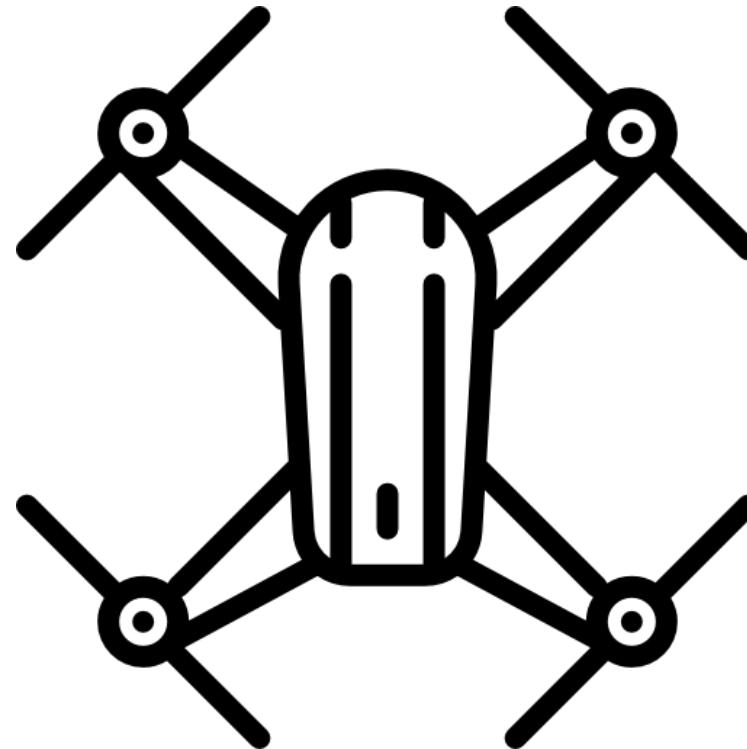
# Modes of operation of Hybrid VTOL



Multirotor



# Modes of operation of Hybrid VTOL



**Multirotor**

## Acceleration

- Lateral (Rolling): Full range
- Longitudinal (Pitching): Full range
- Vertical (Throttle): (almost) Full range

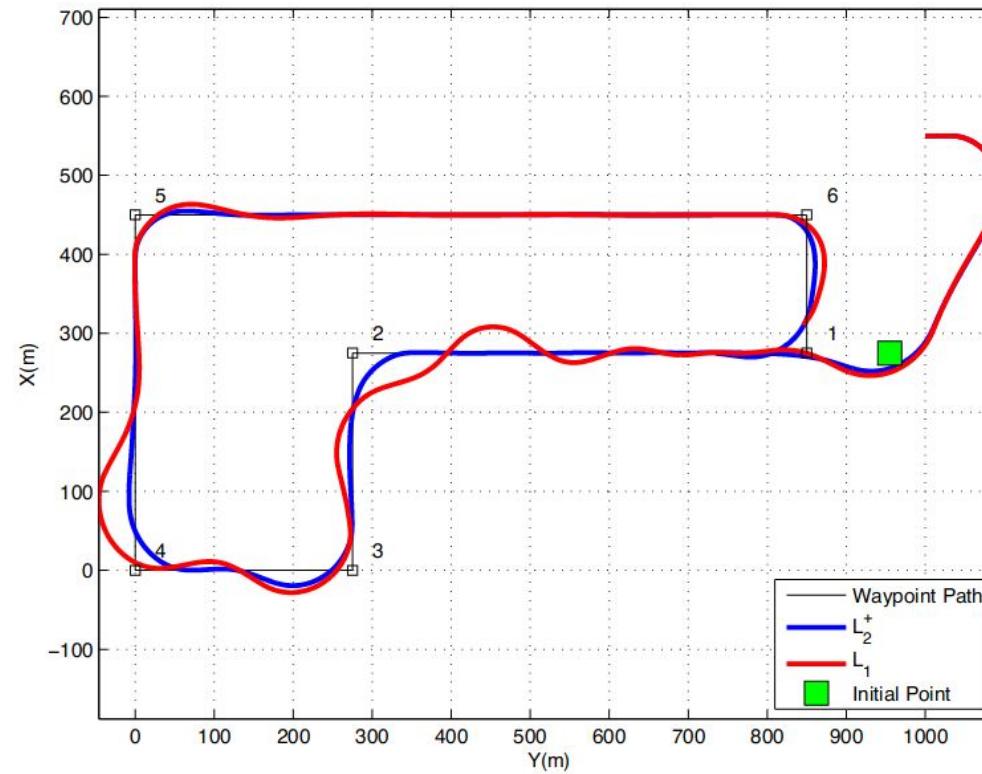
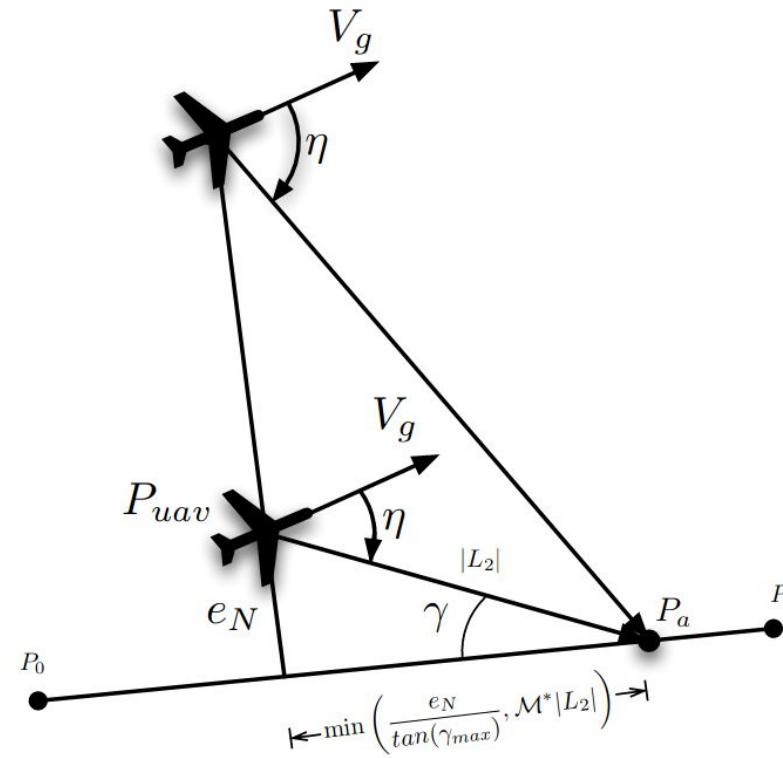
## Velocity

- Airspeed: Full range

# Related Work: Path Following on Fixed Wing

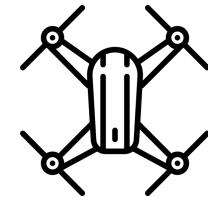


- Nonlinear Control [Stastny, IROS, 2019]
- Line of Sight Control [Curry, ACC, 2013]

