

1. e
 2. c, d
 3. a, c
 4. b, d
 5. c
 6. a, e
 7. b
8. (a) $E(u_t | Y_{t-1}, Y_{t-2}, \dots) = 0$ because Y_{t-p} for $p = 1, 2, \dots$ is a function of $(u_{t-p}, u_{t-p-1}, \dots)$ and u_t is i.i.d.
- (b) $E(Y_t) = \frac{\beta_0}{1 - \beta_1}$, $\text{var}(Y_t) = \frac{\sigma_u^2}{1 - \beta_1^2}$ due to stationarity of Y_t and $E(u_t) = 0$ and $\text{var}(u_t) = \sigma_u^2$
- (c) $\rho_1 = \text{corr}(Y_t, Y_{t-1}) = \beta_1$ from $\text{cov}(Y_t, Y_{t-1}) = \beta_1 \text{var}(Y_{t-1}) = \frac{\beta_1 \sigma_u^2}{1 - \beta_1^2}$
- $\rho_2 = \text{corr}(Y_t, Y_{t-2}) = \beta_1^2$ from $\text{cov}(Y_t, Y_{t-2}) = \beta_1^2 \text{var}(Y_{t-2}) = \frac{\beta_1^2 \sigma_u^2}{1 - \beta_1^2}$
- $\rho_p = \text{corr}(Y_t, Y_{t-p}) = \beta_1^p$ from $\text{cov}(Y_t, Y_{t-p}) = \beta_1^p \text{var}(Y_{t-p}) = \frac{\beta_1^p \sigma_u^2}{1 - \beta_1^2}$
- (d) $Y_{T+1|T} = E(Y_{T+1} | Y_T, Y_{T-1}, \dots) = E(\beta_0 + \beta_1 Y_T + u_{T+1} | Y_T, Y_{T-1}, \dots) = \beta_0 + \beta_1 Y_T = \beta_0 + \beta_1$
9. (a)

	Sample mean (\overline{earn})	Sample standard deviation (s_{earn})	Number of observations (n)
All	369.349	174.952	8033
Those without a college degree ($colgrad = 0$)	320.043	130.012	4233
College graduates ($colgrad = 1$)	424.273	200.315	3800

\overline{earn} is equivalent to the constant term estimate \hat{c} from $earn_i = c + \varepsilon_i$.

$$s_{earn} = \sqrt{n \times SE(\overline{earn})^2} = \sqrt{8033 \times 1.952^2} = 174.9519$$

From $earn_i = \gamma_0 + \gamma_1 colgrad_i + \varepsilon_i$,

$$\overline{earn}_{lcol} = \hat{\gamma}_0 = 320.0428$$

$$\overline{earn}_{colgrad} = \hat{\gamma}_0 + \hat{\gamma}_1 = 320.0428 + 104.2304 = 424.2732$$

$$s_{earn, lcol} = \sqrt{n_{lcol} \times SE(\hat{\gamma}_0)^2} = \sqrt{4233 \times 1.9983^2} = 130.0124$$

$$s_{earn, colgrad} = \sqrt{n_{colgrad} \times \left(SE(\hat{\gamma}_1)^2 - \frac{s_{earn, lcol}^2}{n_{lcol}} \right)} = \sqrt{n_{colgrad} \times (SE(\hat{\gamma}_1)^2 - SE(\hat{\gamma}_0)^2)}$$

$$= \sqrt{3800 \times (3.8148^2 - 1.9983^2)} = 200.315$$

- (b) $\hat{\beta}_1 = 110.9976$. Among 30–59 year old, male, full-time wage workers, college graduates earn 1,109,976 KRW more than those without a college degree holding age group constant.

Yes. When testing $H_0 : \beta_1 = 100$ vs. $H_1 : \beta_1 > 100$, the null hypothesis is rejected

at the 1% significance level because $t = \frac{110.9976 - 100}{3.7588} = 2.9258 > 2.33$.

(c) $\bar{R}^2 = 1 - \frac{n-1}{n-k-1}(1 - R^2) = 1 - \frac{8033-1}{8033-4}(1 - 0.1342542) = 0.1339$

- (d) Including *age3039* in the regression specification with a constant term results in perfect multicollinearity because $age3039 + age4049 + age5059 = 1$.

- (e) $H_0 : \beta_1 = \beta_2 = \beta_3 = 0$ vs. $H_1 : \beta_1 \neq 0$ and/or $\beta_2 \neq 0$ and/or $\beta_3 \neq 0$

The heteroskedasticity-robust F -statistic = 393.19 and the p -value $< 2.2 \times 10^{-16}$.

Thus, we can reject the null hypothesis at the 1% significance level.

- (f) No. Even when age (i.e., experience) are controlled for, there could still be systematic differences between college graduates and those without a college degree, for example, in family background or innate ability. If college graduates have higher innate ability and more able people earn more, $\hat{\beta}_1$ would be biased upwards and fail to uncover the causal effect of a college degree on earnings.