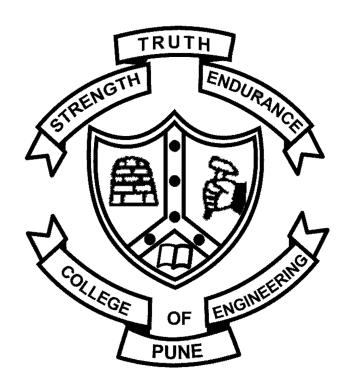
DTL Assignment 3 - Include Graphics and Tables

Avdhut Kamble



January 18, 2023

1 LAUC Syllabus

1.1 Unit 1

- 1. Linear Algebra
- 2. Vector Spaces
- 3. Differential Equations

1.2 Unit 2

- 1. Laplace Inverse Transform
- 2. Transfer Function
- 3. Time Domain Analysis

1.3 Unit 3

- 1. Functions of several variables
- 2. Level curves and level surfaces
- 3. Partial and directional derivatives

College of Engineering, Pune.

B.Tech II Year

November 2022, Odd Semester

Linear Algebra and Uni-variate Calculus TEST - 1

Duration-1.5 hours

Marks 30

Q.1) Solve the following:

(a)
$$3x(xy-2)dx + (x^3+2y)dy = 0$$
 [CO 2] [2]

(b)
$$(2\cos y + 4x^2)dx - x\sin ydy == 0$$
 [CO 2] [3]

Q.2) Prove the following matrices equal if $AB = A^T . B^T$. [CO 1] [1]

$$B_{m \times n} = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \cdots & a_{mn} \end{bmatrix}$$

$$A_{m \times n} = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{nn} & a_{nn} & \cdots & a_{nn} \end{bmatrix}$$

Q.3)State whether the following differential equations are linear or non linear ,justify and solve:

(a)
$$xy' + 2y = \frac{e^{3x}}{x}, x > 0$$
with $y(1) = 1 + \frac{e^3}{3}$. [CO 2] [3]

(b)
$$x^2 y \frac{dy}{dx} - xy^2 = 1$$
 [CO 2] [3]

Q.4) If x^2 and 1 are solutions of yy'' - xy' = 0 then so is any linear combination of these. State true or false and justify. [CO 4] [2]

Q.5) Find a linear ordinary differential equation for which the function $e^{-x}\cos 2x$ and $e^{-x}\sin 2x$ are linearly independent solutions. [CO 2] [3]

Q.6) Solve the given equation of form AX = B

$$A = \begin{pmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \\ 1 & 4 & 7 \end{pmatrix}, X = \begin{pmatrix} x \\ y \\ z \end{pmatrix} B = \begin{pmatrix} 6 \\ 14 \\ 30 \end{pmatrix}$$

 $\mathbf{Q}.7)$ Show that the following matrix is diagonalizable:

$$A = \begin{pmatrix} 1 & 0 & 1 \\ 1 & 2 & 1 \\ 2 & 2 & 3 \end{pmatrix}$$

2 Table from raw values

Table 1: Price of stationary

Sr. no.	${\bf Item}$	Price
1	Pencil	20
2	Pen	40
3	Notebook	50
4	Writing Pad	60
5	Bag	10

3 Include table from CSV

Name	Age	College
142203001	Avdhut	SY 5
142203002	Test 1	SY 6
142203003	Test2	SY 7
142203004	Test 3	SY 8
142203005	Test 4	SY 9
142203006	Test 5	SY 10
142203007	Test 6	SY 11
142203008	Test 7	SY 12
142203009	Test 8	SY 13
142203010	Test 9	SY 14
142203011	Test 10	SY 15
142203012	Test 11	SY 16
142203013	Test 12	SY 17
142203014	Test 13	SY 18
142203015	Test 14	SY 19
142203016	Test 15	SY 20
142203017	Test 16	SY 21
142203018	Test 17	SY 22