

Question 1

1)

a) Answer: D6.4E97

Convert to Binary number first: Integer Part :

$$214 = 128 + 64 + 16 + 4 + 2$$

$$214 = 11010110_2$$

Fractional Part :

$$0.307 \times 2 = 0.614$$

$$0.614 \times 2 = 1.228$$

$$0.228 \times 2 = 0.456$$

$$0.456 \times 2 = 0.912$$

$$0.912 \times 2 = 1.824$$

$$0.824 \times 2 = 1.648$$

$$0.648 \times 2 = 1.296$$

$$0.296 \times 2 = 0.592$$

$$0.592 \times 2 = 1.184$$

$$0.184 \times 2 = 0.368$$

$$0.368 \times 2 = 0.736$$

$$0.736 \times 2 = 1.472$$

$$0.472 \times 2 = 0.944$$

$$0.944 \times 2 = 1.888$$

$$0.888 \times 2 = 1.776$$

$$0.776 \times 2 = 1.552$$

0100 1110 1001 0111

$$214 = 11010110.0100\ 1110\ 1001\ 0111_2$$

$$= D6.4E97$$

b)

Decimal	Binary	Grey
0	000	000
1	001	001
2	010	011
3	011	010
4	100	110
5	101	111
6	110	101
7	111	100

Grey code change one bit when traversing from one point to another. In a not non-synchronized process, for a normal binary digit system, incrementing or decrementing can leave the number in a variety of intermediary states.

c) Answer: $ac' + ad + b'cd + e'$

$$F(a, b, c, d, e) = [(c' + b e) (a' e + b' c)]' [(c d') + e']$$

$$(a' c' e + b' c c' + a' b e + b b' c e)' (c' + d + e')$$

$$= (a' c' e + a' b e)' (c' + d + e')$$

$$= [a' e (c' + b)]' (c' + d + e')$$

$$= [(a' e)' + (c' + b)'] (c' + d + e')$$

$$= (a + e' + c b') (c' + d + e')$$

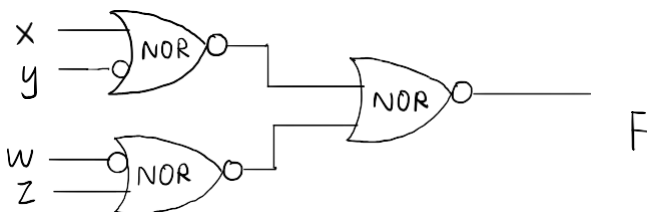
$$= a c' + a d + a e' + e' c' + e' d + e' + b' c c' + c b' d + c b' e'$$

$$= a c' + a d + c b' d + e'$$

d)

NOR Gate $(A+B)'$

$$F = ((x + y')' + (w' + z)')$$



e)

AB/CD	00	01	11	10
00	1	0	0	1
01	0	1	1	0
11	0	1	1	0
10	1	1	0	1

Circle 0

$$\text{Answer: } F = (B' + D)(A + B + D')(B + C' + D')$$

Question 2

2)

a) 10001100

$$\begin{array}{r} 10001100 \\ +10011010 \\ \hline 100100110 \end{array}$$

There is overflow, the 2 same sign bit added and got an answer with the opposite sign. Add two negative number and get a positive answer indicates that there is overflow.

$$\begin{array}{r} 01001010 \\ +00111111 \\ \hline 10001001 \end{array}$$

No overflow

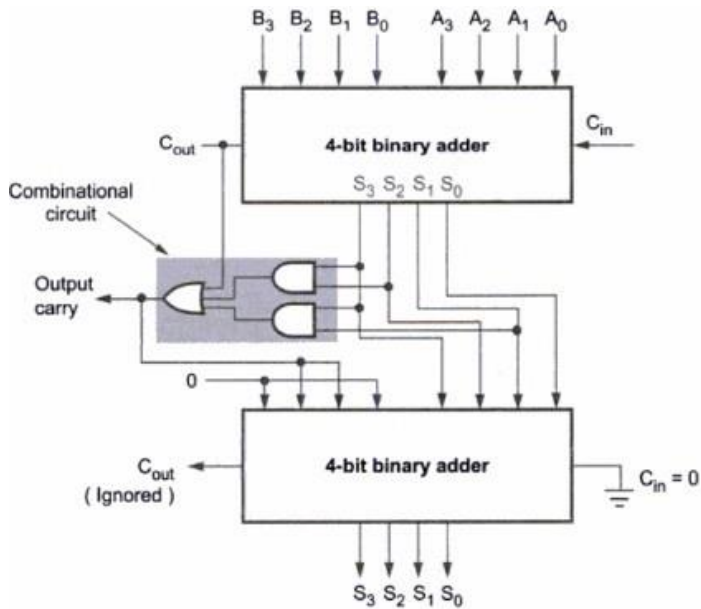
b)

