

Thoughts while making final presentation

I had some thoughts & deeper review / overview on the project’s status while making the final presentation: [Junwoo Hwang | Final Presentation | BA](#). I would like to collect them here and discuss after the trial presentation.

Ground Velocity Curve

- **Look-ahead angle** as a function of normalized track error alone **defines the exact ground course profile of approaching the path!**
 - V_approach and V_path only acts as a ‘starting’ and ‘ending’ speed while following that course profile, and nothing else!
 - Technically, the same ground course profile can be followed with either: Constant speed, varying speed, etc, that’s up to the velocity setpoint
 - When look-ahead angle function is fixed, the **‘track error boundary’ defines solely the scaling of the whole ground course.**
 - In fact, the **parallel travel along the path until convergence is only dependent on the track error boundary** with a fixed look-ahead angle function. And it scales linearly.
 - Proof:
$$d_{conv} = - \int_{e_b}^0 V_g^{\parallel} \cdot \frac{1}{V_g^{\perp}} de = e_b \cdot \int_0^1 V_g^{\parallel} \cdot \frac{1}{V_g^{\perp}} d\hat{e} = e_b \cdot \int_0^1 \tan(\theta_{la}(\hat{e})) d\hat{e}$$
 - Reference: [15 Multirotor NPFG Formulation](#)
- However the **‘convergence time’ is indeed dependent in the magnitude of the velocity** following the ground course profile!

Therefore, the ground velocity curve problem breaks down into:

1. Defining look-ahead angle function (Shape of approach)
2. Defining track error boundary (Scale of approach)
3. Defining speed (norm of the velocity) profile (Convergence time & dynamics)

And the step 2 ~ 3 essentially encompasses the choice of V_approach and V_path!

Evaluations

Bringing back the evaluations, we can re-formulate the 3 step process incorporated into metrics like so:

Variables: $\theta_{la}(\hat{e})$ course shape, e_b track error boundary, $V_g(\hat{e})$ speed over ground profile

Criteria	Description	Evaluation
Time to convergence on a path [s]	Time required by the vehicle to converge to the path when following the ground velocity vector field with no error $t_{conv} = - \int_{e_b}^0 \frac{1}{V_g^{\perp}} de = e_b \cdot \int_0^1 \frac{1}{V_g(\hat{e}) \cdot \cos(\theta_{la}(\hat{e}))} d\hat{e} \text{ (when } e_b \text{ is constant)}$	Smaller the better
Track error boundary length [m]	e_b	Smaller the better
Converging path parallel distance [m]	Path-parallel distance travelled to converge to path when following ground velocity vector field with no error $d_{conv} = - \int_{e_b}^0 V_g^{\parallel} \cdot \frac{1}{V_g^{\perp}} de = e_b \cdot \int_0^1 V_g^{\parallel} \cdot \frac{1}{V_g^{\perp}} d\hat{e} = e_b \cdot \int_0^1 \tan(\theta_{la}(\hat{e})) d\hat{e} \text{ (when } e_b \text{ is constant)}$	Smaller the better

Velocity on Path fulfilled [bool]	$V_g^{\parallel} = V_{path} \text{ when } \hat{e} = 0$	Needs to be True
Speed monotonicity [bool]	Whether the magnitude of velocity grows or decreases consistently throughout track error boundary $\{\frac{d}{de} V_g(e) \geq 0 \mid \text{for all } e \in [0, e_b]\}$ Or $\{\frac{d}{de} V_g(e) \leq 0 \mid \text{for all } e \in [0, e_b]\}$	Needs to be True
Total acceleration RMS [m/s^2]	Root-Mean-Square value of acceleration $acc_{rms} = \sqrt{-\frac{1}{e_b} \cdot \int_{e_b}^0 (\frac{d}{dt}V_g(e) ^2) de} = \sqrt{\int_0^1 (\frac{d}{dt}V_g(\hat{e}) ^2) d\hat{e}} \text{ (when } e_b \text{ is constant)}$ $= \sqrt{\int_0^1 [\frac{d}{dt}V_g(\hat{e}) ^2 + V_g(\hat{e}) \cdot \frac{d}{dt}\theta_{la}(\hat{e})] d\hat{e}} = \sqrt{\frac{1}{e_b} \int_0^1 [V_g(\hat{e}) \cos(\theta_{la}(\hat{e})) \cdot \frac{d}{de}V_g(\hat{e}) ^2 + (V_g(\hat{e}) \cdot \frac{d}{de}\theta_{la}(\hat{e}))^2] d\hat{e}}$	Smaller the better
Maximum acceleration total [m/s^2]	Maximum total acceleration $acc_{max} = \max\{\frac{d}{dt}V_g(e) \mid \text{for } e \in [0, e_b]\} = \frac{1}{e_b} \cdot \max\{V_g \cos(\theta_{la}(\hat{e})) \cdot \sqrt{ \frac{d}{de}V_g(\hat{e}) ^2 + (V_g(\hat{e}) \cdot \frac{d}{de}\theta_{la}(\hat{e}))^2} \text{ for } \hat{e} \in [0, 1]\} \text{ (when } e_b \text{ is constant)}$	Smaller the better

Track error boundary scaling with ground speed

- This removes the absolute magnitude dependency (scaling), and keeps the scaling consistent
- HOWEVER, this doesn't apply in high-wind situations where the wind speed affects the ground speed significantly for different course targets!
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Path Following high-level command output

- To unify the control of MC & FW, the following commands are expected:
 - Course over ground
 - Ground speed
- Depending on whether it's a FW or a MC, we can have a different approach to controlling the vehicle to follow that setpoint
 - For FW: COG is maintained, but ground speed will likely not be exactly the same
 - For MC: COG and ground speed is both expected to be followed closely
- However, there's still a problem:
 - What do we do in an intermediate transition state?
 - How should this high-level path following control setpoint morph between MC <-> FW configuration, to create sane setpoints?
 - Lateral acceleration command is only applicable to FW case, and thus the whole control pipeline isn't really *unified
 - **INDI** could help in this case?
 - E.g. <https://onlinelibrary.wiley.com/doi/abs/10.1002/rnc.6503>