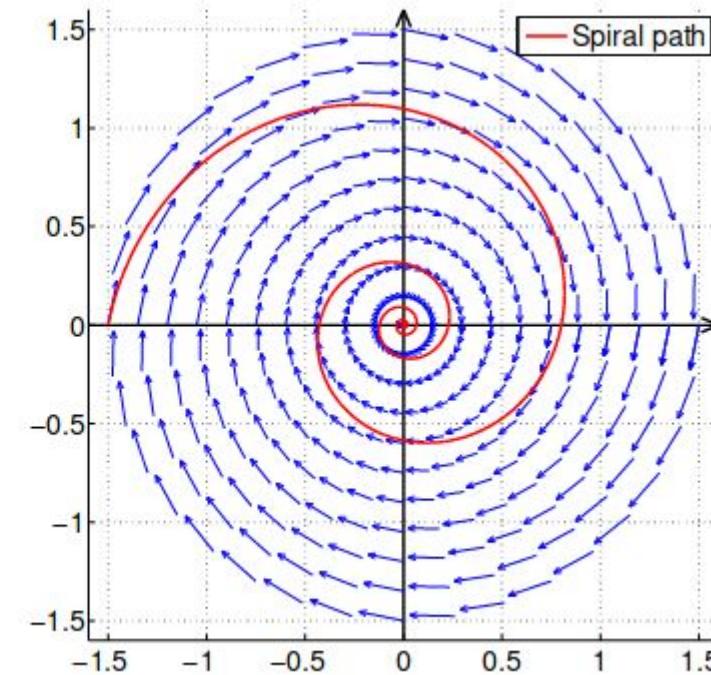
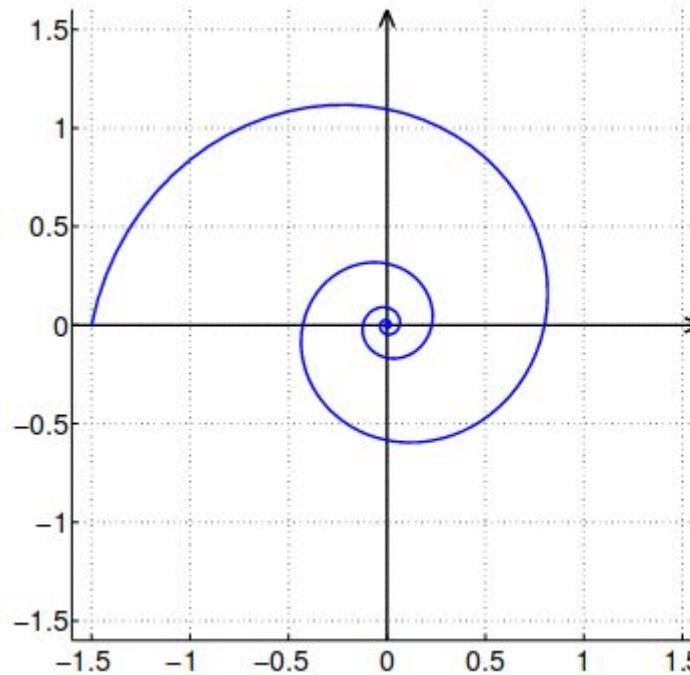


T. Stastny. "On Flying Backwards: Preventing Runaway of Small, Low-speed, Fixed-wing UAVs in Strong Winds". IROS, 2019  
 R. Curry. "L+2, an improved line of sight guidance law for UAVs". American Control Conference, 2013

# Related Work: Path Following on Multirotor



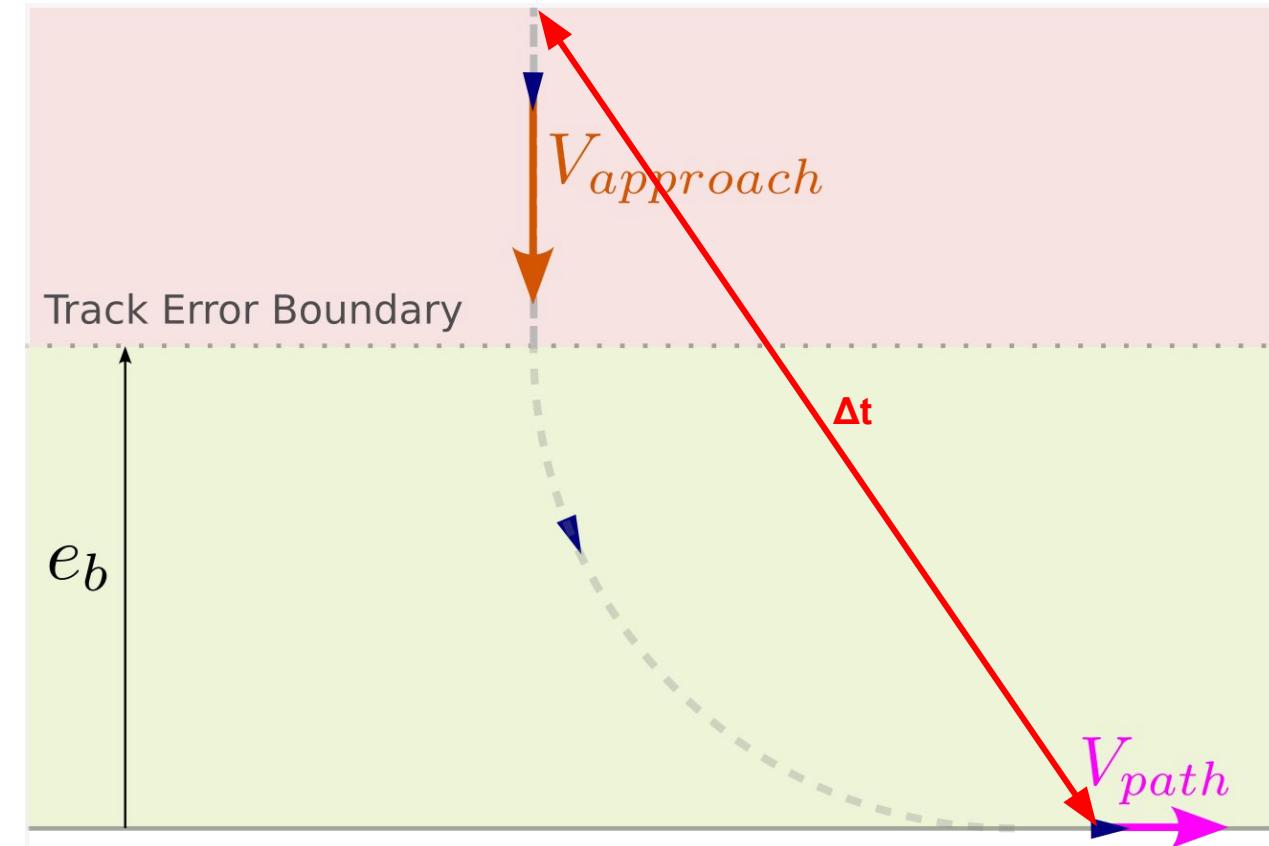
- Virtual Target Pursuit [Manjunath, 2016]
- Vector Field [Zhou, 2014]



Manjunath, A. R.. "Path following by a quadrotor using virtual target pursuit guidance." (2016).  
D. Zhou, "Vector field following for quadrotors using differential flatness," ICRA (2014)