i) $X=1$ when $\text{sum} \geq 9$

Sum[3:0]	00	01	11	10
00	0	0	0	0
01	0	0	0	0
11	1	1	1	1
10	0	0	1	1

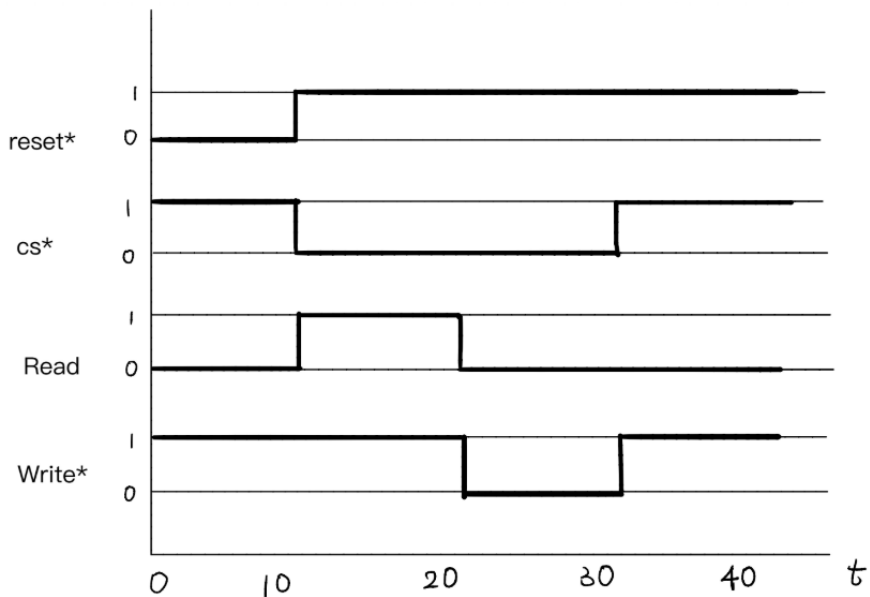
$$X = \text{sum}[3]\text{sum}[2] + \text{sum}[3]\text{sum}[1]$$

ii)



Source: <https://www.gues10.com/p/15365/implement-single-digit-bcd-adder-using-4-bit-bin-2/>

c)



d)

i) $Z = 1$

Boolean Expression: $A'(B' + C') + D'$

$B = 0$ or $C = 0$ and $A = 0$ or $D = 0$, Z produces logic 1.

$Z = 0$

Boolean Expression: $(A + BC)D$

$B = 1$ and $C = 1$ or $A = 1$ and $D = 1$, Z produce logic 0

ii)

A	B	C	D	Z
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	1
0	1	1	0	1
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	1
1	1	1	1	0

		CD			
Z	AB	00	01	11	10
		1	1	1	1
01		1	1	0	1
11		1	0	0	1
10		1	0	0	1

Answer:

$$Z = (A' + D')(B' + C' + D')$$

Question 3

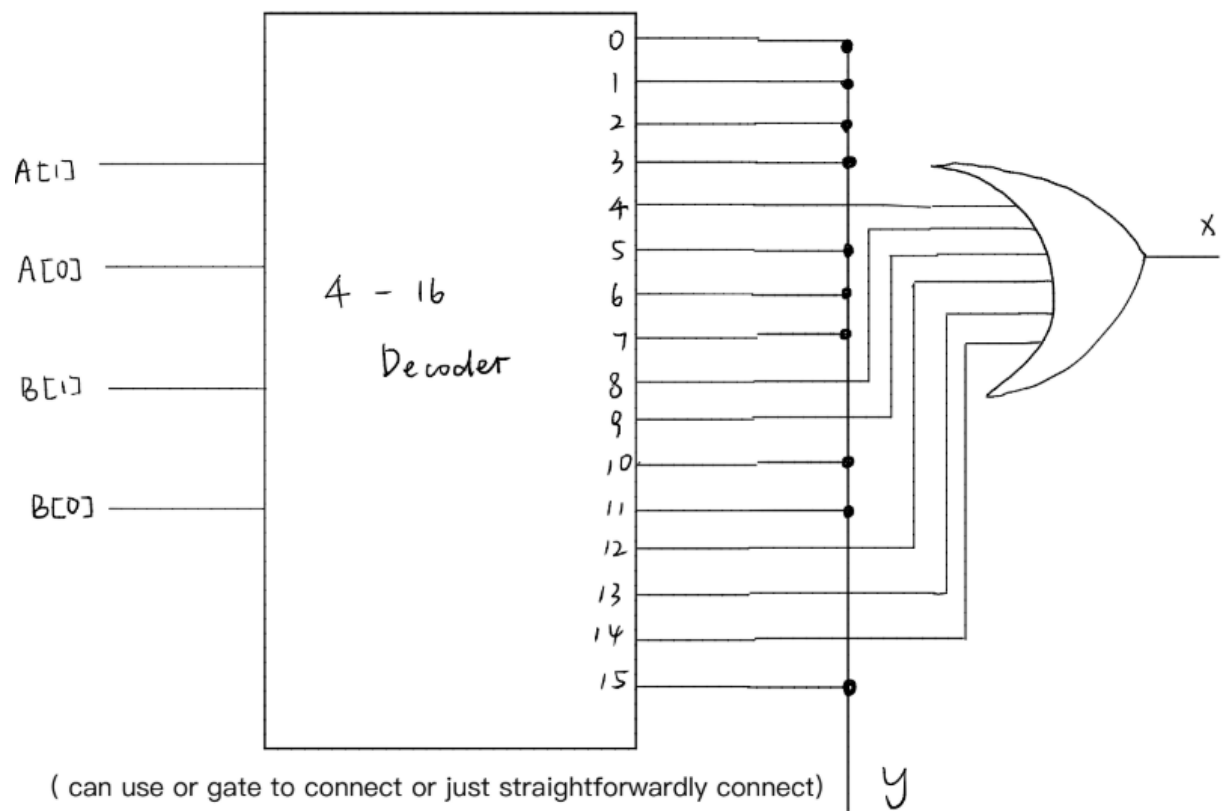
3)

a)

i)

A[1]	A[0]	B[1]	B[0]	X	Y
0	0	0	0	0	1
0	0	0	1	0	1
0	0	1	0	0	1
0	0	1	1	0	1
0	1	0	0	① 4	0
0	1	0	1	0	1
0	1	1	0	0	1
0	1	1	1	0	1
1	0	0	0	① 8	0
1	0	0	1	① 9	0
1	0	1	0	0	1
1	0	1	1	0	1
1	1	0	0	① 12	0
1	1	0	1	① 13	0
1	1	1	0	① 14	0
1	1	1	1	0	1

ii)



b)

//write the module for the 2-4 decoder

```
module decoder2_4 (output reg [3:0] d_out,
                  input [1:0] ival)
always @*
    case(ival)
        2'b00 : d_out = 4'b0001;
        2'b01 : d_out = 4'b0010;
        2'b10 : d_out = 4'b0100;
        2'b11 : d_out = 4'b1000;
    endcase
endmodule
```

//combinational circuit, instantiated decoder module

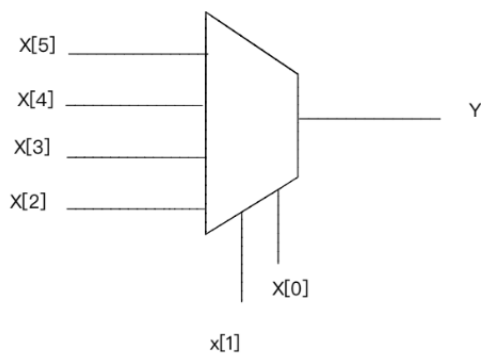
```
module decoder_app (input [5:0] X,
                   output Y)
    wire [3:0] d;
    wire xd1, xd2, xd3, xd4;

    decoder2_4 dd (.output(d[3:0]),
                  .input(x[1:0]));

    assign xd1 = x[2]&d[0];
    assign xd2 = x[3]&d[1];
    assign xd3 = x[4]&d[2];
    assign xd4 = x[5]&d[3];

    assign Y = xd1|xd2|xd3|xd4;
endmodule
```

c) It is a 4 input multiplexer with 2 selection pin.



