

DATA SCIENCE

LECTURE 4: K-NEAREST NEIGHBORS CLASSIFICATION

YUCHEN ZHAO / DAT-14

RECAP

LAST TIME:

I. DATA RETRIEVAL (API, JSON)

II. ETL INTRO (DATABASE)

III. VISUALIZATION (D3.JS)

EXERCISES:

IV. PANDAS

V. MINING TWITTER VIA API

QUESTIONS?

I. CLASSIFICATION PROBLEMS

II. BUILDING EFFECTIVE CLASSIFIERS

EXERCISES:

III. THE KNN CLASSIFICATION MODEL

I. CLASSIFICATION PROBLEMS

	<i>continuous</i>	<i>categorical</i>
<i>supervised</i>	???	???
<i>unsupervised</i>	???	???

	<i>continuous</i>	<i>categorical</i>
<i>supervised</i>	<i>regression</i>	<i>classification</i>
<i>unsupervised</i>	<i>dimension reduction</i>	<i>clustering</i>

Here's (part of) an example dataset:

Fisher's *Iris* Data

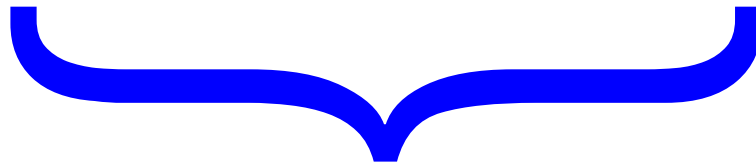
Sepal length ⇅	Sepal width ⇅	Petal length ⇅	Petal width ⇅	Species ⇅
5.1	3.5	1.4	0.2	<i>I. setosa</i>
4.9	3.0	1.4	0.2	<i>I. setosa</i>
4.7	3.2	1.3	0.2	<i>I. setosa</i>
4.6	3.1	1.5	0.2	<i>I. setosa</i>
5.0	3.6	1.4	0.2	<i>I. setosa</i>
5.4	3.9	1.7	0.4	<i>I. setosa</i>
4.6	3.4	1.4	0.3	<i>I. setosa</i>
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*independent
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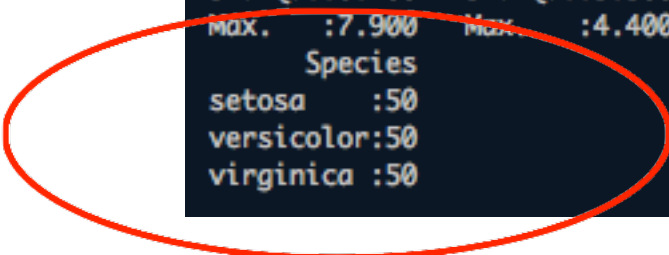
*class
labels
(qualitative)*

Q: What does “supervised” mean?

Q: What does “supervised” mean?

A: We know the labels.

```
Welcome to R! Thu Feb 28 13:07:25 2013
> summary(iris)
  Sepal.Length Sepal.Width Petal.Length Petal.Width
Min.   :4.300   Min.   :2.000   Min.   :1.000   Min.   :0.100
1st Qu.:5.100   1st Qu.:2.800   1st Qu.:1.600   1st Qu.:0.300
Median :5.800   Median :3.000   Median :4.350   Median :1.300
Mean   :5.843   Mean   :3.057   Mean   :3.758   Mean   :1.199
3rd Qu.:6.400   3rd Qu.:3.300   3rd Qu.:5.100   3rd Qu.:1.800
Max.   :7.900   Max.   :4.400   Max.   :6.900   Max.   :2.500
 Species
setosa   :50
versicolor:50
virginica :50
```



Q: How does a classification problem work?

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A: Data in, predicted labels out.

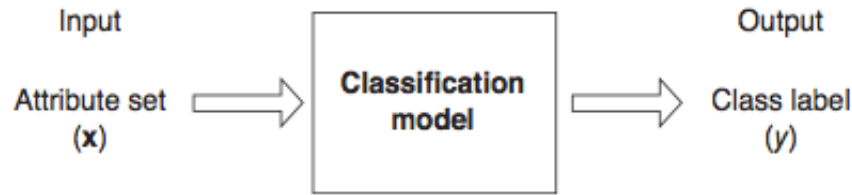
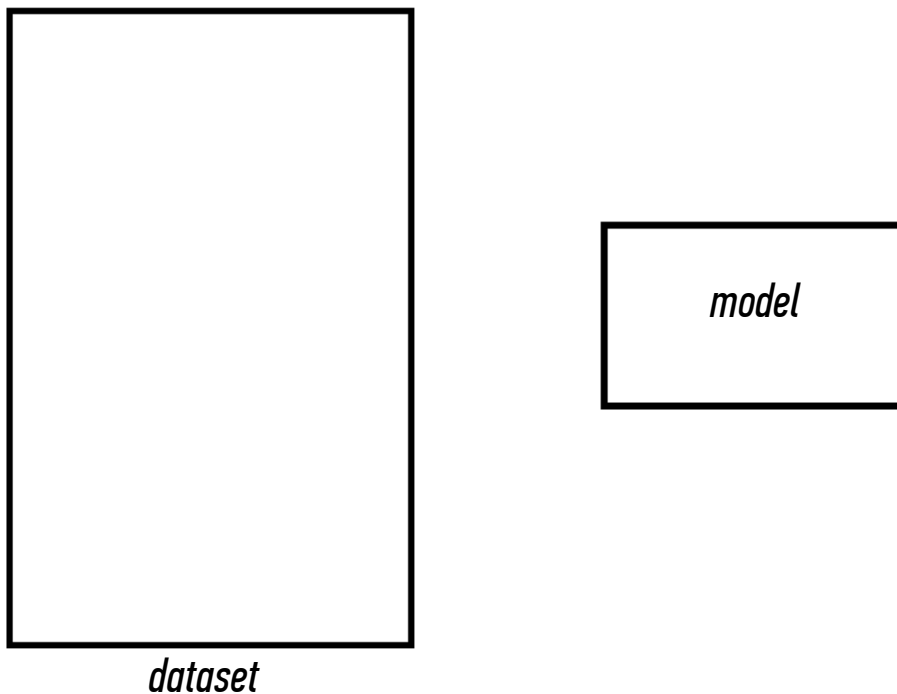


