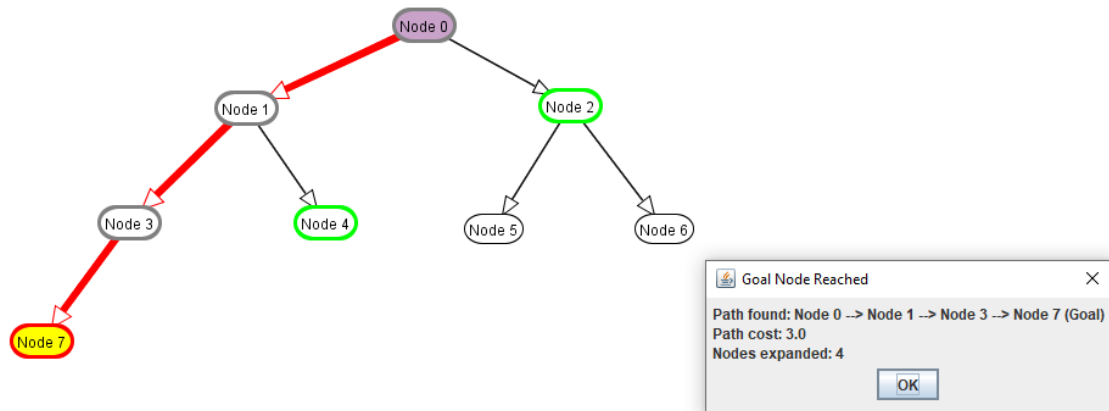


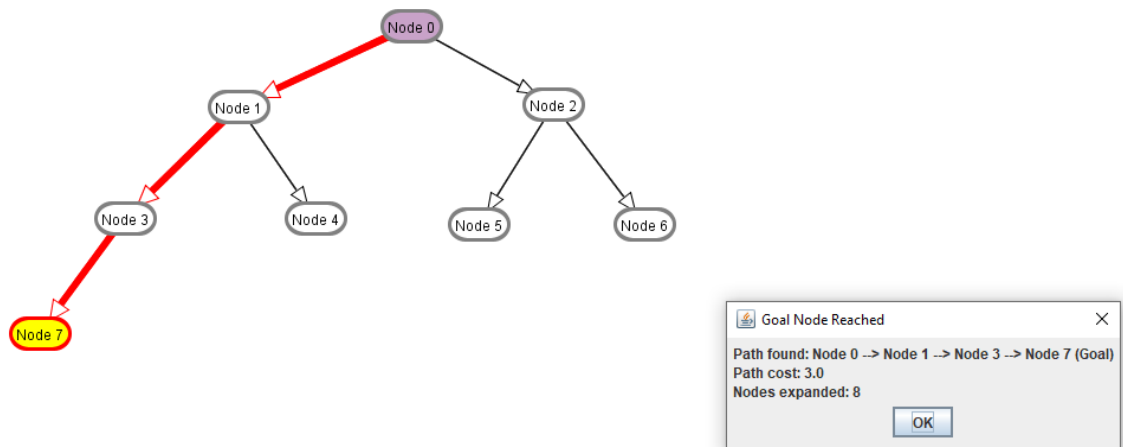
1 a)

Goal Node reached! (Node 0 → Node 1 → Node 3 → Node 7 (Goal))



**Figure 1.1: DFS**

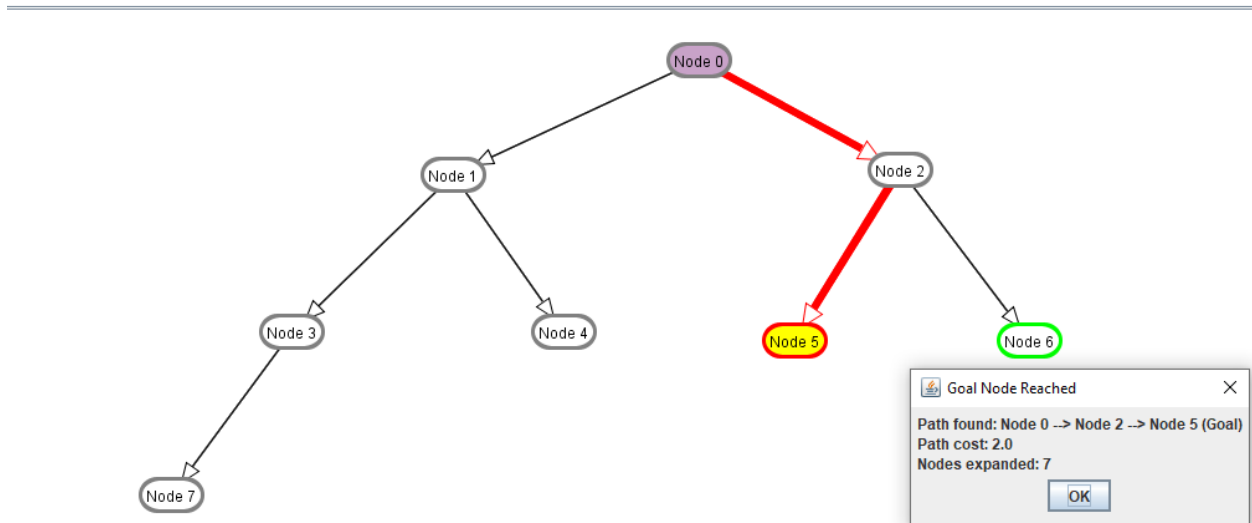
Goal Node reached! (Node 0 → Node 1 → Node 3 → Node 7 (Goal))



