

```
clear all
load RSS
plot(RSS)
plot(d)
y = RSS';
d = d';
```

Part a

```
% model is  $RSS = 2A + B/2 \ln(d) + v_k$ 
%  $v_k \sim N(0, 5^2)$ 
%  $[A; B] \sim N([10; -20], 20 \cdot I)$ 

%this is linear fitting problem  $y = H \cdot \theta + \epsilon_k$ ,
% where
%  $y = RSS$ 
%  $H = [2, \ln(d)/2]$ 
%  $\theta = [A; B]$ 
%  $\epsilon_k = v_k$ 

%lets solve this problem, using model codes from exercise 2
H=[2*ones(size(d)) log(d)/2];
m0=[10;-20];
P0=20*eye(2);
R=5^2*eye(80);
```

The posterior mean and covariance computed with the formulas of slide 2.11 are

```
K=P0*H'*inv(H*P0*H'+R);
mT=m0+K*(y-H*m0)
```

```
mT = 2x1
    11.1892
   -18.2031
```

```
PT=P0-K*H*P0
```

```
PT = 2x2
    3.9228   -3.0833
   -3.0833    2.4725
```

```
%seems that posterior for
% A = 11.1892
% B = -18.2031
```

```
%Confidence interval 95%
%A
```

```
A_CI95 = [mT(1)-1.96*sqrt(PT(1,1)),mT(1)+1.96*sqrt(PT(1,1))]
```

```
A_CI95 = 1x2
    7.3073    15.0712
```

```
%B
```

```
B_CI95 = [mT(2)-1.96*sqrt(PT(2,2)),mT(2)+1.96*sqrt(PT(2,2))]
```

```
B_CI95 = 1x2
        -21.2851  -15.1212
```

```
% plot to clarify if result is somehow correct
plot(log(d),y, '.',log(d),2*mT(1)+mT(2)*log(d)/2, '-');
legend('Measurement', 'Estimate');
```

Part b

```
%code taken from linreg_mcmc.m
% Gradient-free optimisation
logmvnpdf=@(x,m,P) -0.5*(x-m)'/P*(x-m)-trace(log(chol(2*pi*P)));
phiT=@(th) -logmvnpdf(y,H*th,R)-logmvnpdf(th,m0,P0);

% Robust Adaptive Metropolis algorithm
Sigma=eye(2)*0.002;
Nburnin=1500; %CHANGED
N=15000;      %CHANGED
gamma=0.9;
alpha_target=0.234;
theta=zeros(2,N);
accept_count=0;
theta_prev=mvnrnd(m0,P0)';
phi_prev=phiT(theta_prev);
S=chol(Sigma, 'lower');
for i=1:N
    r=randn(size(m0));
    theta_prop=theta_prev+S*r;
    phi_prop=phiT(theta_prop);
    alpha=min(1,exp(phi_prev-phi_prop));
    if alpha>=rand
        accept_count=accept_count+1;
        theta(:,i)=theta_prop;
        theta_prev=theta_prop;
        phi_prev=phi_prop;
    else
        theta(:,i)=theta_prev;
    end
    if i>Nburnin
        eta=1/(i-Nburnin)^gamma;
        u=r/norm(r);
        SS=S*(eye(size(S))+eta*(alpha-alpha_target)*(u*u'))*S';
        S=chol(SS, 'lower');
    end
end
disp('Robust Adaptive Random-walk Metropolis')
```

```
Robust Adaptive Random-walk Metropolis
```

```
mMCMC=mean(theta(:,Nburnin:end),2)
```

```
mMCMC = 2x1
        11.3865
```

-18.3650

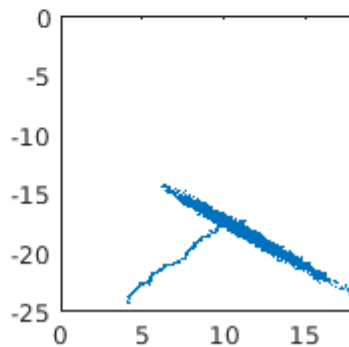
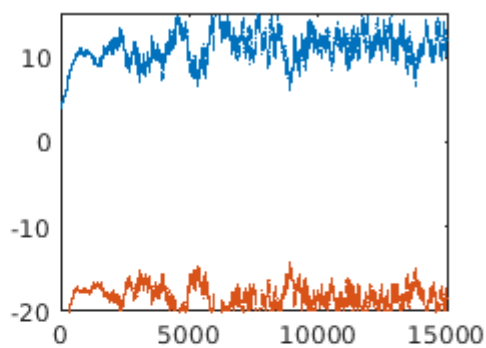
```
Pmcmc=cov(theta(:,Nburnin:end)')
```

```
Pmcmc = 2x2  
    3.1746   -2.4852  
   -2.4852    1.9933
```

```
accept_rate=accept_count/N
```

```
accept_rate = 0.6429
```

```
subplot(222)  
plot(1:N,theta,',' , 'markersize',1)  
axis([0 N -20 15]) %CHANGED  
subplot(224)  
plot(theta(1,:),theta(2,:),',' , 'markersize',1)  
axis([0 18 -25 0]), axis square %CHANGED
```



```
%seems that posterior for  
% A  
A_MCMC = mMCMC(1)
```

```
A_MCMC = 11.3865
```

```
% B  
B_MCMC = mMCMC(2)
```

```
B_MCMC = -18.3650
```

```
%Confidence interval 95%
```

```
% A
```

```
A_MCMC_CI95 = quantile(theta(1,:),[0.025 0.975])
```

```
A_MCMC_CI95 = 1x2  
    7.1760    14.8893
```

```
% B
```

```
B_MCMC_CI95 = quantile(theta(2,:),[0.025 0.975])
```

```
B_MCMC_CI95 = 1x2  
   -21.7823   -15.7825
```