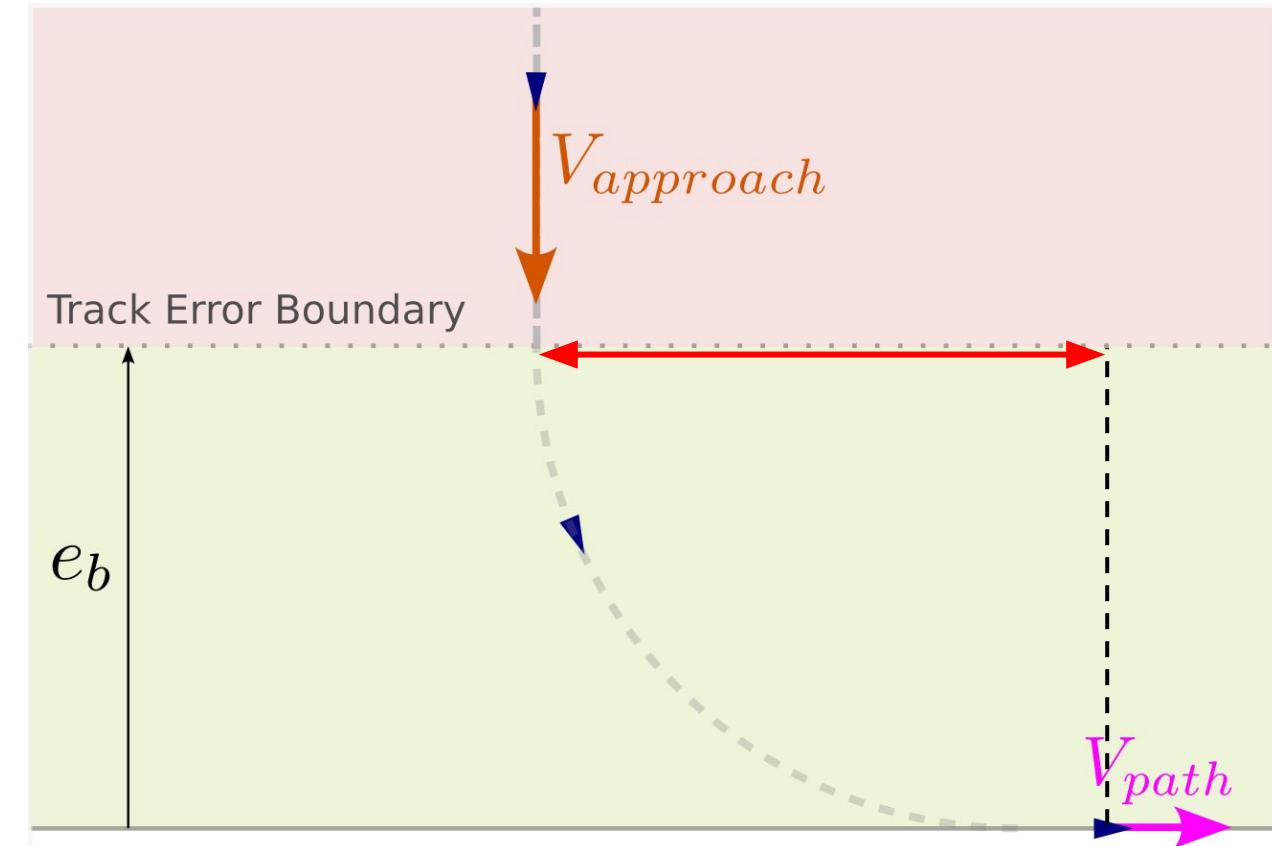
# Evaluation Criteria

- Time to Convergence



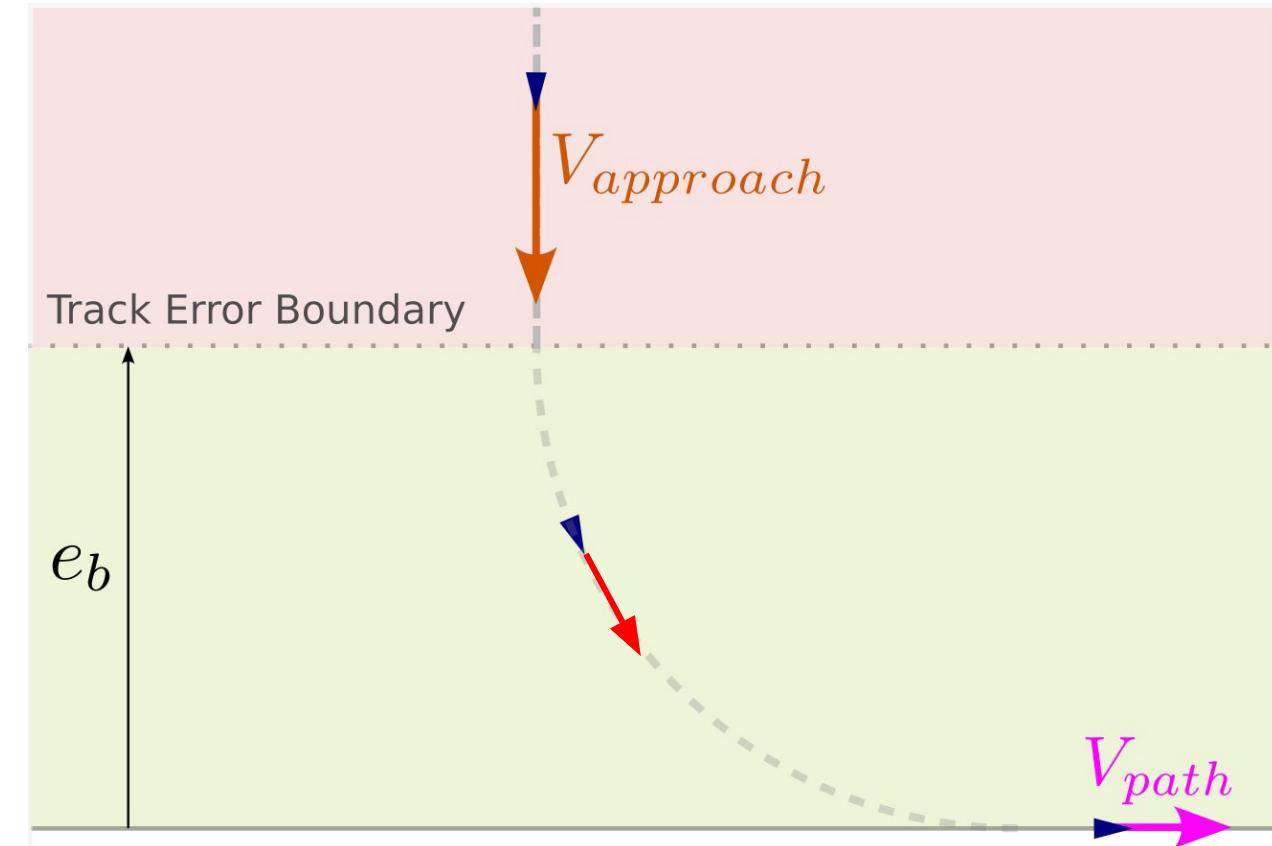
# Evaluation Criteria

- Time to Convergence
- Converging Path Parallel Distance



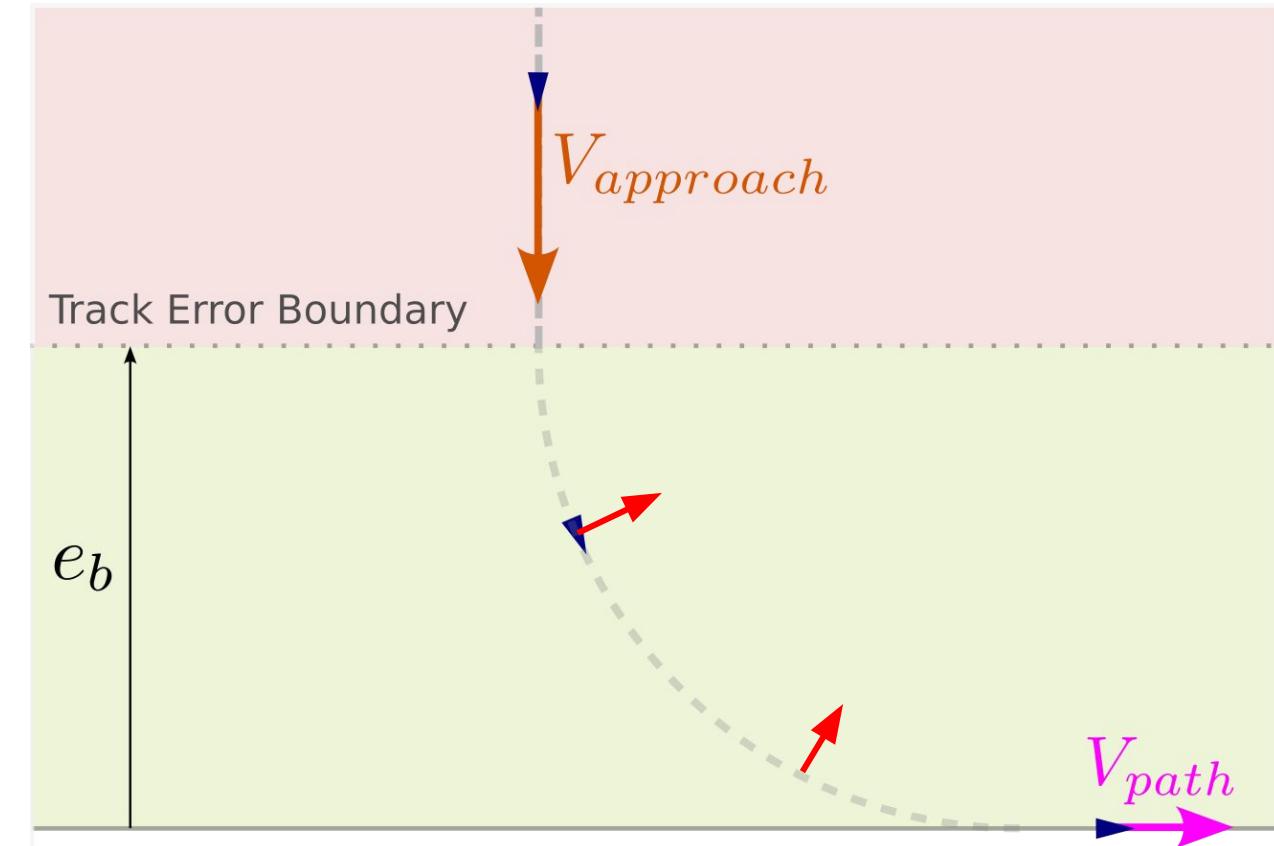
# Evaluation Criteria

- Time to Convergence
- Converging Path Parallel Distance
- Monotonicity of Ground Speed