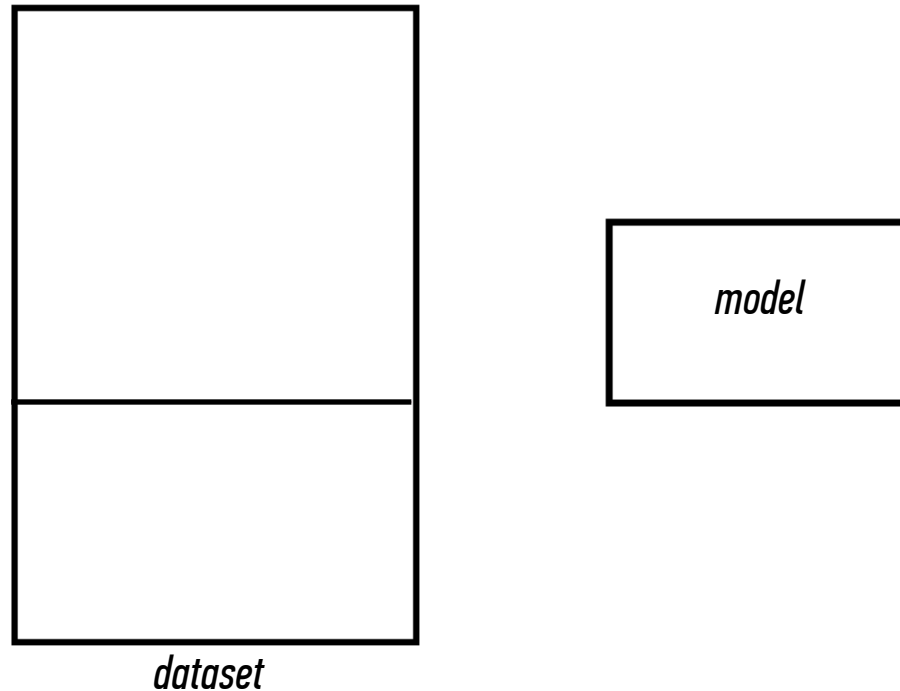
Figure 4.2. Classification as the task of mapping an input attribute set x into its class label y .

Q: What steps does a classification problem require?



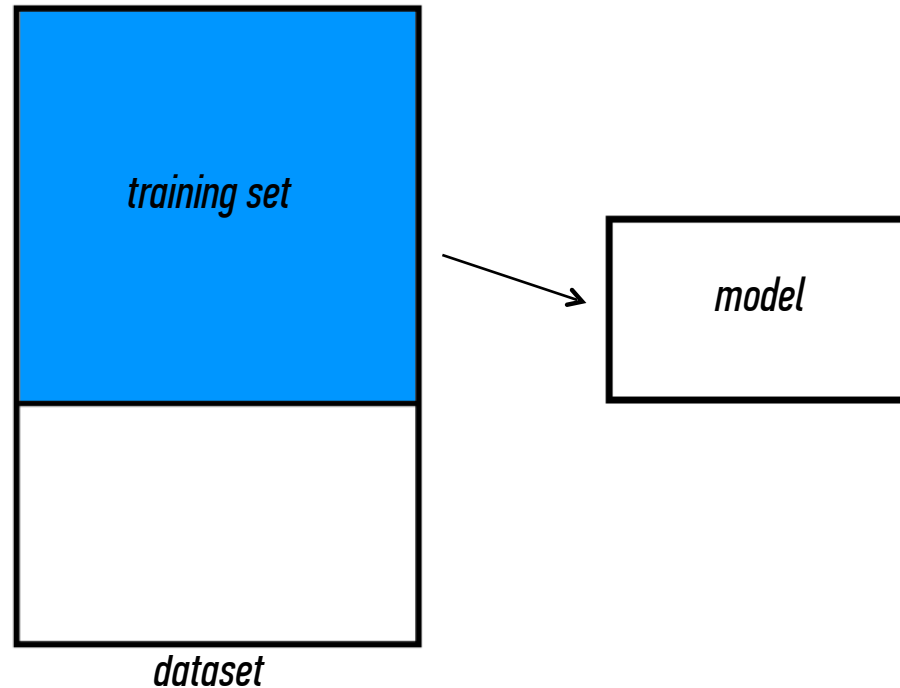
Q: What steps does a classification problem require?

1) split dataset



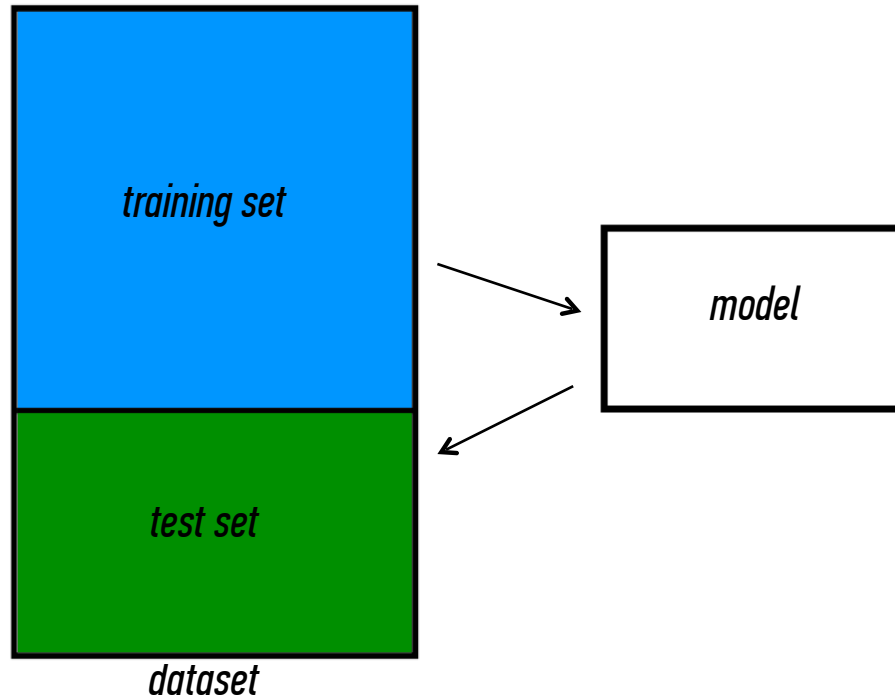
Q: What steps does a classification problem require?