d)

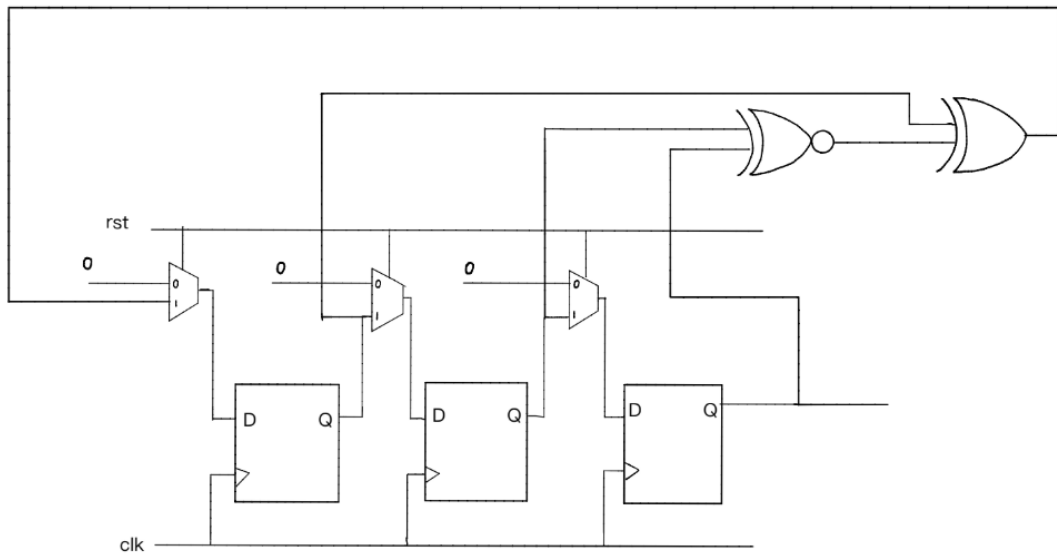
```
module mux_4to1 ( input [5:0] X, output reg Y);
always @ * begin
    case(X [1:0])
        2'b00: out <= X[2];
        2'b01: out <= X[3];
        2'b10: out <= X[4];
        2'b11: out <= X[5];
    endcase
end
endmodule
```

Question 4

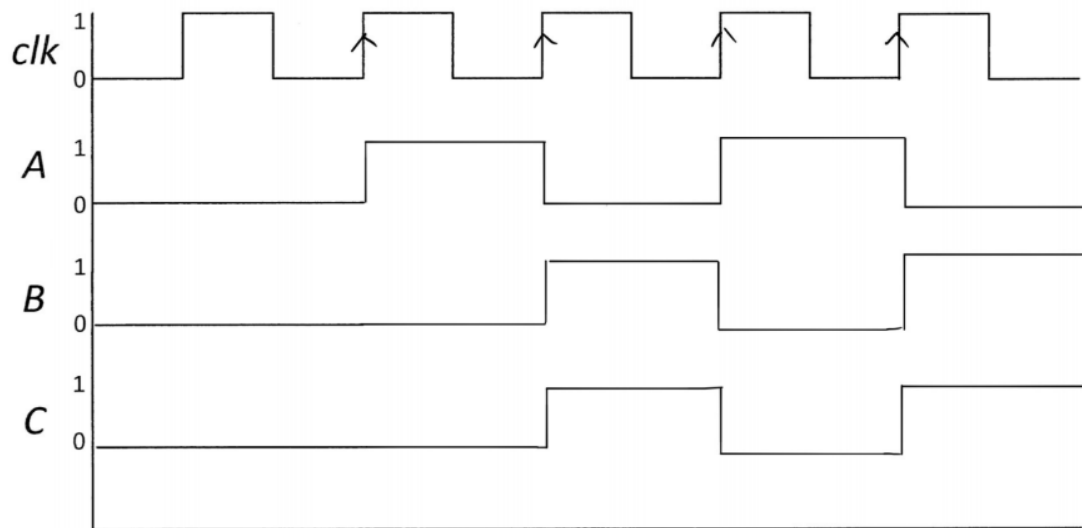
4)

a)

i)



ii)



b)

i)