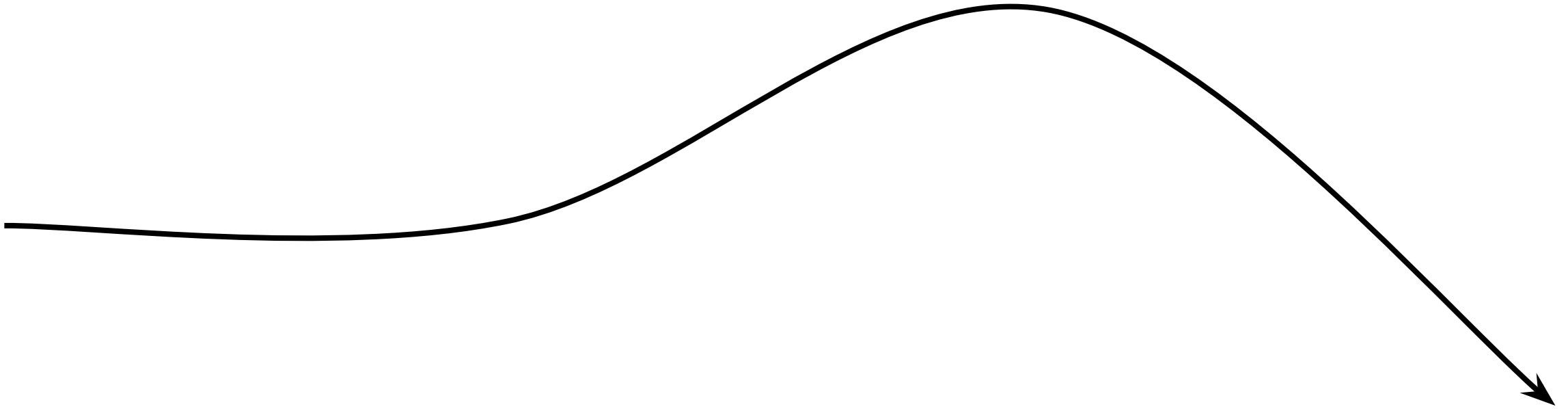
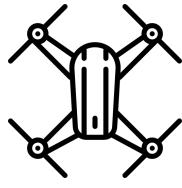


# Evaluation Criteria

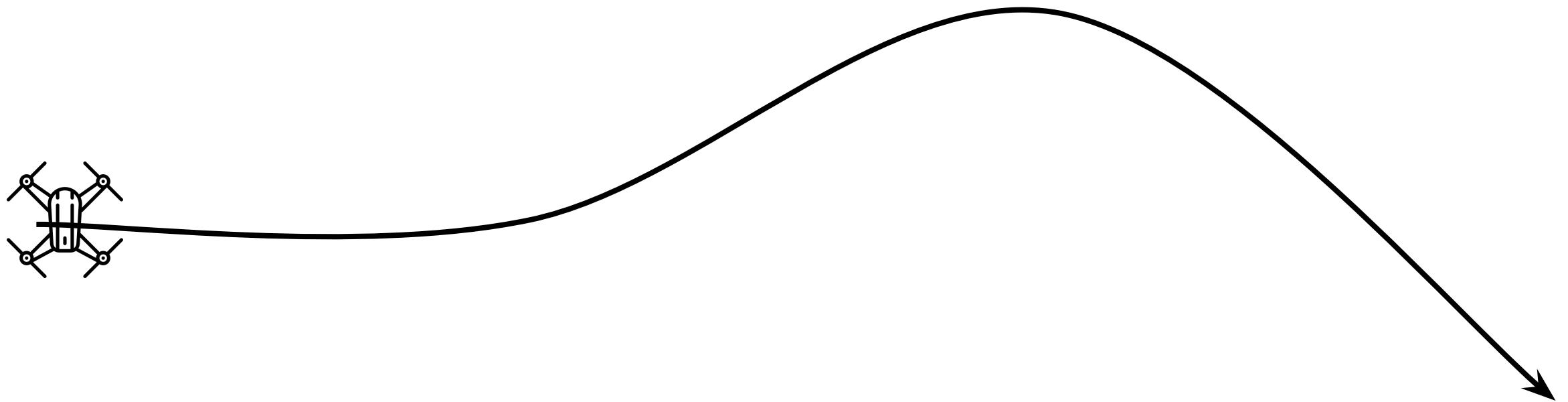
- Time to Convergence
- Converging Path Parallel Travel
- Monotonicity of Ground Speed
- Total Acceleration RMS



# What is Path Following?



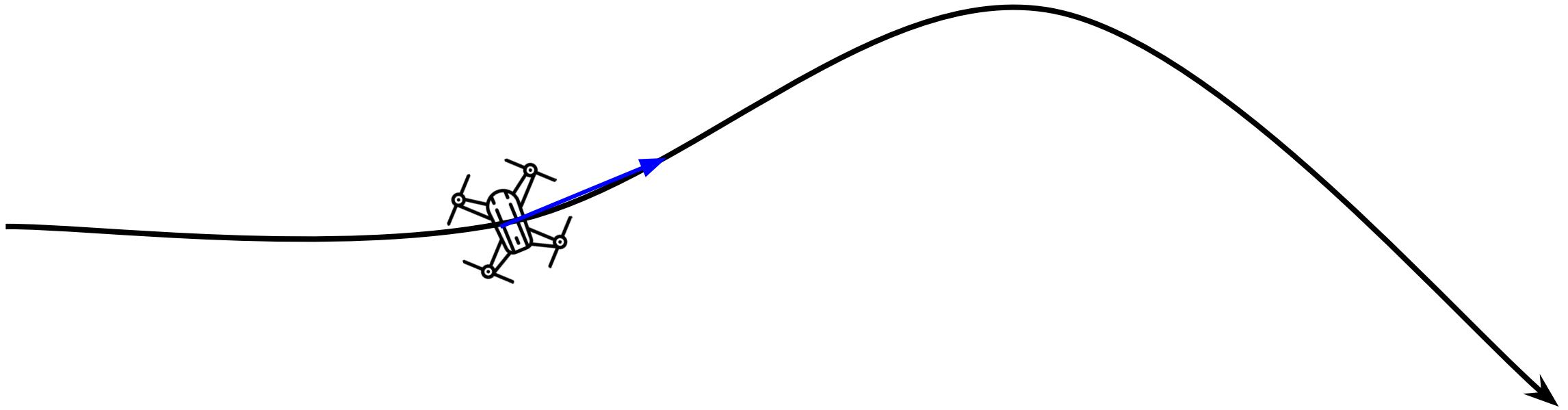
# What is Path Following?



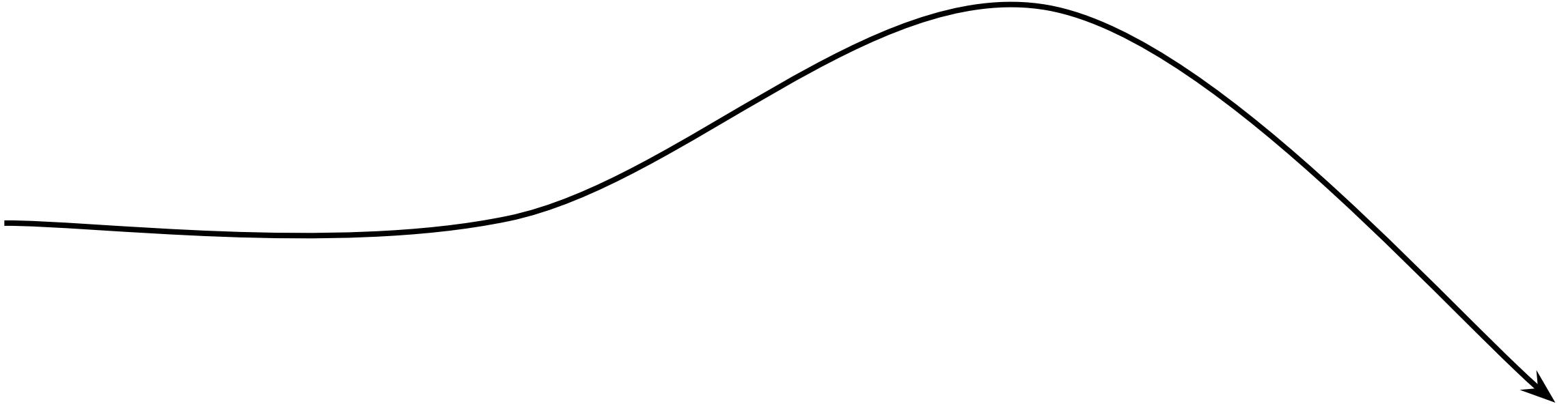
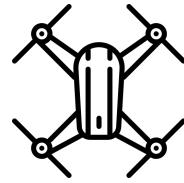
# What is Path Following?