**Figure 1.2: BFS**

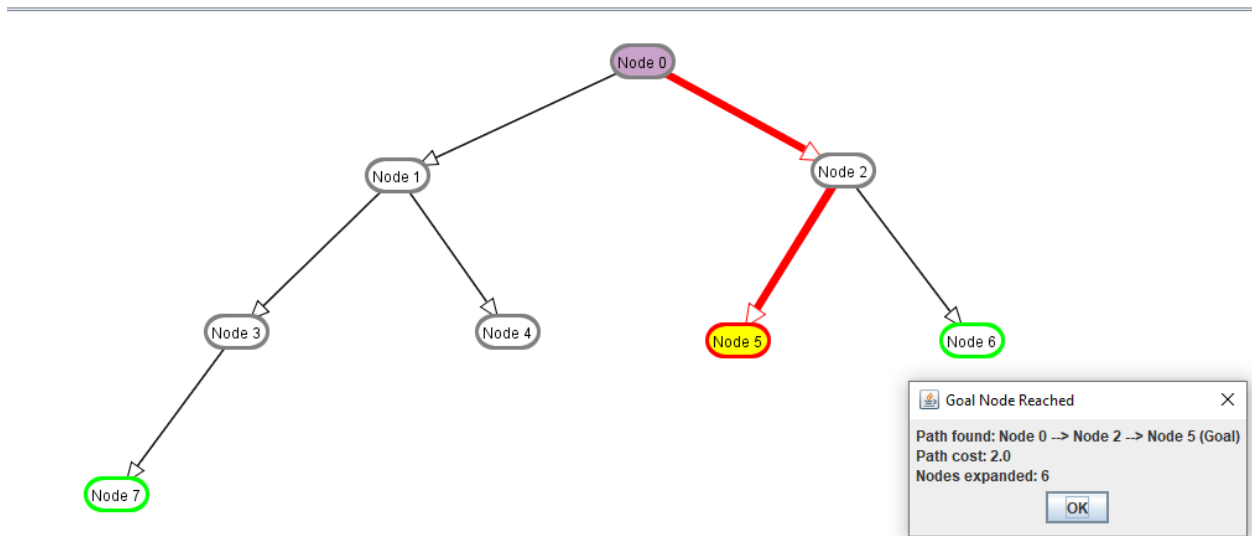
1 b)

Goal Node reached! (Node 0 --> Node 2 --> Node 5 (Goal))



**Figure 1.3: DFS**

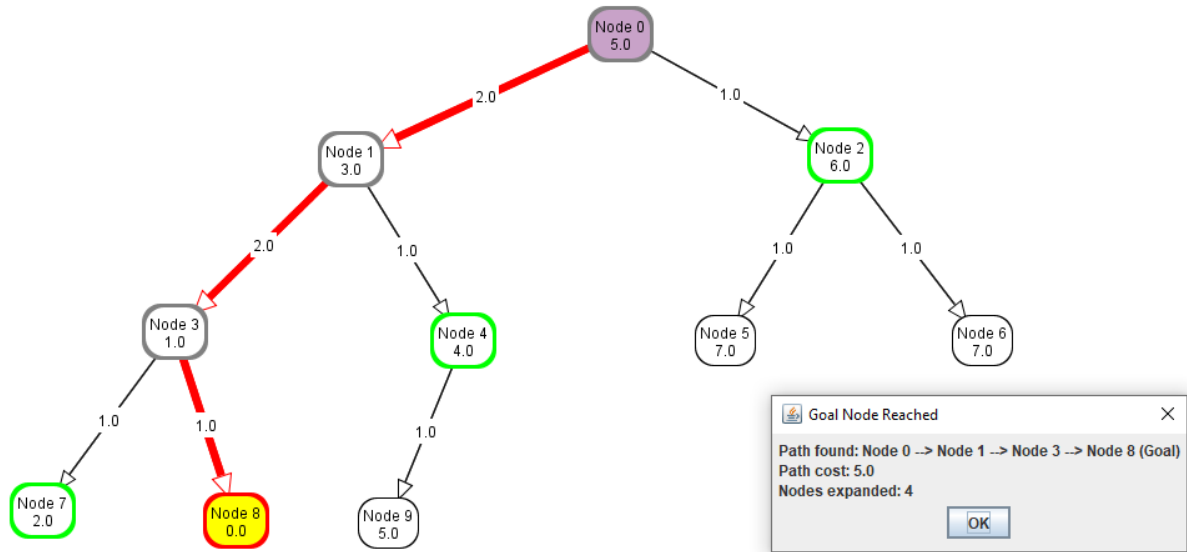
Goal Node reached! (Node 0 --> Node 2 --> Node 5 (Goal))



**Figure 1.4: BFS**

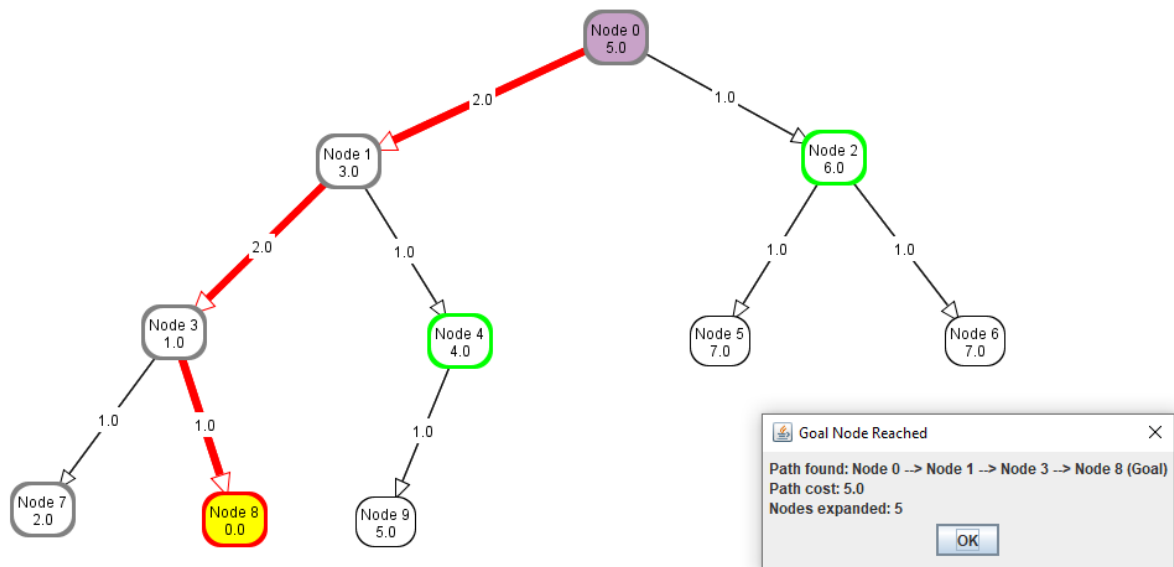
1 c) When there are heuristic values, estimated cost of reaching the goal.