B	Current_State	Next_State [1:0]	X
0	00	00	0
1	00	10	0
0	01	11	0
1	01	10	0
0	10	01	0
1	10	10	0
0	11	00	1
1	11	10	1

ii)

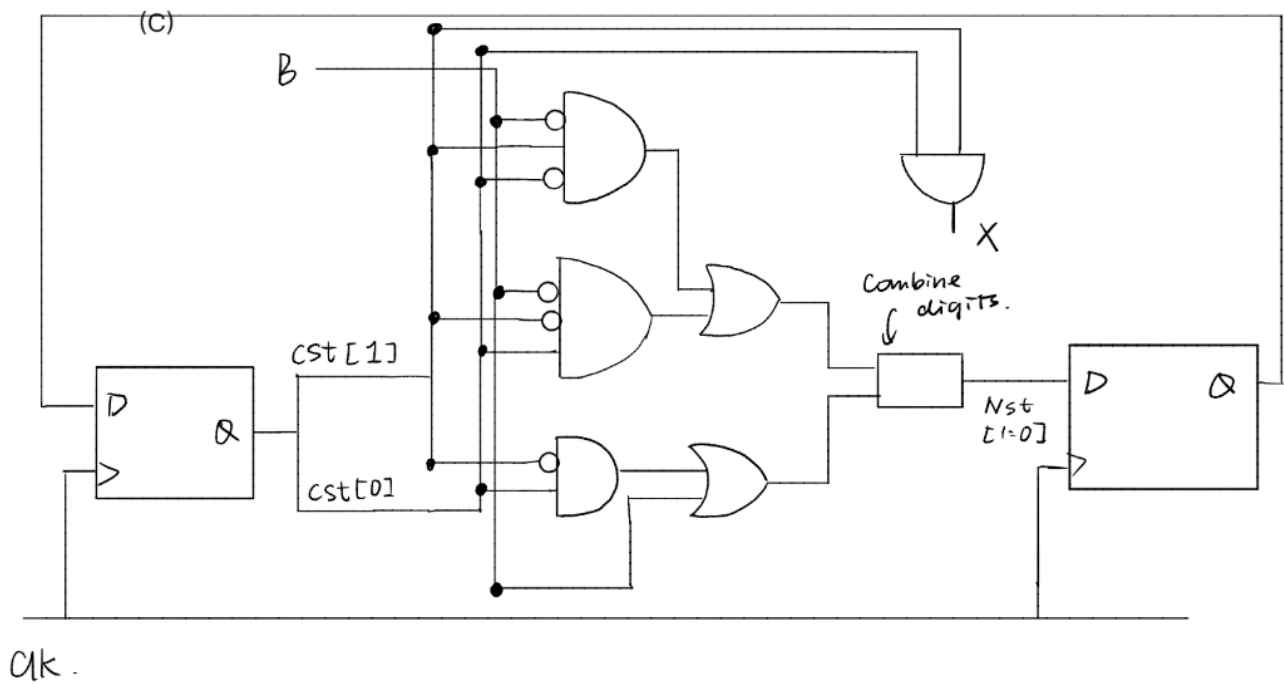
cst[1]	cst[0] B	Next_State[1]	Next_State[0]
000		0	0
001		1	0
010		1	1
011		1	0
100		0	1
101		1	0
110		0	0
111		1	0

$$\text{Next_State}[1] = B + \text{cst}[1]'\text{cst}[0]$$

$$\text{Next_State}[0] = \text{cst}[1]'\text{cst}[0]B' + \text{cst}[1]\text{cst}[0]B'$$

$$X = \text{cst}[1]\text{cst}[0]$$

c)



== End of Answers ==

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