- 1) split dataset*
- 2) train model*



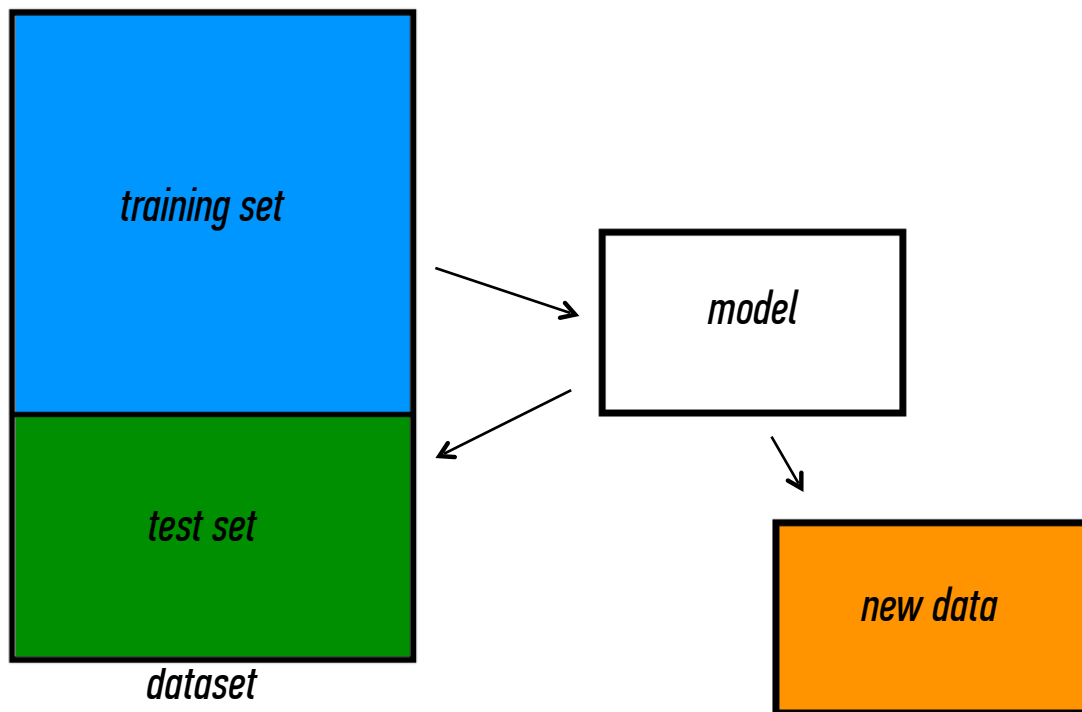
Q: What steps does a classification problem require?

- 1) split dataset*
- 2) train model*
- 3) test model*



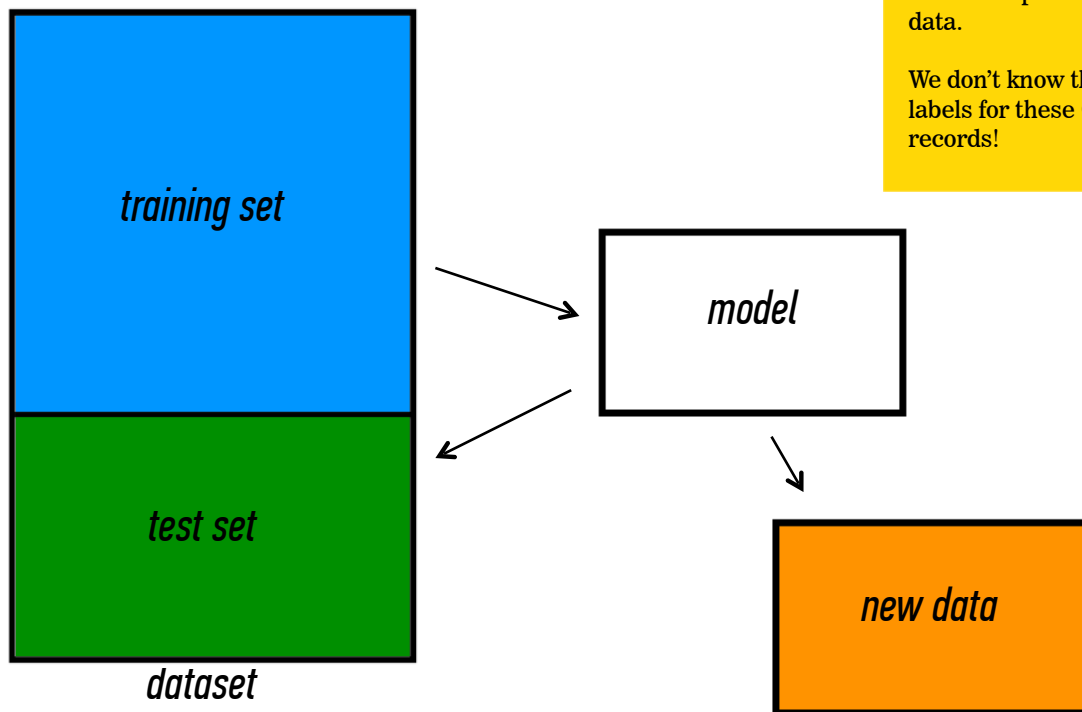
Q: What steps does a classification problem require?

- 1) split dataset*
- 2) train model*
- 3) test model*
- 4) make predictions*



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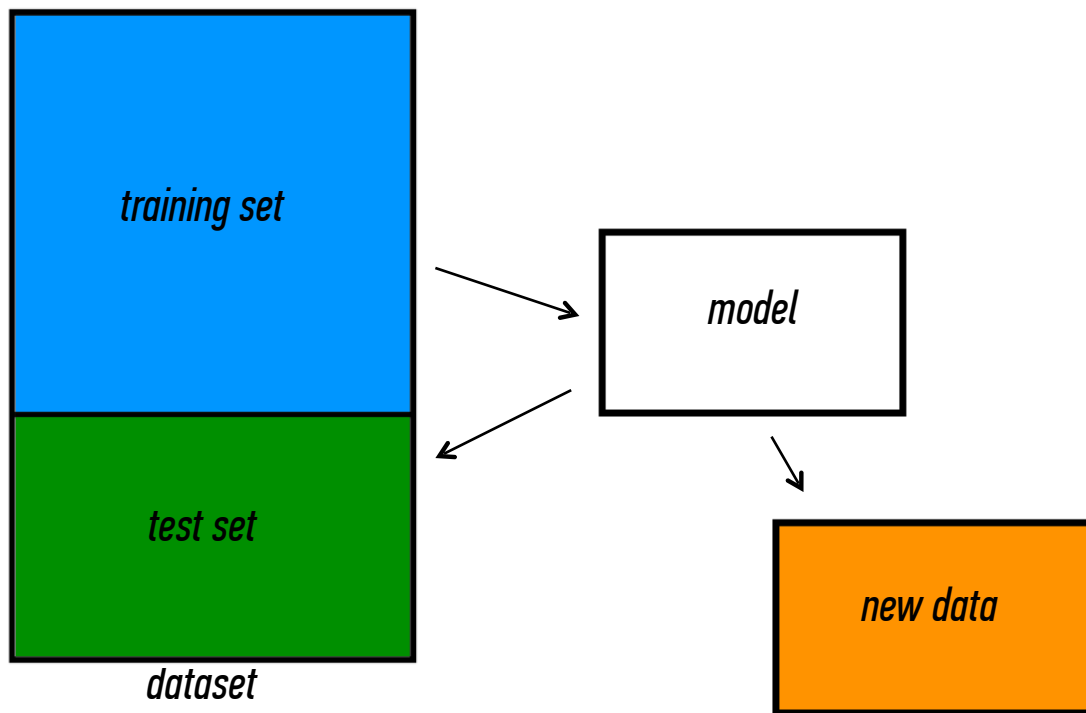
NOTE

This new data is called out of sample data.

We don't know the labels for these OOS records!