Goal Node reached! (Node 0 → Node 1 → Node 3 → Node 8 (Goal))



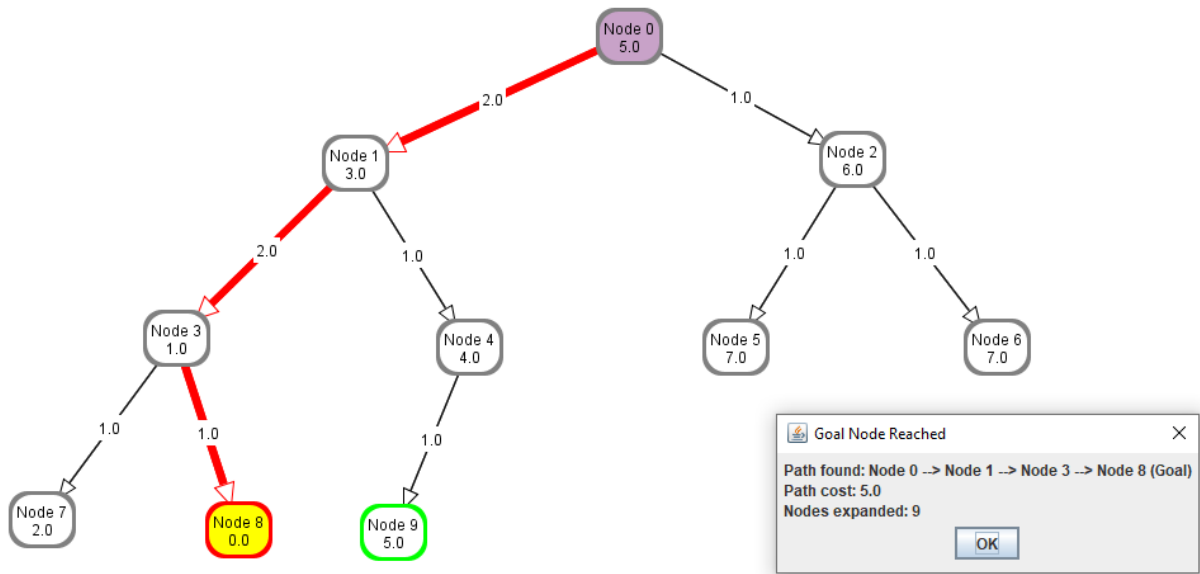
**Figure 1.5: A\***

Goal Node reached! (Node 0 → Node 1 → Node 3 → Node 8 (Goal))



**Figure 1.6: DFS**

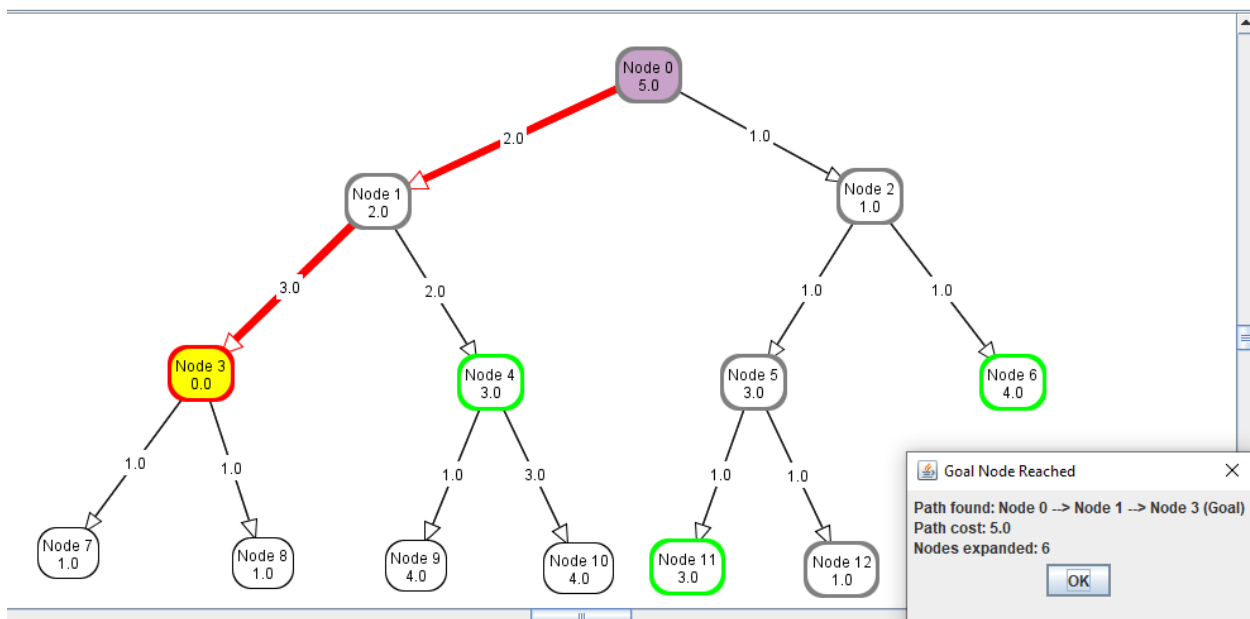
Goal Node reached! (Node 0 → Node 1 → Node 3 → Node 8 (Goal))



