





0.95. Optimalna vrednost za potrošnju je  $I_{max} = 3.3 \text{ mA}$

- izračunite povrečni doseg  $\bar{s}$  do punjenja
- Z optimizacijo lahko dosegemo  $H_{L2} = 0.87$ , a se nam zaradi tega dostop do glejega punjenika poveča na 60 ms. Ali je optimizacija smiselna?
- Kakšna bi morala biti vrednost zadetka v L1, da bi pri primeru iz točke b) dosegli  $I_{avg\_accr} = 3.3 \text{ mA}$ ?

a)

$$\begin{aligned} H_{L1} &= 2 \text{ mAh} & H_{L1} &= 0.05 \\ H_{L2} &= 2 \text{ mAh} & H_{L2} &> 0.85 \\ H_{L1} &= 5 \text{ mAh} \\ \therefore t_{avg\_accr} &= \frac{H_{L2} - H_{L1}}{I_{avg\_accr}} \\ &= 2 \text{ mAh} + 0.05 \cdot \left( 20 \text{ mAh} + (0.17 \cdot 0.5 \text{ mAh}) \right) = 3.57 \text{ mAh} \end{aligned}$$

b)

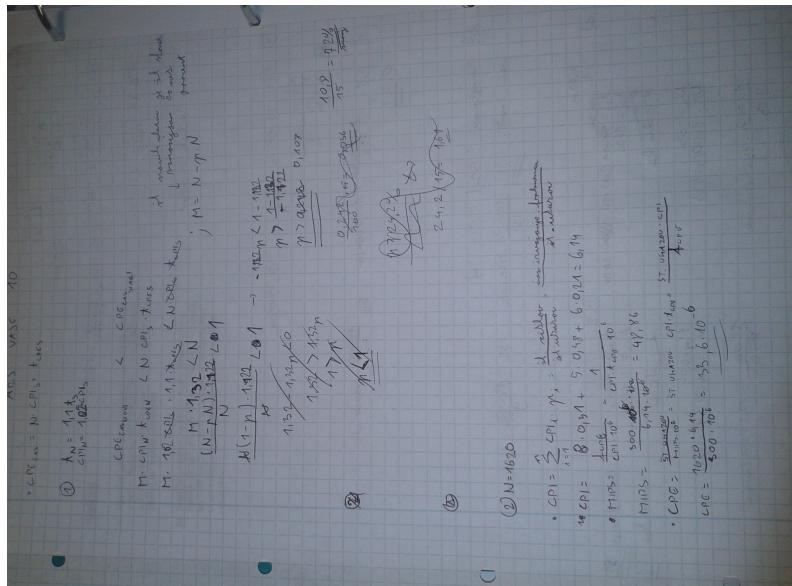
$$\begin{aligned} H_{L2} &= 0.81 & H_{L2} &= 0.19 \\ I_{avg} &= 60 \text{ ms} \\ t_{avg\_accr} &= 2 \text{ mAh} + 0.05 \cdot (20 \text{ mAh} + (0.19 \cdot 0.05)) = 29.8 \text{ mAh} \\ H_{L1} &= 57.15 \text{ mAh} \end{aligned}$$

c)

$$\begin{aligned} 3.3 \text{ mA} &= 2 \text{ mAh} \cdot (1 - H_{L1}) \cdot (20 \text{ mAh} + 0.19 \cdot (0.05)) = \\ 1.3 \text{ mA} &= \frac{3.14 \text{ mAh}}{24.4 - 1.3} = 3.14 \text{ mA} / 23.09 \text{ mA} \\ H_{L1} &= \frac{0.14825}{24.4 - 23.09} \end{aligned}$$