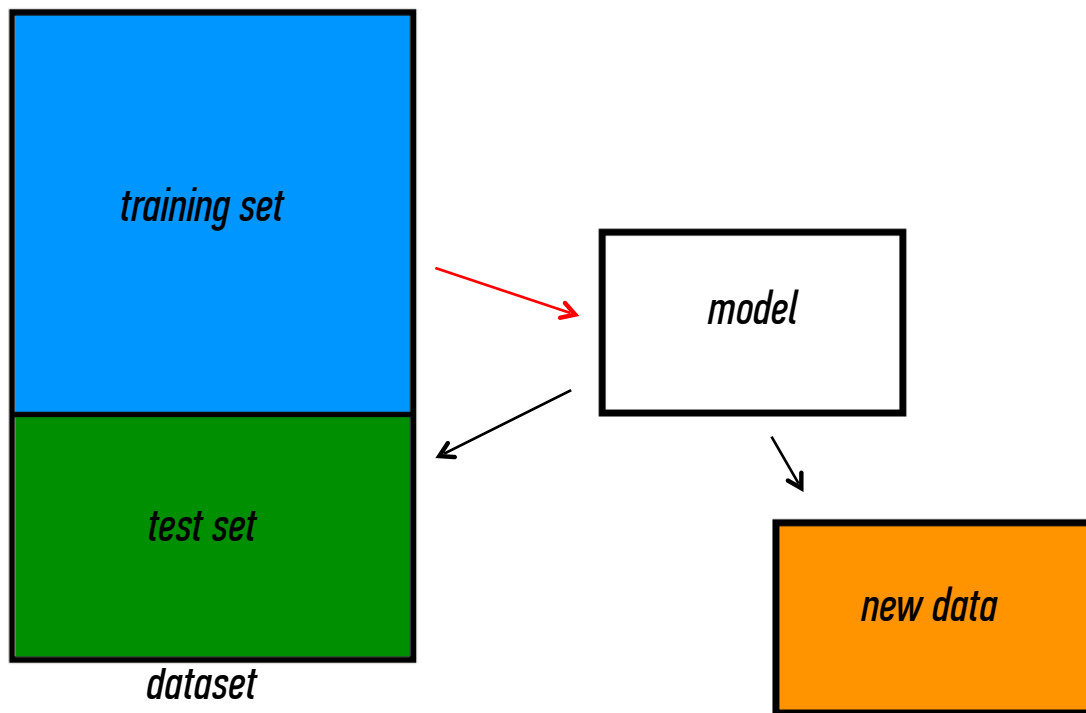
II. BUILDING EFFECTIVE CLASSIFIERS

Q: What types of prediction error will we run into?



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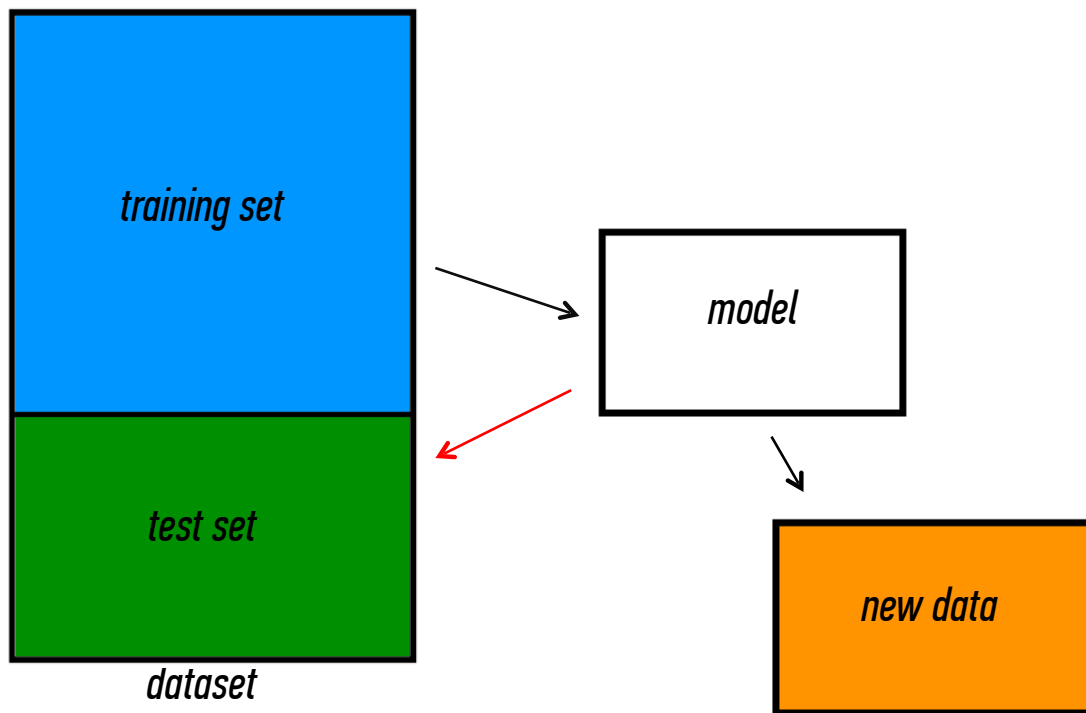
1) training error



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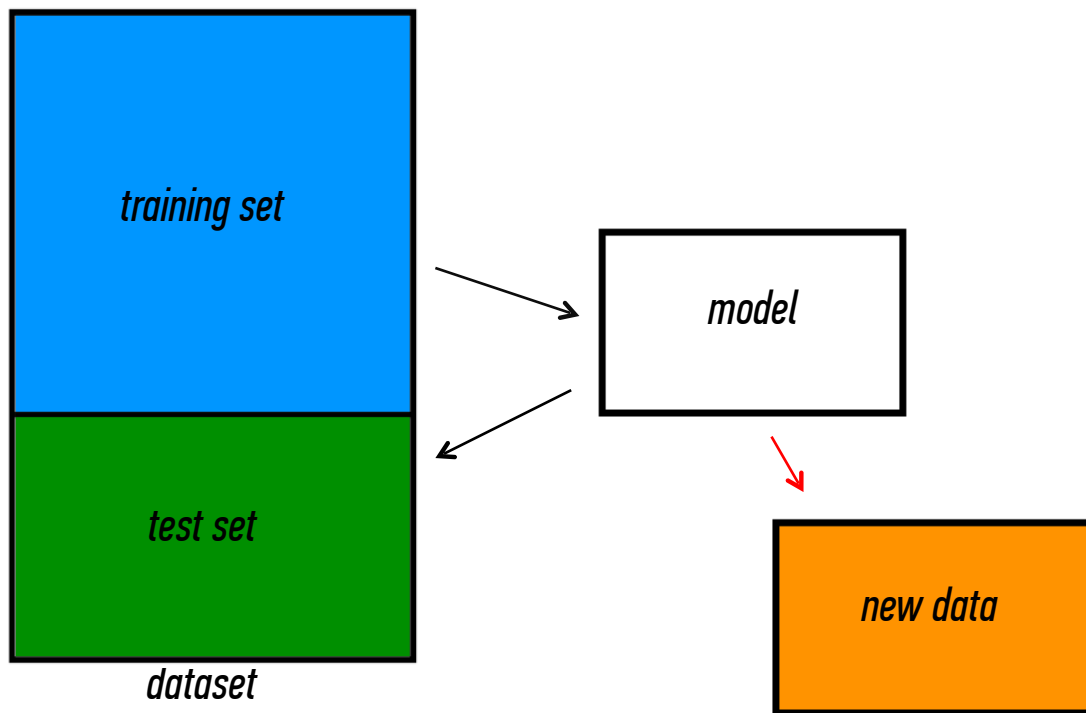
- 1) *training error*
- 2) *generalization error*