**Figure 1.7: BFS**

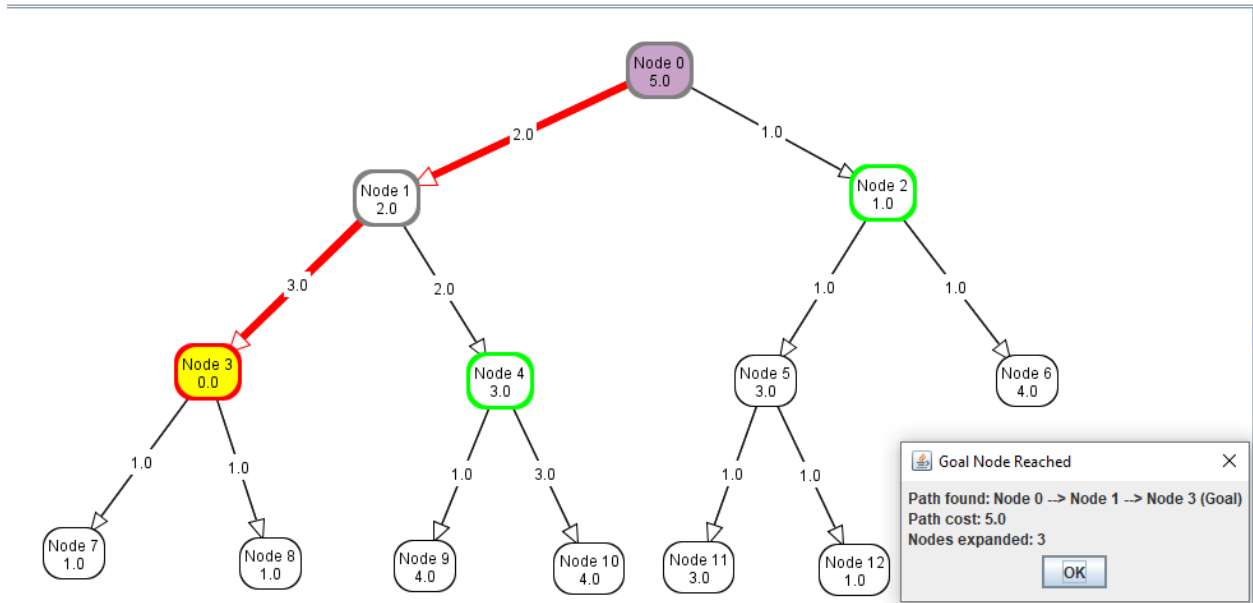
1 d) When the heuristic values are inconsistent, A\* will sometimes be inefficient.

Goal Node reached! (Node 0 → Node 1 → Node 3 (Goal))



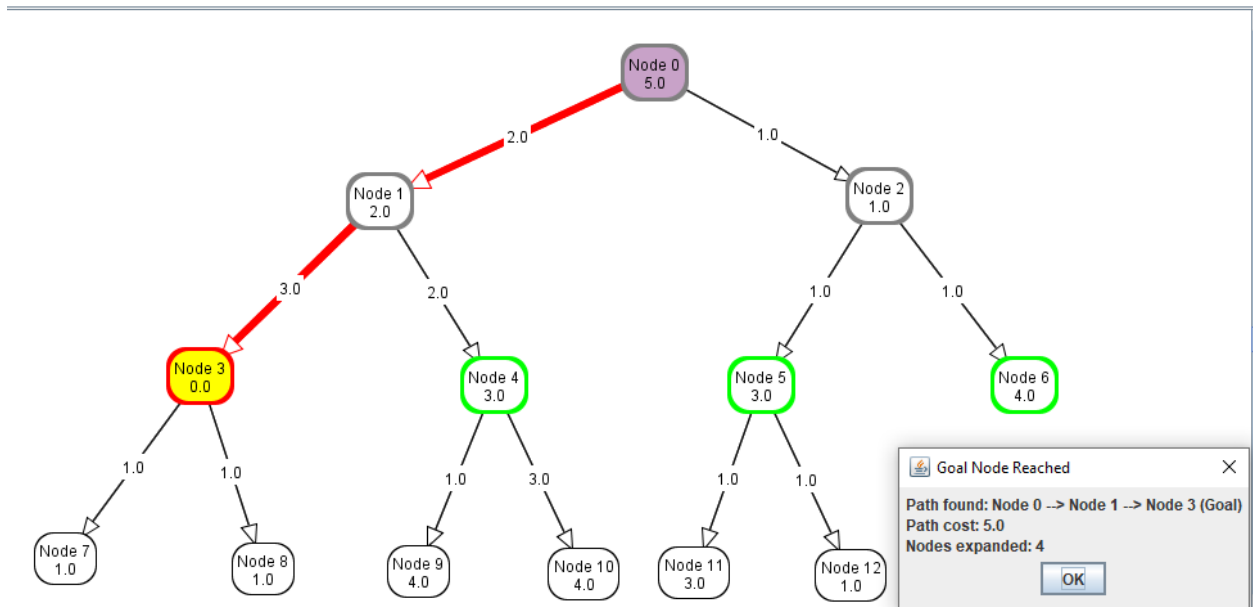
**Figure 1.8: A\***

Goal Node reached! (Node 0 → Node 1 → Node 3 (Goal))



**Figure 1.9: DFS**

Goal Node reached! (Node 0 → Node 1 → Node 3 (Goal))



**Figure 1.10: BFS**

2 a) Time taken to find an optimal solution will sometimes be slower, but solution is always optimal.

If  $h(n)$  is an underestimate, A\* will explore paths even if it is a non-optimal path, but the cost of exploration will start to add up and eventually be a non-optimal path. Then it will start to explore other paths until it reaches the goal. The solution will always be optimal.