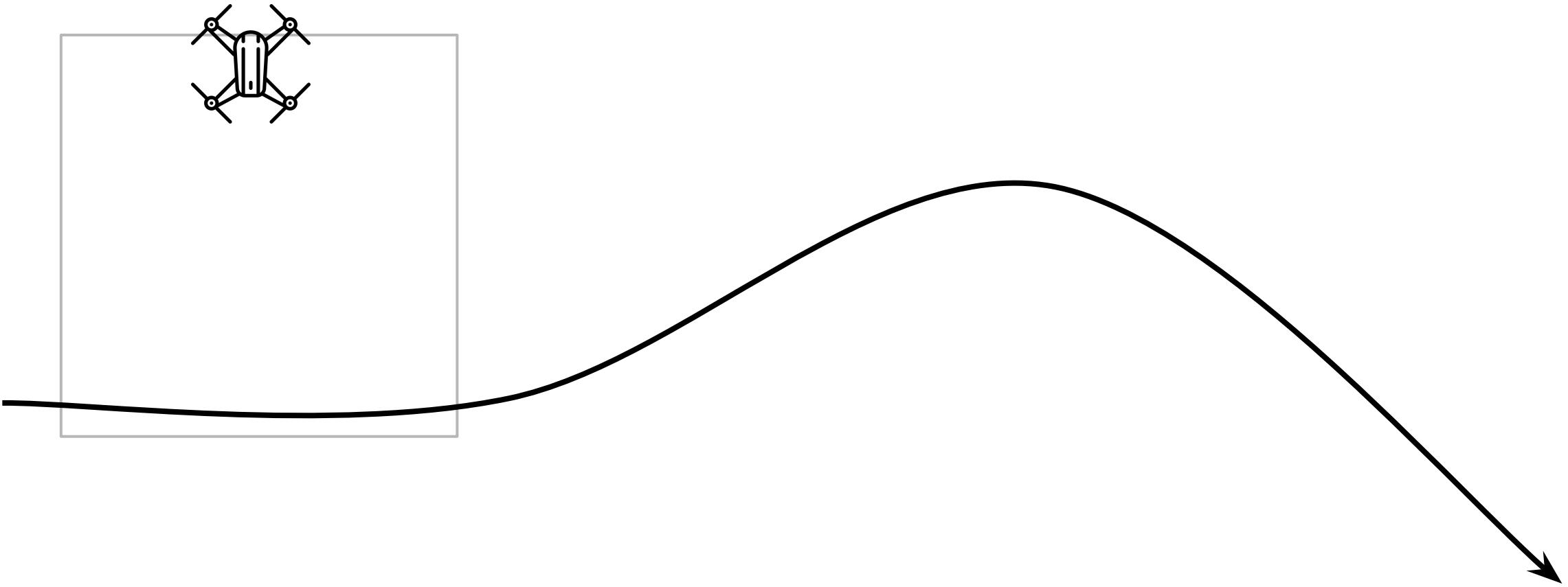
# What is Path Following?