VIS VAE 3

3.1

$$X = \begin{pmatrix} -1 & 0 & 2 \\ 0 & 0.2 & 0.3 \\ 0.1 & 0.1 & 0.3 \end{pmatrix} \sim \mathcal{N}(0, I_3)$$

$$E(X) = 2 = \sum_{\omega} X(\omega) P(X=\omega) = -1(0.4) + 0.02 + 0.1(0.2) + 0.3 = 1.4$$

$$\text{Var}(X) = \sum_{\omega} x^2(\omega) P(X=\omega) - E(X)^2 = (1)^2(0.1) + 0^2(0.2) + 1^2(0.02) + 2^2(0.1) + 0^2(0.3) = 5.2$$

$$E(X^2) = \sum_{\omega} x^2(\omega) P(X=\omega) = 1(0.1) + 0^2(0.2) + 1^2(0.02) + 2^2(0.1) + 0^2(0.3) = 5.2$$

3.2  $E(X) = E(X - E(X))^2 = E(X^2) - E(X)^2$

$$= 3.2 - 1.4^2 = 1.36$$

$$\sigma(X) = \sqrt{\text{Var}(X)} = \sqrt{1.36}$$

3.3  $E(Y) = \int_{\Omega} Y(\omega) P(\omega) d\omega = \int_{\Omega} Y(\omega) d\mu = E(Y)$

3.4  $\mathbb{E}[Y] = \int_{\Omega} Y(\omega) d\mu = \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{4}$

3.5  $P(X=1, Y=0) = \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{4}$

3.6  $P(X=1 | Y=0) = \frac{P(X=1, Y=0)}{P(Y=0)} = \frac{\frac{1}{4}}{\frac{1}{2}} = \frac{1}{2}$

3.7  $E(X^2) = \int_{\Omega} X(\omega)^2 d\mu = \int_{\Omega} \left( \sum_{i=1}^3 a_i \omega_i \right)^2 d\mu = \sum_{i=1}^3 \int_{\Omega} a_i^2 \omega_i^2 d\mu = \sum_{i=1}^3 a_i^2 \cdot \int_{\Omega} \omega_i^2 d\mu =$ 

$$= 6 \left( \frac{1}{2} \right)^2 + 2 \left( \frac{1}{3} \right)^2 = \frac{7}{18}$$

$$E(X^2) - E(X)^2 = \left( \frac{7}{18} \right)^2 - \frac{1}{4} = \frac{49}{324} - \frac{1}{16} = \frac{25}{324} = 0.0773$$

$$\text{Var}(X) = E(X^2) - E(X)^2 = \frac{25}{324} = 0.0773$$

3.8  $\text{Cov}(X, Y) = \text{Cov}(X, X) = E(X^2) - E(X)^2 = \frac{25}{324} = 0.0773$

3.9  $E(X) = \sum_{\omega} X(\omega) P(X=\omega) = \sum_{\omega} X(\omega) \frac{1}{n}$

3.10  $E(X) = \sum_{\omega} X(\omega) \frac{1}{n} = \frac{1}{n} \sum_{\omega} X(\omega)$

3.11  $E(X) = \frac{1}{n} \sum_{\omega} X(\omega) = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \omega_i = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \frac{1}{n} = \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i =$ 

$$= \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i = \frac{1}{n^2} \sum_{i=1}^d \sum_{\omega} a_i = \frac{1}{n^2} \sum_{i=1}^d n a_i = a_i$$

$$= a_i$$

3.12  $E(X) = \sum_{\omega} X(\omega) P(X=\omega) = \sum_{\omega} X(\omega) \frac{1}{n} = \frac{1}{n} \sum_{\omega} X(\omega) = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \omega_i = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \frac{1}{n} = \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i =$ 

$$= \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i = \frac{1}{n^2} \sum_{i=1}^d \sum_{\omega} a_i = \frac{1}{n^2} \sum_{i=1}^d n a_i = a_i$$

3.13  $E(X) = \sum_{\omega} X(\omega) P(X=\omega) = \sum_{\omega} X(\omega) \frac{1}{n} = \frac{1}{n} \sum_{\omega} X(\omega) = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \omega_i = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \frac{1}{n} = \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i =$ 

$$= \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i = \frac{1}{n^2} \sum_{i=1}^d \sum_{\omega} a_i = \frac{1}{n^2} \sum_{i=1}^d n a_i = a_i$$