**Example: If we were to reduce  $h(n)$  by factors of its default value**

Referring to Figure 2 below,

$h(n) = 1x$ , Nodes Expanded = 5.

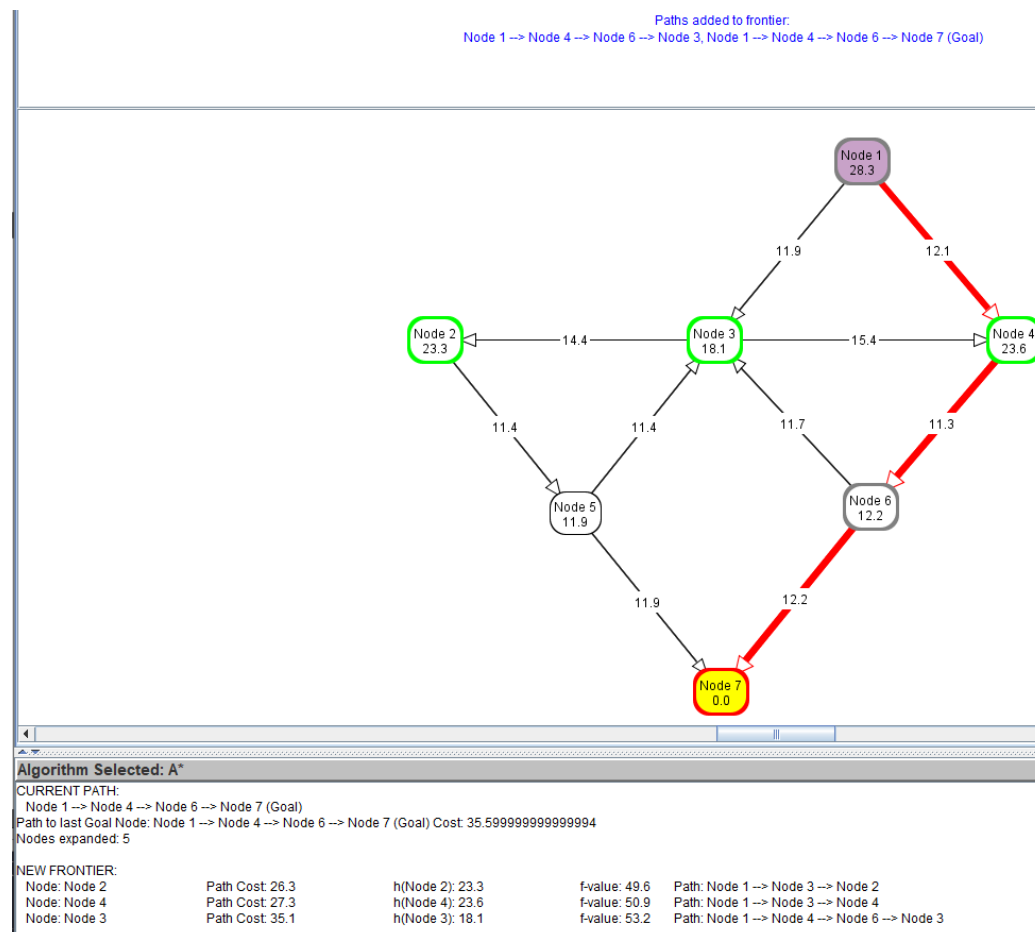
$h(n) = 0.9x$ , Nodes Expanded = 5.

$h(n) = 0.7x$ , Nodes Expanded = 5.

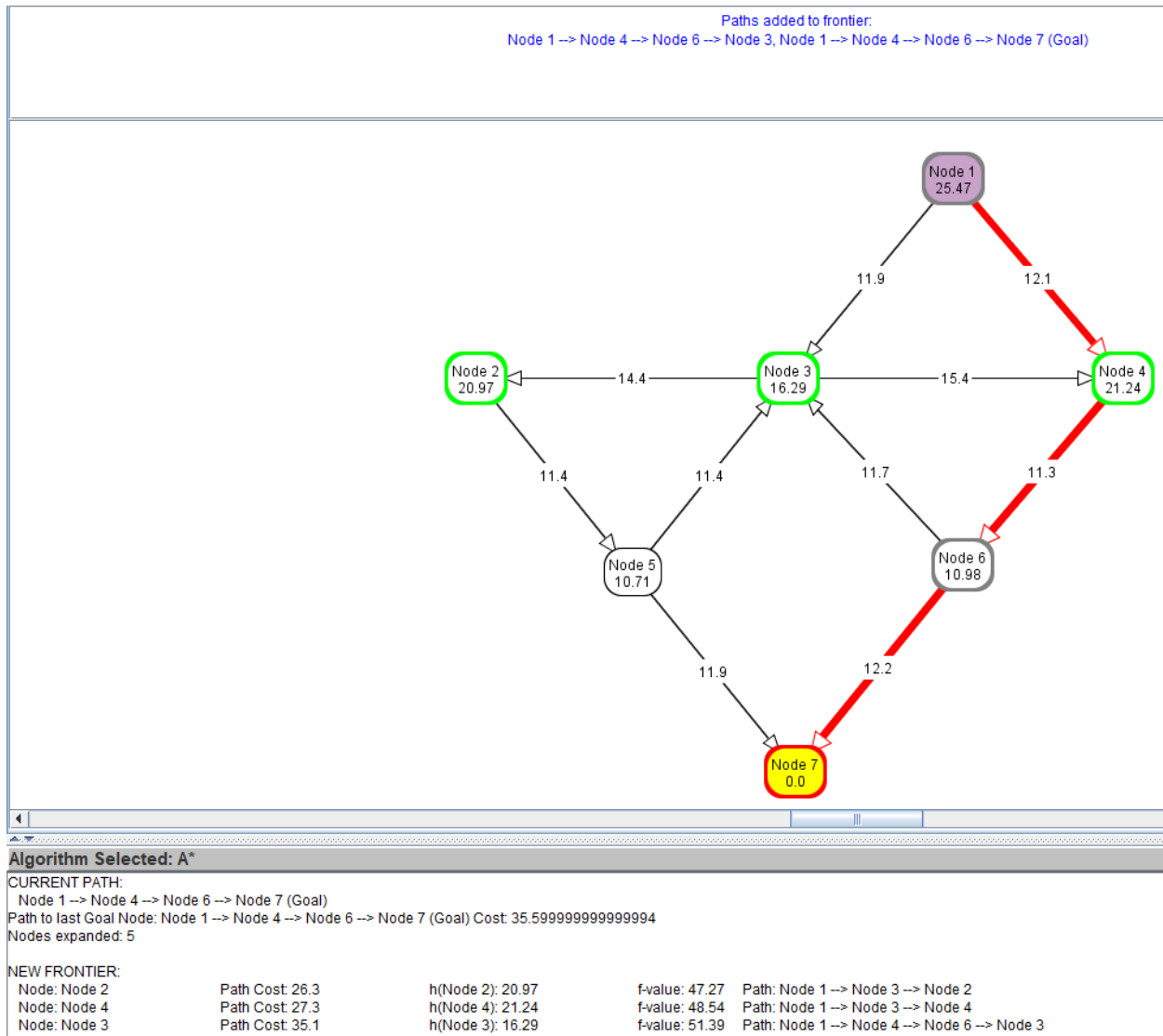
$h(n) = 0.3x$ , Nodes Expanded = 7.