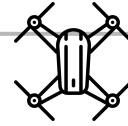
# Problem Definition: Revisited



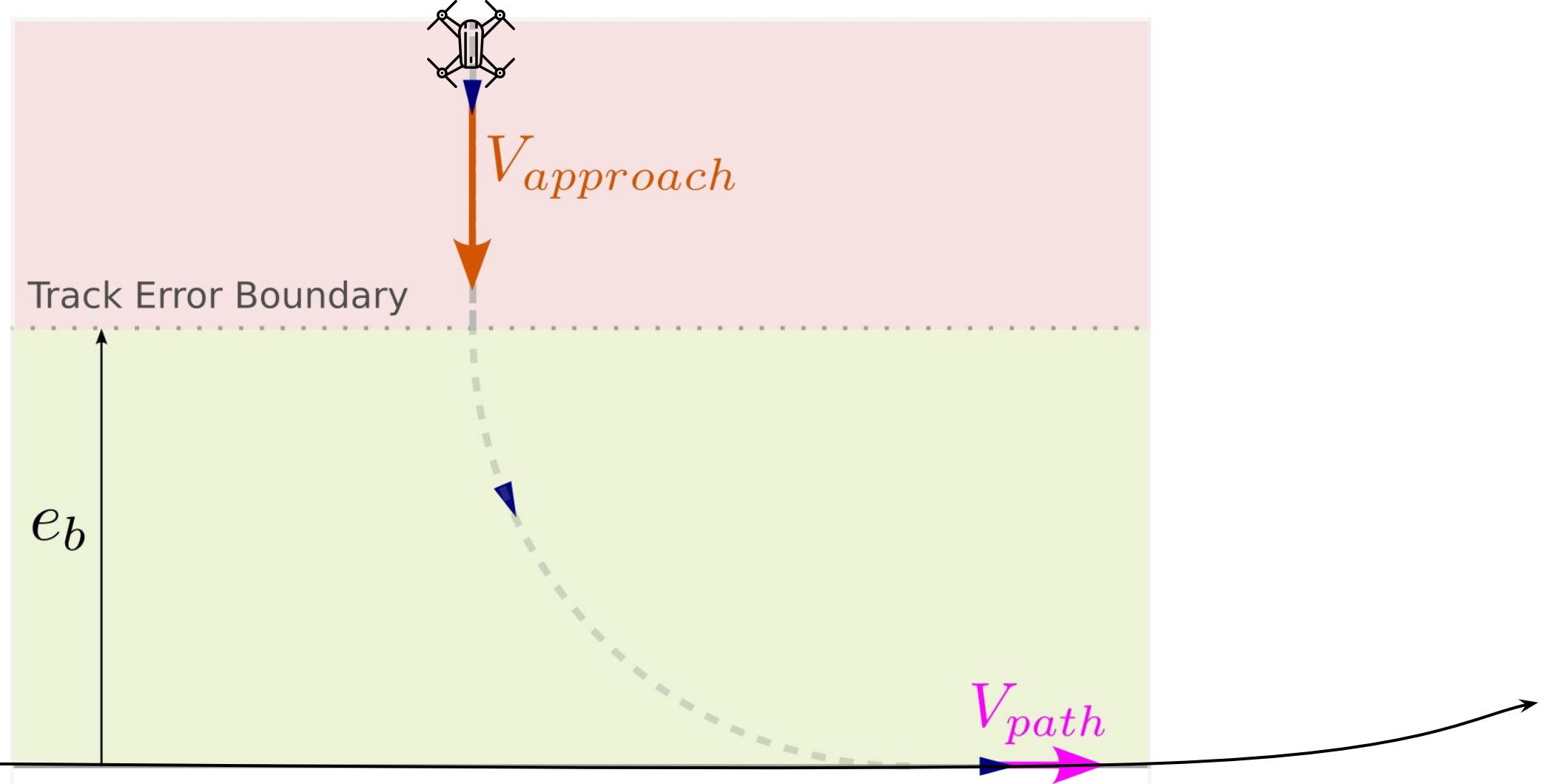
# Problem Definition: Revisited



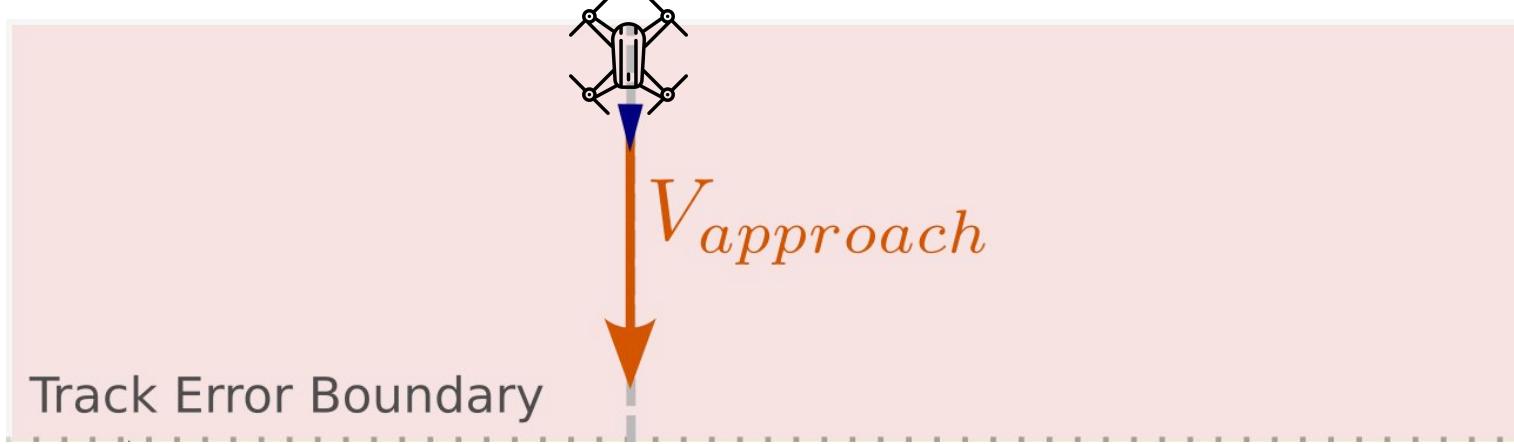
# Problem Definition: Revisited



# Problem Definition: 3 Phase breakdown



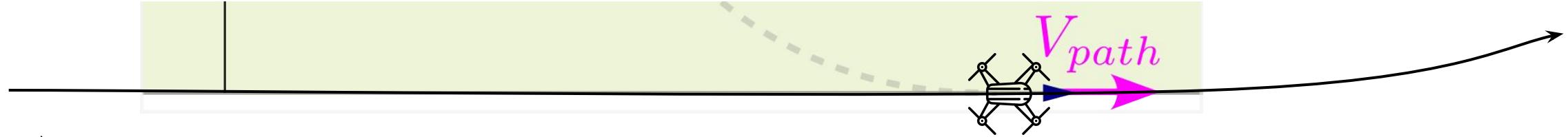
# Problem Definition: Approach phase



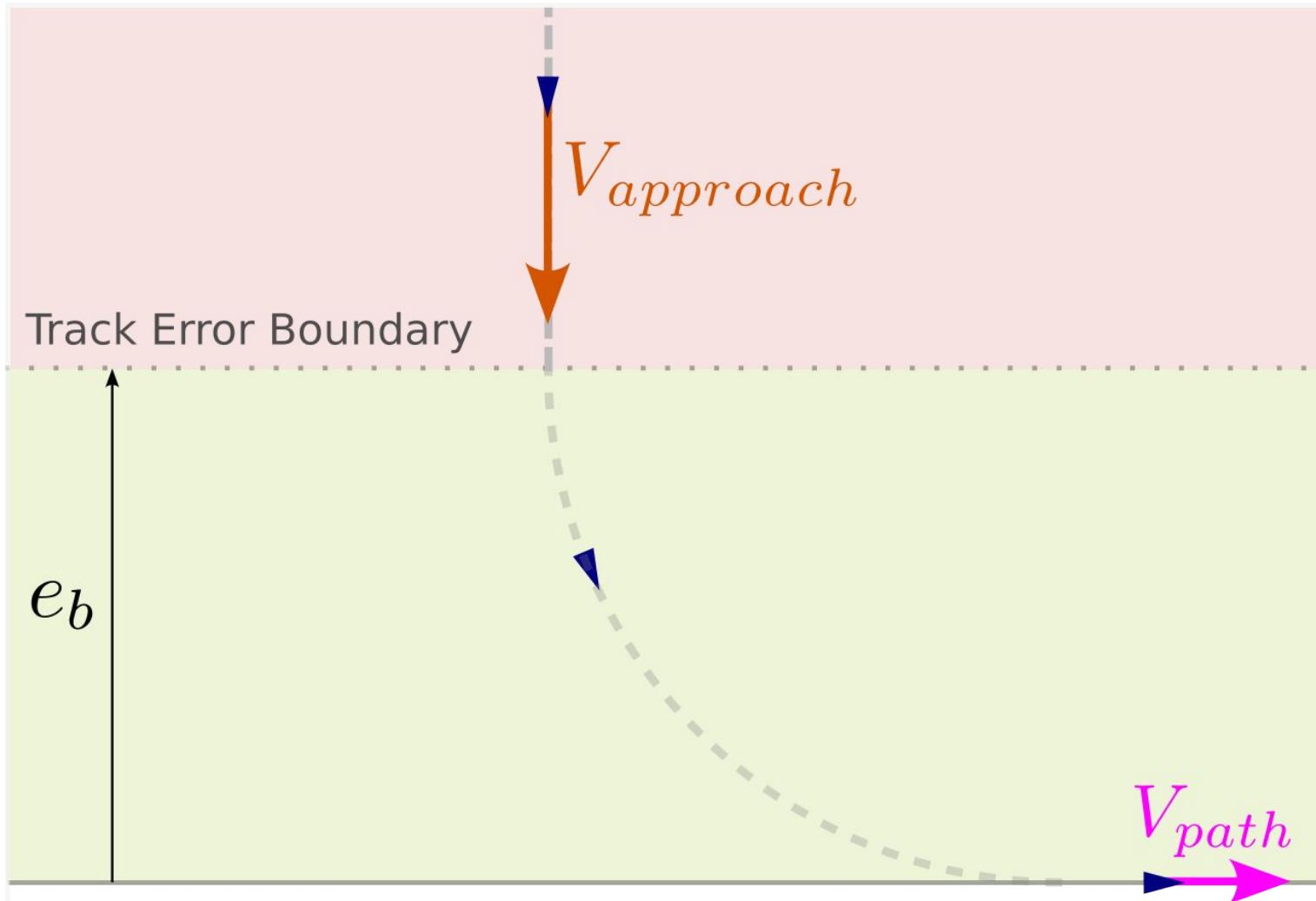
# Problem Definition: Turning phase



# Problem Definition: On path phase

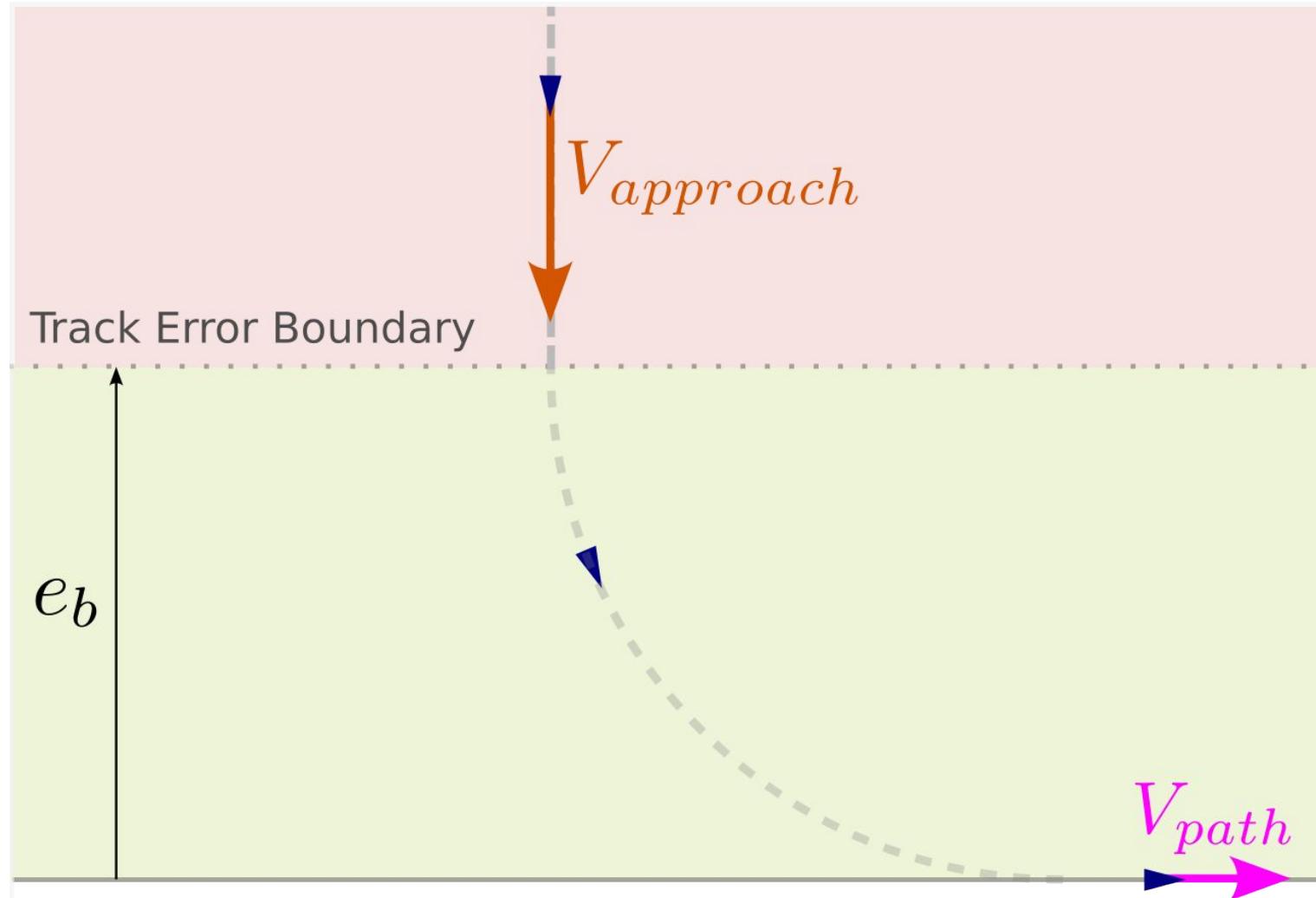