3.14  $E(X) = \sum_{\omega} X(\omega) P(X=\omega) = \sum_{\omega} X(\omega) \frac{1}{n} = \frac{1}{n} \sum_{\omega} X(\omega) = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \omega_i = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \frac{1}{n} = \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i =$ 

$$= \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i = \frac{1}{n^2} \sum_{i=1}^d \sum_{\omega} a_i = \frac{1}{n^2} \sum_{i=1}^d n a_i = a_i$$

3.15  $X \sim \text{Bin}(n, p)$

$$E(X) = \sum_{\omega} X(\omega) P(X=\omega) = \sum_{\omega} X(\omega) \frac{1}{n} =$$

$$= \dots = \frac{1}{n} \sum_{\omega} X(\omega) = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \omega_i =$$

$$= \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \frac{1}{n} = \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i =$$

$$= \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i = \frac{1}{n^2} \sum_{i=1}^d \sum_{\omega} a_i =$$

$$= \frac{1}{n^2} \sum_{i=1}^d n a_i = a_i$$

3.16  $X \sim \text{Bin}(n, p)$

$$E(X) = \sum_{\omega} X(\omega) P(X=\omega) = \sum_{\omega} X(\omega) \frac{1}{n} =$$

$$= \dots = \frac{1}{n} \sum_{\omega} X(\omega) = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \omega_i =$$

$$= \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \frac{1}{n} = \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i =$$

$$= \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i = \frac{1}{n^2} \sum_{i=1}^d \sum_{\omega} a_i =$$

$$= \frac{1}{n^2} \sum_{i=1}^d n a_i = a_i$$

3.17  $E(X) = \sum_{\omega} X(\omega) P(X=\omega) = \sum_{\omega} X(\omega) \frac{1}{n} = \frac{1}{n} \sum_{\omega} X(\omega) = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \omega_i = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \frac{1}{n} = \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i =$ 

$$= \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i = \frac{1}{n^2} \sum_{i=1}^d \sum_{\omega} a_i =$$

$$= \frac{1}{n^2} \sum_{i=1}^d n a_i = a_i$$

3.18  $E(X) = \sum_{\omega} X(\omega) P(X=\omega) = \sum_{\omega} X(\omega) \frac{1}{n} = \frac{1}{n} \sum_{\omega} X(\omega) = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \omega_i = \frac{1}{n} \sum_{\omega} \sum_{i=1}^d a_i \frac{1}{n} = \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i =$ 

$$= \frac{1}{n^2} \sum_{\omega} \sum_{i=1}^d a_i = \frac{1}{n^2} \sum_{i=1}^d \sum_{\omega} a_i =$$

$$= \frac{1}{n^2} \sum_{i=1}^d n a_i = a_i$$

Nachtrag  
 $\begin{pmatrix} 1 & 1 \end{pmatrix}$  - eine 2x2-matrix, die die einzelnen Beobachtungen und geschätzten  
 erwarteten Positionen darstellen kann.

$$\text{① } \sum_{i=1}^n \frac{\partial}{\partial x_i} \left( \frac{1}{2} \|y_i - \hat{y}_i\|^2 \right) = \sum_{i=1}^n (y_i - \hat{y}_i) \cdot \frac{\partial}{\partial x_i} (\hat{y}_i) = \sum_{i=1}^n (y_i - \hat{y}_i) \cdot b_i = 0 \quad \text{aufgrund der Linearität der Ableitung}$$

$$\hat{y}(x) = D(x) \cdot b = D(x) \cdot \begin{pmatrix} 1 \\ 1 \end{pmatrix} = D(x) \cdot \begin{pmatrix} 1 & 1 \end{pmatrix}^T$$

$$e(x, y) = y - \hat{y}(x) = y - D(x) \cdot \begin{pmatrix} 1 & 1 \end{pmatrix}^T$$

$$C_{xy}(x) = E[e(x)e(x)^T]$$

$$= E[y^2] - E[e(x)]^2$$

$$= E[y^2] - D(x) \cdot \begin{pmatrix} 1 & 1 \end{pmatrix}^T \cdot D(x)$$

$$= E[y^2] - D(x) \cdot D(x)^T$$

$$= E[y^2] - D(x) \cdot D(x)^T$$