$h(n) = 0.1x$ , Nodes Expanded = 7.

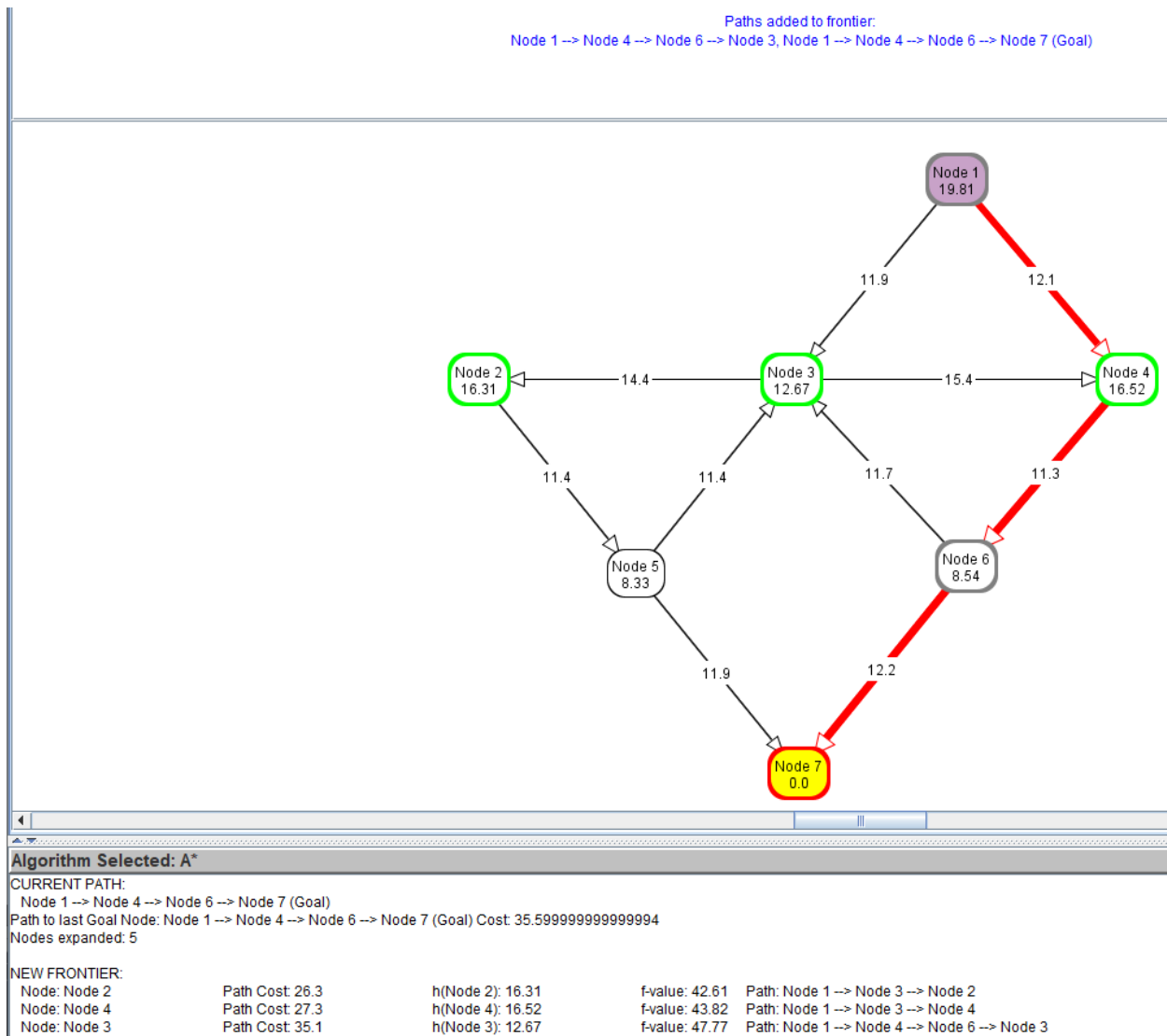
We can conclude that as the value of  $h(n)$  decreases, time taken will increase, however solution is always optimal.