NOTE
measures how
well a learning
machine
generalizes to
unseen(test) data



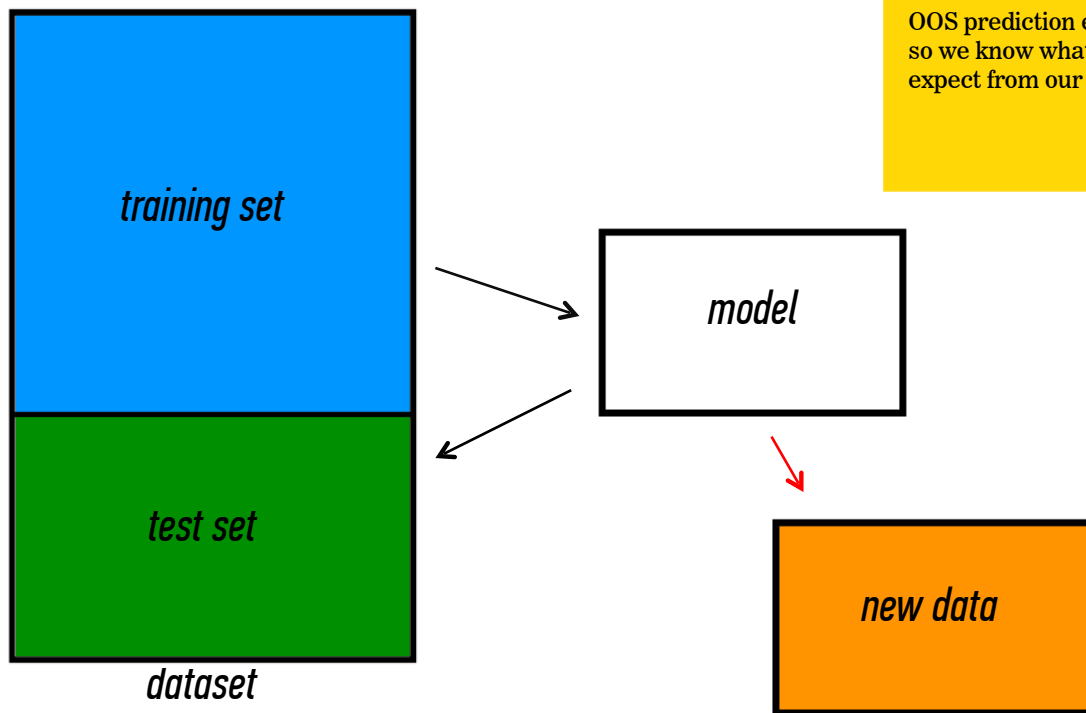
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- 3) *OOS error*



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NOTE

We want to estimate OOS prediction error so we know what to expect from our model.

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TRAINING ERROR

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Thought experiment:

Suppose instead, we train our model using the entire dataset.

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NOTE

This phenomenon is called overfitting.

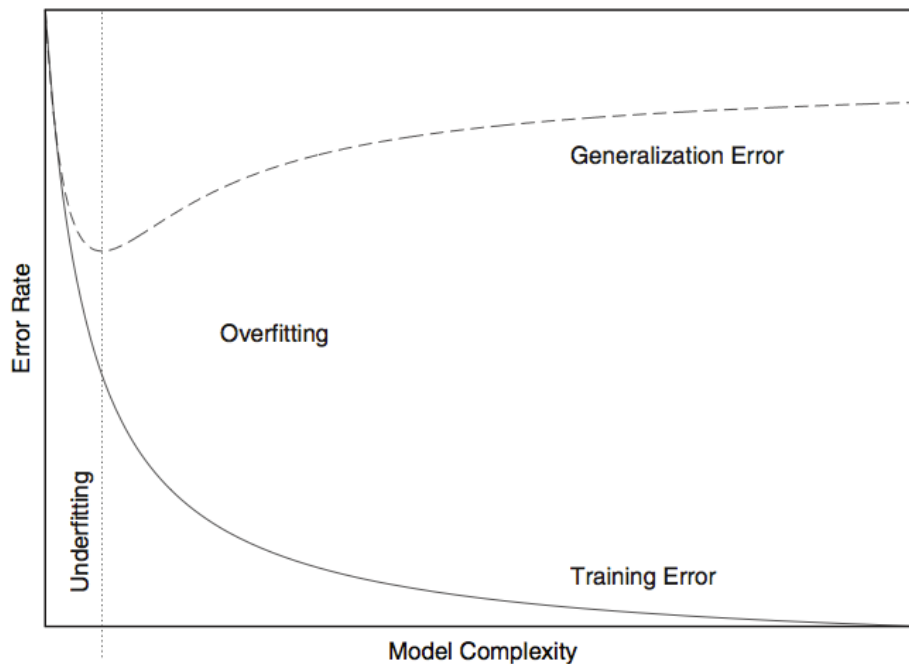
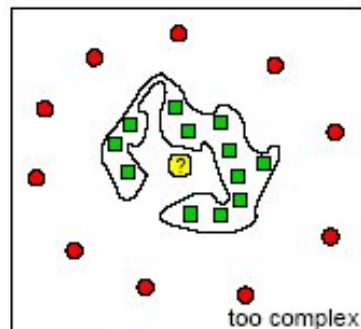
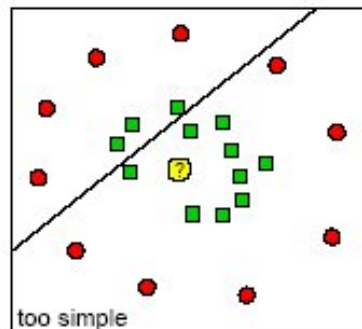


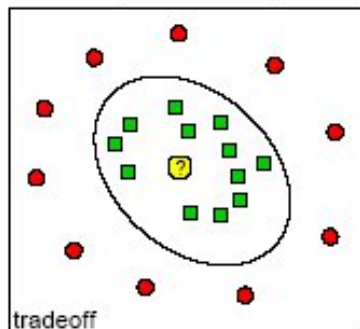
FIGURE 18-1. Overfitting: as a model becomes more complex, it becomes increasingly able to represent the training data. However, such a model is overfitted and will not generalize well to data that was not used during training.

