

Input

$$P_m: e_1, e_2, \dots, e_n$$

**Trainable B-spline Functions
(KAN_{transform})**

$$\phi: \quad \downarrow, \quad \downarrow, \quad \dots, \quad \downarrow$$

$$H_m: \phi(e_1), \phi(e_2), \dots, \phi(e_n)$$

$$H_m \rightarrow \text{Concat}(H_m \oplus \mathbf{1}, \mathbf{1} \oplus H_m)$$

Trainable B-spline Functions (KAN_m)

$$\quad \downarrow, \quad \downarrow, \quad \dots, \quad \downarrow$$

The Mapping Function f

$$\quad \downarrow \quad \downarrow \quad \dots \quad \downarrow$$

$$a_t = [a_{t,1}, \dots, a_{t,n}]$$

• **Matrix Multiplication**

KAN-Attention:

$$\text{Input: } P_m = \{e_1^m, e_2^m, e_3^m, \dots, e_n^m\}, m = \{T, A, V\}$$

Matrix:

$$H_T = [\phi_Q(e_1^m), \phi_Q(e_2^m), \phi_Q(e_3^m), \dots, \phi_Q(e_n^m)]$$

$$H_A = [\phi_K(e_1^m), \phi_K(e_2^m), \phi_K(e_3^m), \dots, \phi_K(e_n^m)]$$

$$H_V = [\phi_V(e_1^m), \phi_V(e_2^m), \phi_V(e_3^m), \dots, \phi_V(e_n^m)]$$

$$\text{Get: } H_T, H_A, H_V$$

Equation 6

Attention Weight:

$$a_t = \text{KAN}_t(H_T) a_a = \text{KAN}_a(H_A) a_v = \text{KAN}_v(H_V)$$

Equation 7

$$\alpha_F = \mathbf{w}(\alpha_t + \alpha_a + \alpha_v) + \text{bias}$$

$$\text{Get: } \alpha_F$$

Equation 10

$$\frac{\alpha_t}{\omega_t} + \frac{\alpha_a}{\omega_a} + \frac{\alpha_v}{\omega_v}$$

$$\underbrace{\alpha_F}_{\frac{\alpha_t}{\omega_t} + \frac{\alpha_a}{\omega_a} + \frac{\alpha_v}{\omega_v}} = \underbrace{\phi}_{\frac{\alpha_t}{\omega_t} + \frac{\alpha_a}{\omega_a} + \frac{\alpha_v}{\omega_v}} + \text{bias}$$

$$P'_T = \text{KAN}(\text{Softmax}(\alpha_F) \cdot H_T)$$

$$P'_A = \text{KAN}(\text{Softmax}(\alpha_F) \cdot H_A)$$

$$P'_V = \text{KAN}(\text{Softmax}(\alpha_F) \cdot H_V)$$

Equation 11,12,13

$$\text{Output: } P'_T, P'_A, P'_V$$

Kolmogorov-Arnold Networks

$$P'_T \quad \downarrow$$