**Figure 2.1: Auto Generated A\* (Default  $h(n)$  values)**



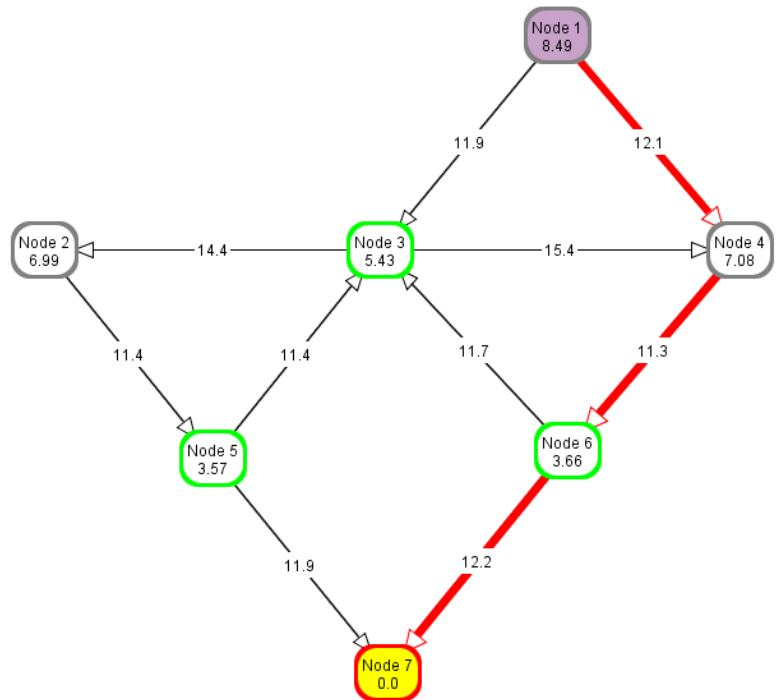
**Figure 2.2: Auto Generated A\* ( $h(n) = 0.9 \cdot h(n)$ )**



**Figure 2.3: Auto Generated A\* ( $h(n) = 0.7 \cdot h(n)$ )**



Paths added to frontier:  
Node 1 --> Node 3 --> Node 4 --> Node 6



#### Algorithm Selected: A\*

##### CURRENT PATH:

Node 1 --> Node 4 --> Node 6 --> Node 7 (Goal)

Path to last Goal Node: Node 1 --> Node 4 --> Node 6 --> Node 7 (Goal) Cost: 35.599999999999994

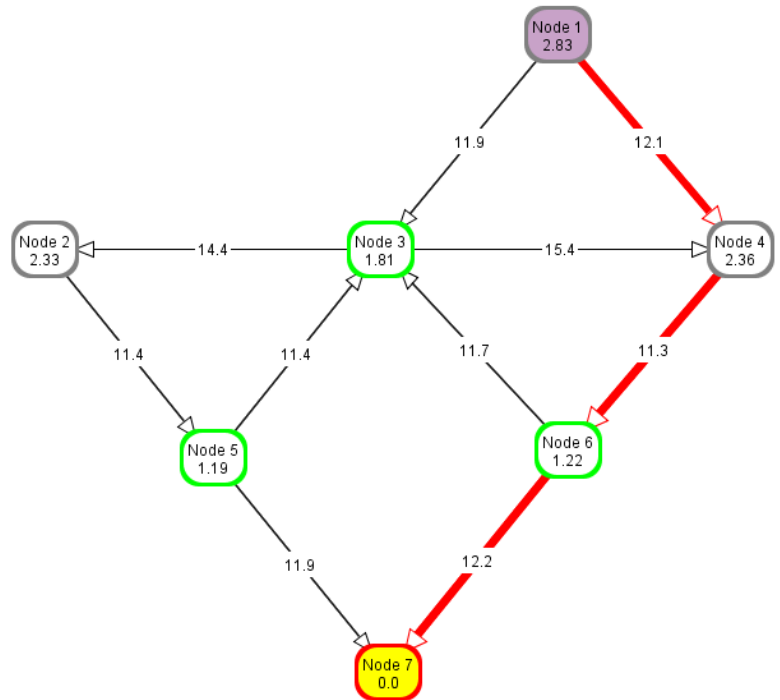
Nodes expanded: 7

##### NEW FRONTIER:

Node: Node 3	Path Cost: 35.1	h(Node 3): 5.43	f-value: 40.53	Path: Node 1 --> Node 4 --> Node 6 --> Node 3
Node: Node 5	Path Cost: 37.7	h(Node 5): 3.57	f-value: 41.27	Path: Node 1 --> Node 3 --> Node 2 --> Node 5
Node: Node 6	Path Cost: 38.6	h(Node 6): 3.66	f-value: 42.26	Path: Node 1 --> Node 3 --> Node 4 --> Node 6

**Figure 2.4: Auto Generated A\* ( $h(n) = 0.3 \cdot h(n)$ )**

Paths added to frontier:  
Node 1 → Node 3 → Node 4 → Node 6



**Algorithm Selected: A\***

**CURRENT PATH:**

Node 1 → Node 4 → Node 6 → Node 7 (Goal)

Path to last Goal Node: Node 1 → Node 4 → Node 6 → Node 7 (Goal) Cost: 35.599999999999994