OVERFITTING - EXAMPLE

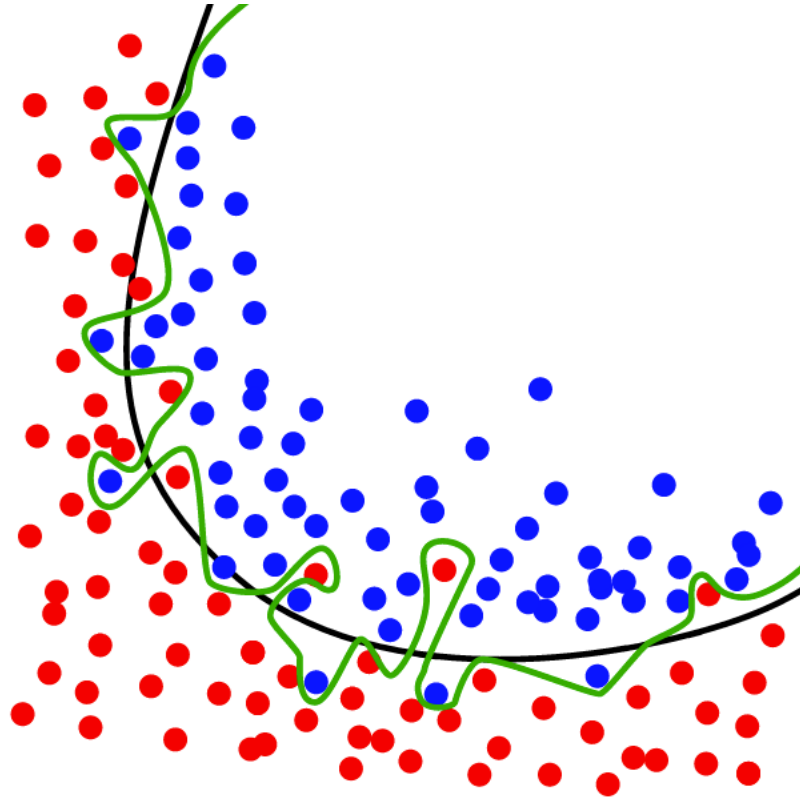
Underfitting and Overfitting



- negative example
- positive example
- new patient



OVERFITTING - EXAMPLE



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A: Down to zero!

A: Training error is not a good estimate of OOS accuracy.

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GENERALIZATION ERROR

Suppose we do the train/test split.

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Q: How well does generalization error predict OOS accuracy?

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A: On its own, not very well.

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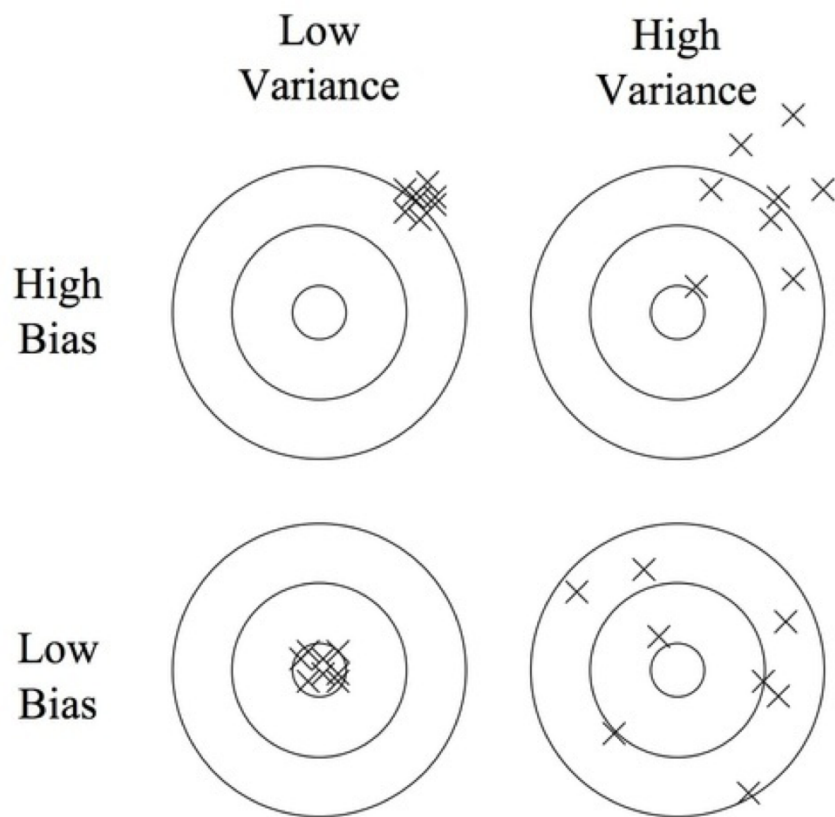
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A: Of course not!

A: On its own, not very well.

NOTE

The generalization error gives a high-variance estimate of OOS accuracy.



Something is still missing!

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Different train/test splits will give us different generalization errors.

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A: Cross-validation.

CROSS-VALIDATION

Steps for n -fold cross-validation:

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- 5) Take the average generalization error as the estimate of OOS accuracy.*

CROSS-VALIDATION: 5-FOLD EXAMPLE

Dataset	Fold 1	Fold 2	Fold 3	Fold 4	Fold 5	<u>Accuracy</u>
1	Test	Train	Train	Train	Train	$k_1 \%$
2	Train	Test	Train	Train	Train	$k_2 \%$
3	Train	Train	Test	Train	Train	$k_3 \%$
4	Train	Train	Train	Test	Train	$k_4 \%$
5	Train	Train	Train	Train	Test	$k_5 \%$