# Problem Definition: Re-defined



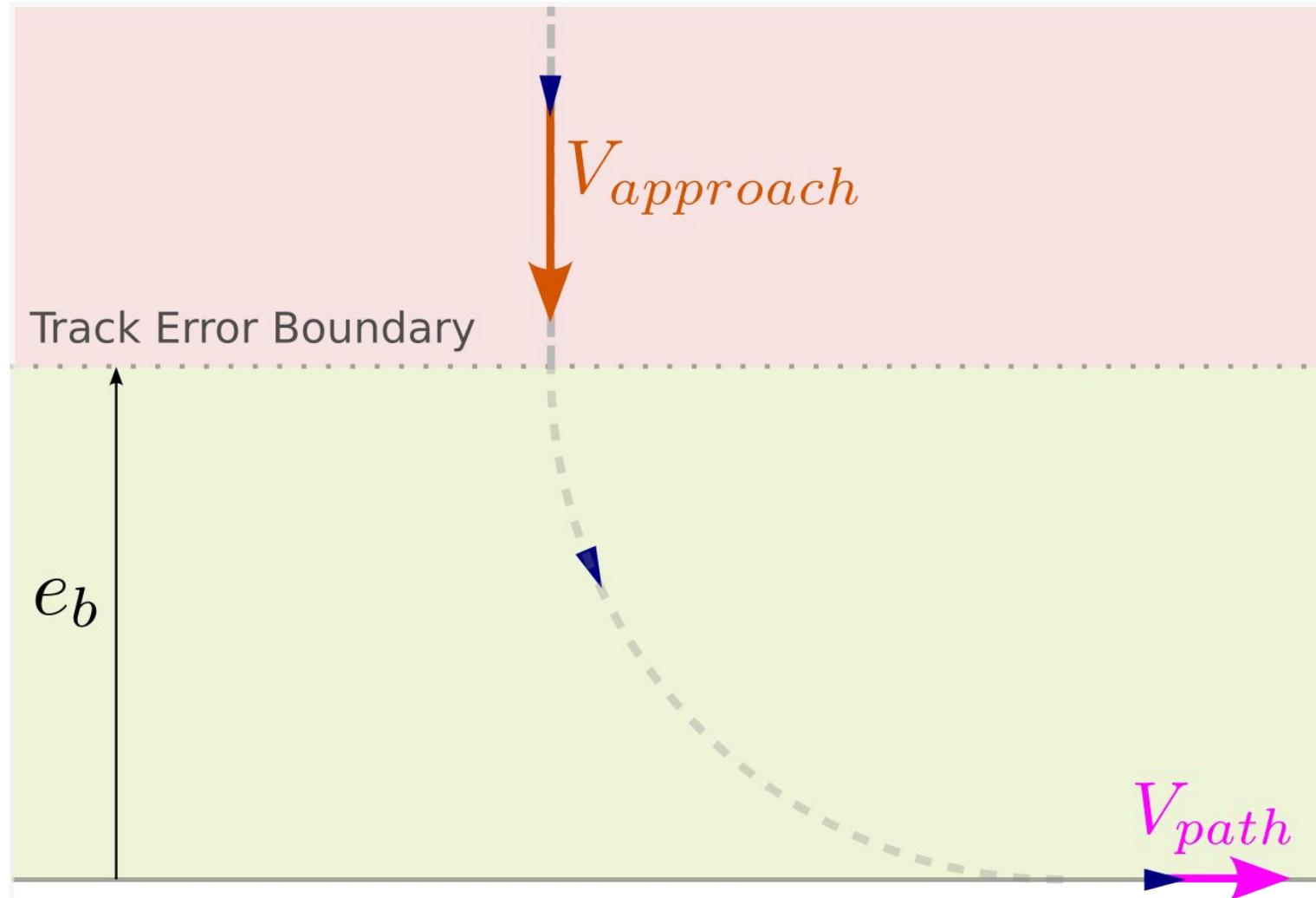
- **3 Phase sequence** (Velocity profile, Track error boundary)

# Problem Definition: Re-defined



- **3 Phase sequence** (Velocity profile, Track error boundary)
- **Acceleration commands** to guide the vehicle

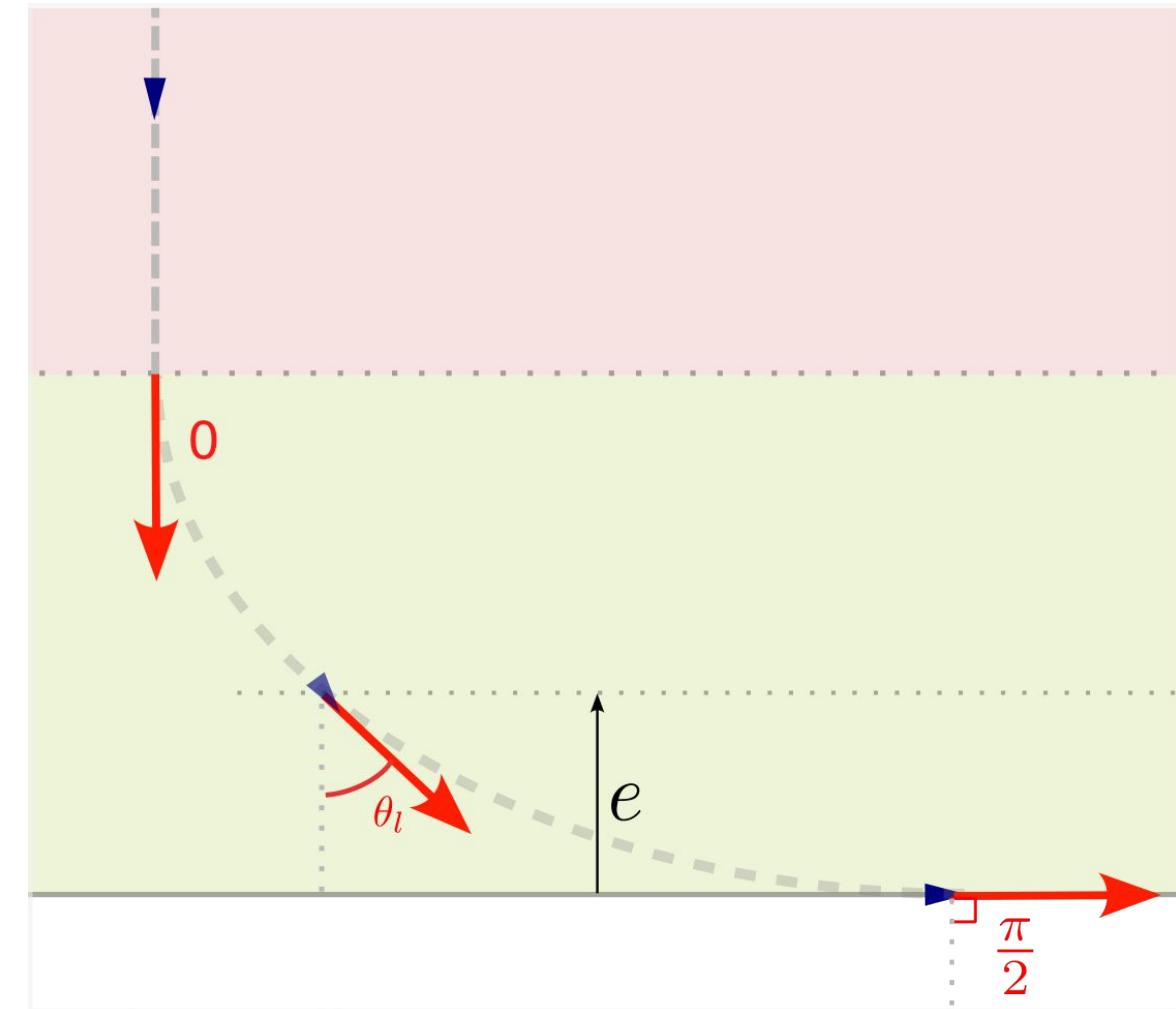
# Problem Definition: Re-defined



- **3 Phase sequence** (Velocity profile, Track error boundary)
- **Acceleration commands** to guide the vehicle
- While respecting vehicle's **maneuverability**