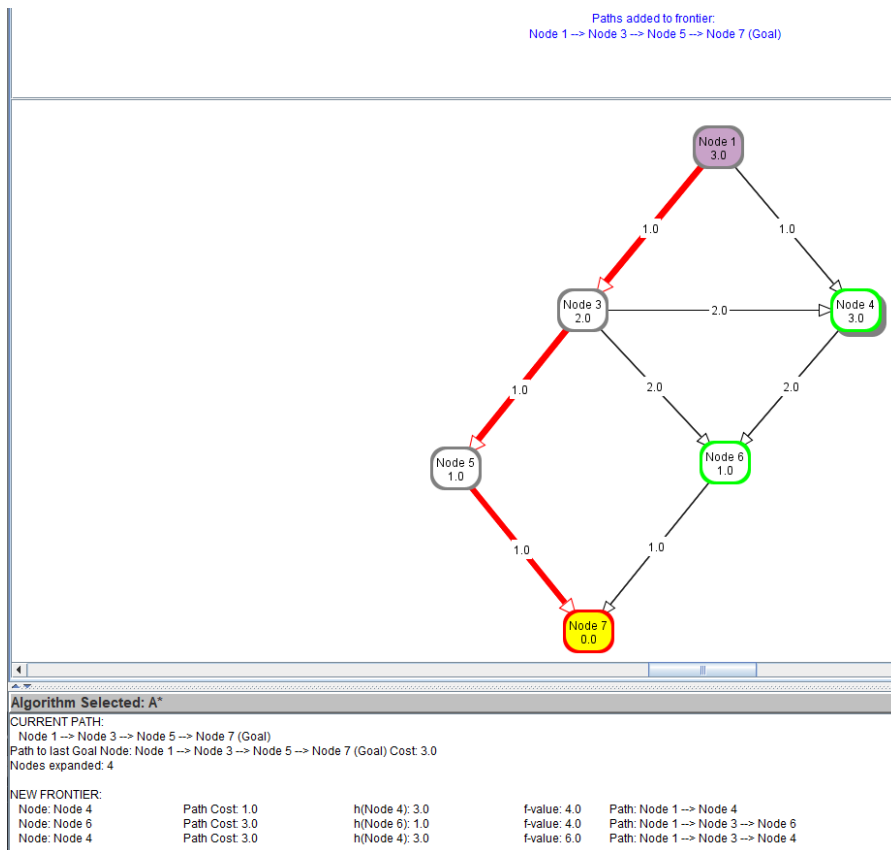
Nodes expanded: 7

**NEW FRONTIER:**

Node: Node 3	Path Cost: 35.1	h(Node 3): 1.81	f-value: 36.91	Path: Node 1 → Node 4 → Node 6 → Node 3
Node: Node 5	Path Cost: 37.7	h(Node 5): 1.19	f-value: 38.89	Path: Node 1 → Node 3 → Node 2 → Node 5
Node: Node 6	Path Cost: 38.6	h(Node 6): 1.22	f-value: 39.82	Path: Node 1 → Node 3 → Node 4 → Node 6

**Figure 2.5: Auto Generated A\* ( $h(n) = 0.1 \cdot h(n)$ )**

2 b) If  $h(n)$  is the exact distance, A\* will calculate the estimated cost and it will reach the goal with the optimal path.

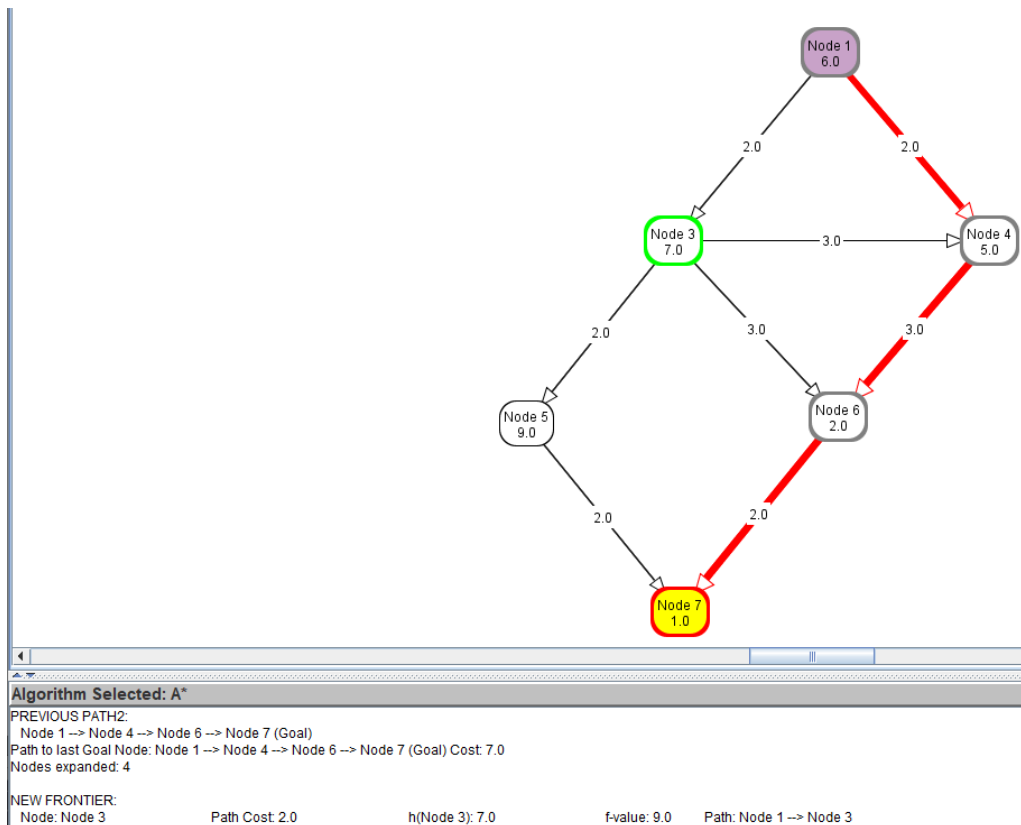


**Figure 2.6: A\* with exact  $h(n)$**

2 c) If  $h(n)$  overestimates, A\* will explore paths even if it is a non-optimal path, and it will not explore an optimal path with overestimated  $h(n)$ , because its value is worse. The solution will not be optimal.

Example:

We can see that the optimal path is from  $N1 \rightarrow N3 \rightarrow N5 \rightarrow N7$ , with a cost of 6. However, since the  $h(n)$  values of N3 and N5 are overestimated, A\* will not go down that optimal path, and will go on another path to reach the goal, where the solution is not optimal.



**Figure 2.7: A\* with overestimated  $h(n)$**