overall accuracy: $(k_1 + k_2 + k_3 + k_4 + k_5) / 5$

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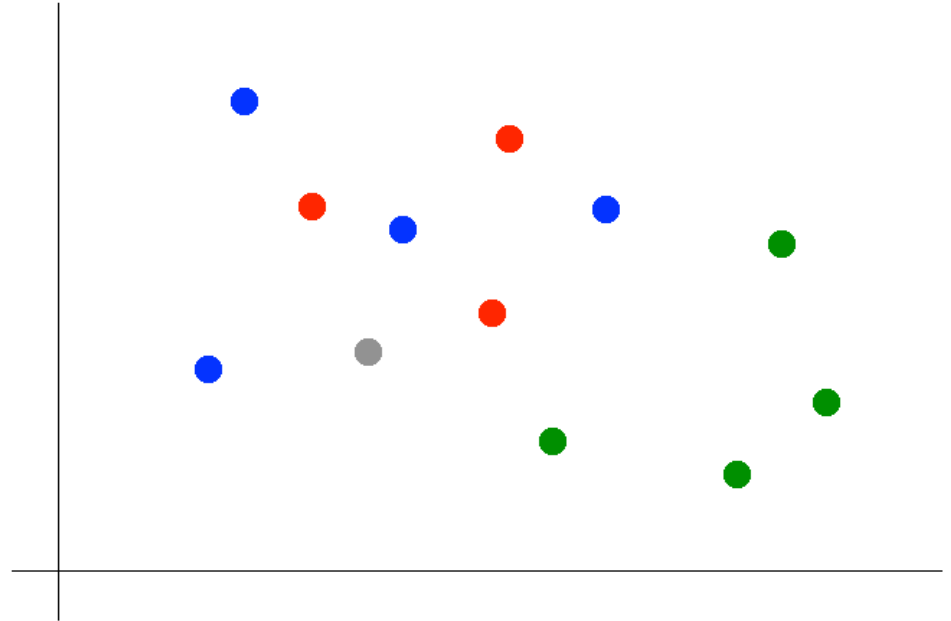
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 - 10-fold CV is 10x more expensive than a single train/test split*

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- 3) Presents tradeoff between efficiency and computational expense.*
 - 10-fold CV is 10x more expensive than a single train/test split*
- 4) Can be used for model selection.*

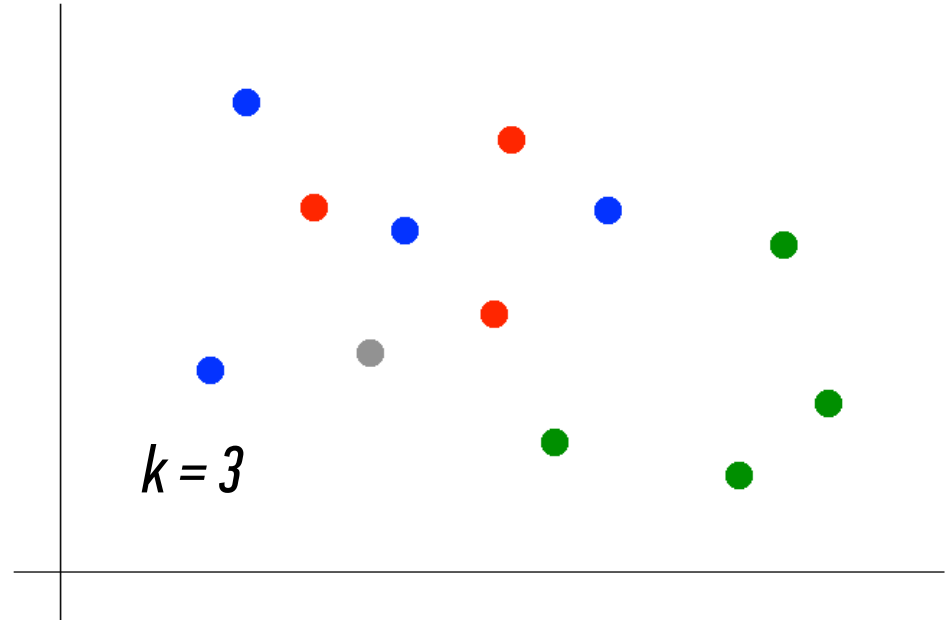
III. KNN CLASSIFICATION

Suppose we want to predict the color of the grey dot.



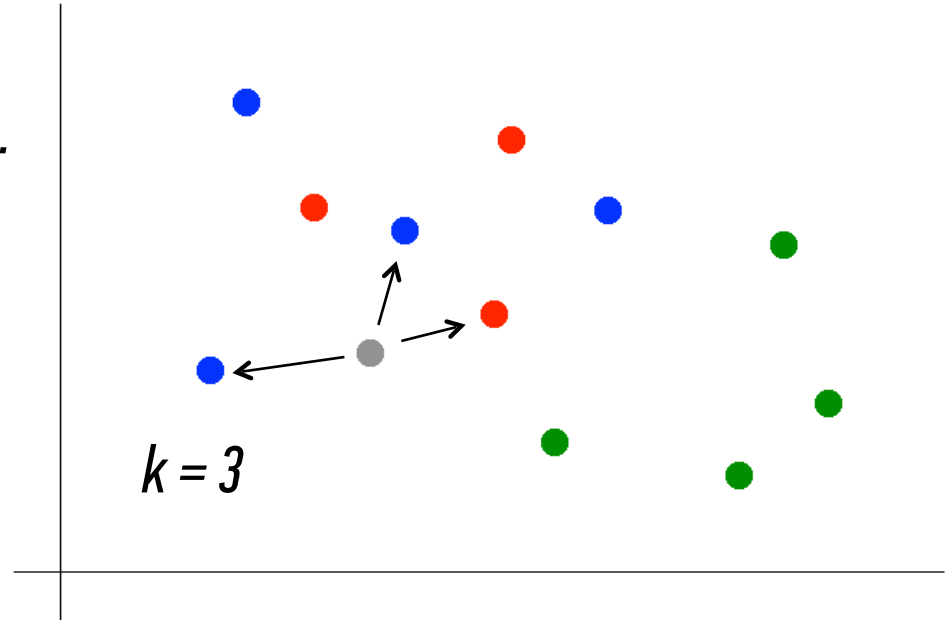
Suppose we want to predict the color of the grey dot.

1) Pick a value for k .



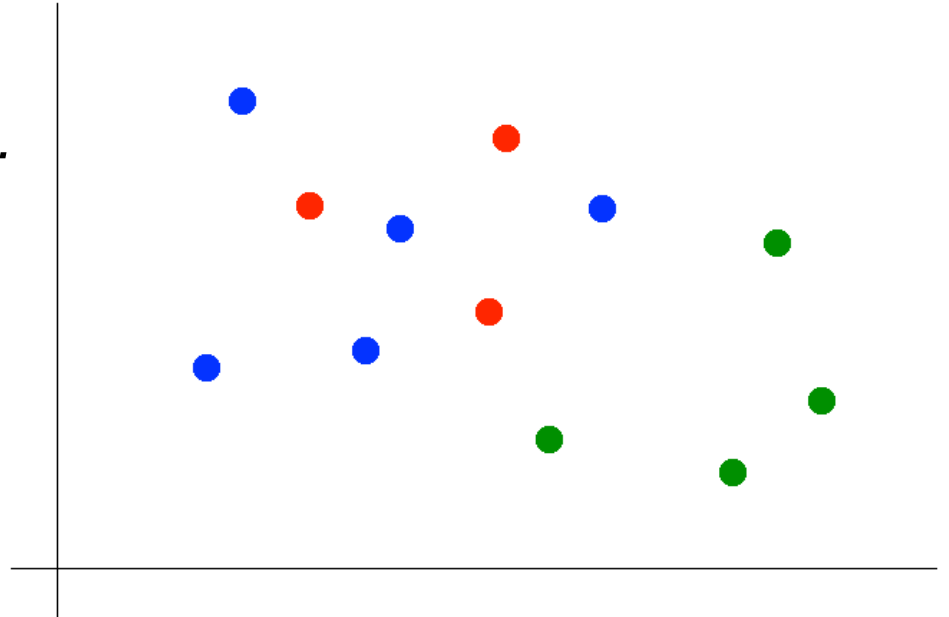
Suppose we want to predict the color of the grey dot.