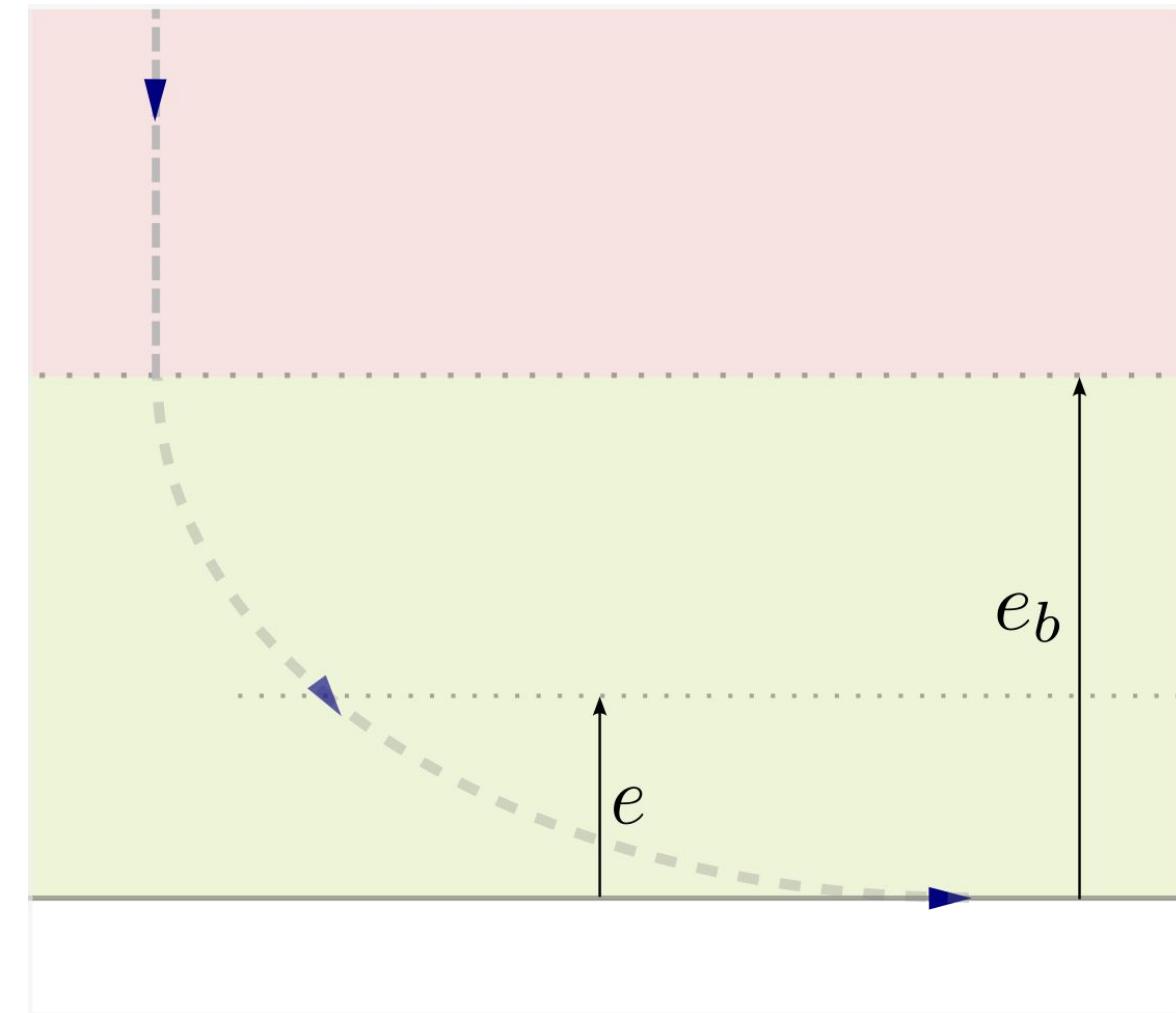
# Problem Definition: Defining the Ground Velocity Curve

- Look-ahead angle



# Problem Definition: Defining the Ground Velocity Curve

- Look-ahead angle
- Path parallel / orthogonal velocity
- **Track error boundary**



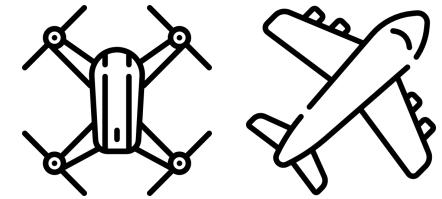
# Evaluation

## Conditions

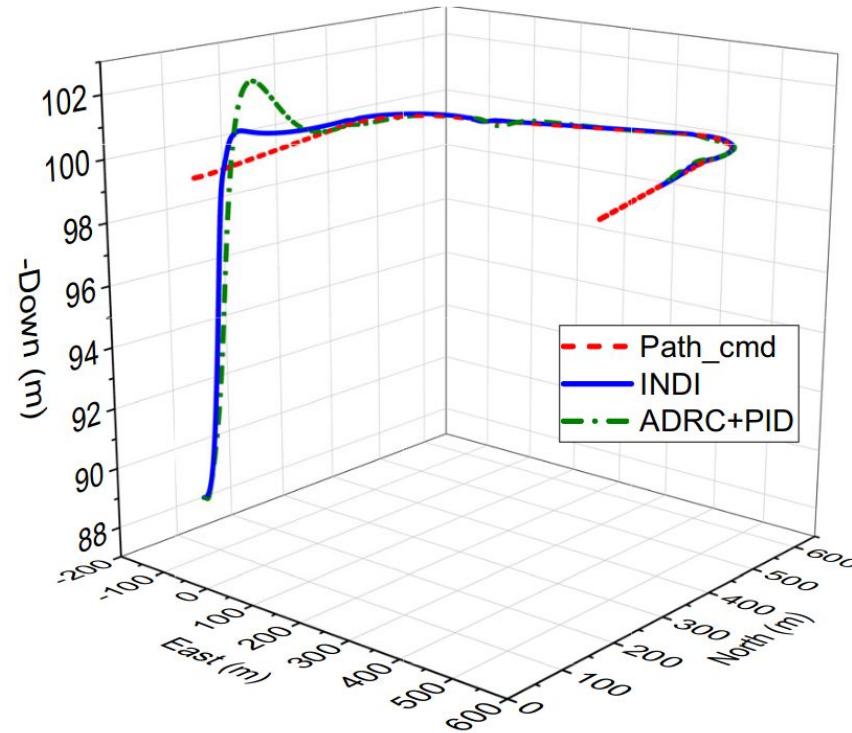
- Track error boundary: 70 m
- Approach speed: 10 m/s
- Speed on path: 15 m/s

Criteria	Unicyclic	Hybrid Unicyclic
Time to Converge	12.5 seconds	21.2 seconds
Converging path parallel travel	82 m	82 m
Ground speed monotonicity	True	True

# Related Work: Path Following on Hybrid VTOL



- INDI based Vector Field Path Following [Zhou, 2022]



Li, Zhou. "Incremental nonlinear dynamic inversion based path-following control for a hybrid quad-plane unmanned aerial vehicle" (2022)

# References

1. <https://www.pix4d.com/blog/modelling-matterhorn/>
2. <https://tenor.com/view/who-cares-meme-gif-24186451>
- 3.