- 1) Pick a value for k .*
- 2) Find colors of k nearest neighbors.*



Suppose we want to predict the color of the grey dot.

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- 3) Assign the most common color to the grey dot.*

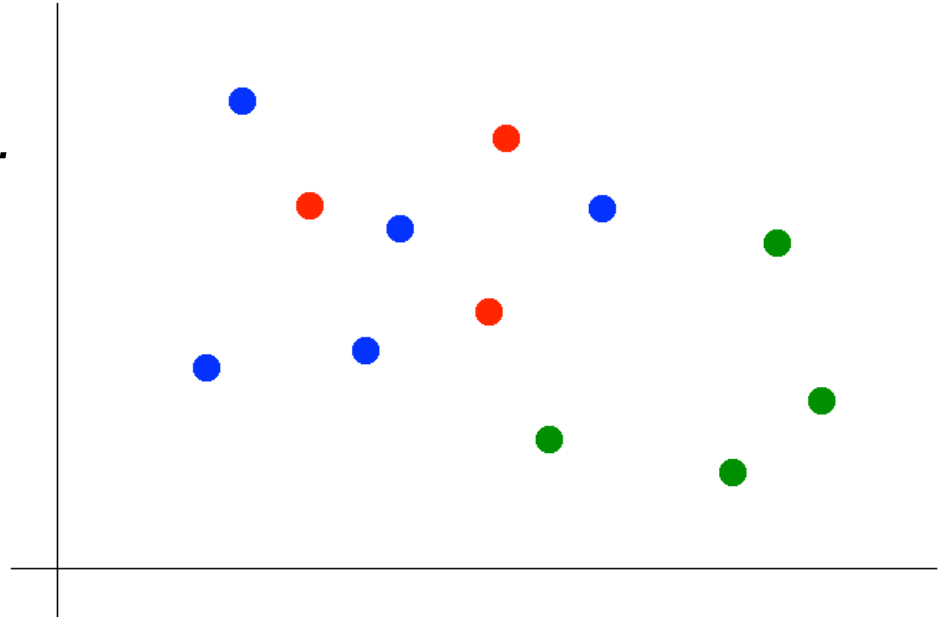


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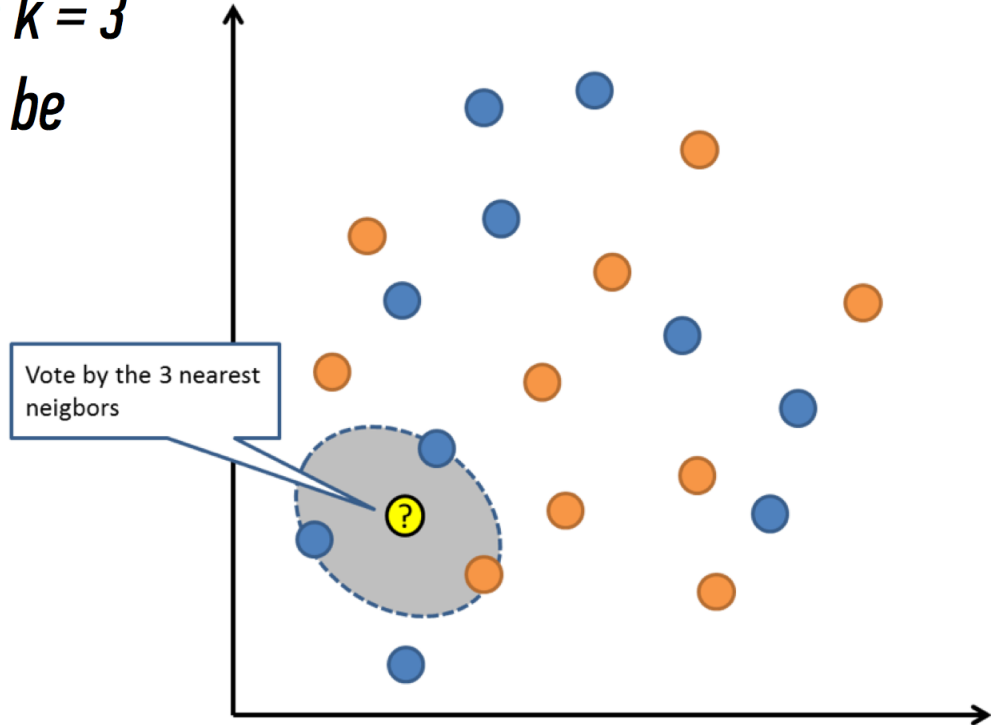
- 1) Pick a value for k .*
- 2) Find colors of k nearest neighbors.*
- 3) Assign the most common color to the grey dot.*

OPTIONAL NOTE

Our definition of “nearest” implicitly uses the Euclidean distance function.



*Another example with $k = 3$
Will our new example be
blue or orange?*



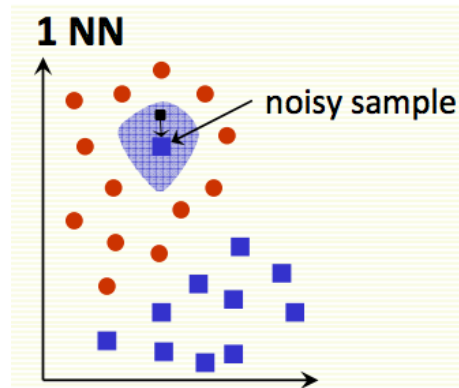
*In theory, if **infinite** number of samples available, the larger is k , the better is classification*

The caveat is that all k neighbors have to be close

- Possible when infinite # samples available*
- Impossible in practice since # samples is finite*

Rule of thumb is $k < \sqrt{n}$, n is number of examples

- interesting theoretical properties*
- In practice, $k = 1$ is often used for efficiency, but can be sensitive to “noise”*



KNN CLASSIFICATION - HOW TO CHOOSE K?

*larger k may improve performance, but too large k destroys locality,
i.e. end up looking at samples that are not neighbors*

cross-validation may be used to choose k

KNN CLASSIFICATION SUMMARY

Advantages

- *Can be applied to the data from any distribution*
- *Very simple and intuitive*
- *Good classification if the number of samples is large enough*

Disadvantages

- *Choosing k may be tricky*
- *Test stage is computationally expensive (no training stage)*
- *Need large number of samples for accuracy*

INTRO TO DATA SCIENCE

LAB