

Basic non-life insurance formulary

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1 Introduction

This basic non-life insurance formulary is to help to understand what are the key facts used in calculating the premium in insurance contracts as well as to show what are the key measures used to analyse of the insurance business. The focus is on pricing calculations. The whole formulary is build on step-by-step approach. In each section some new definitions are introduced, accompanied by their formulas and then the ongoing example is used to illustrate the theory.

2 The story

Assume the following situation: you have 5 friends, with each owning a car. They have approximately the same car, and their driving behaviour is pretty the same, as they are siblings. As none of them wants to be left out in the rain, in case of an car accident, they decide to share the risk and to buy an insurance policy. Your task is to define the price for their insurance give the following information:

- 5 cars
- each cars' new market value is 10.000
- you estimate, that probability to have an accident is equal to 40 percent
- you know that the average size of claim for such cars is 2500 euro
- you face operating expenses of 100 euro per policy
- due to reduce your risk, you decide to reinsure your policies for claims that are higher than 10000 euro. Reinsurance costs per policy are 150 euro
- your goal is to earn 50 euro profit per policy (to cover your alternative capital income costs of putting your money into a bank account)

3 Time

Any time spot is denoted with a letter t , whereas the subscript of t denotes the exact time spot. There are 4 main time spots: the date of policy issue, the date of policy begin, the date of regular policy end and in some cases, the date of policy cancellation. Though some insurers take it very exactly in using using hours in addition to the date, in most cases such precision is not necessary.

- t_I - is the date of policy issue. This date is important as it is the basic date for any policy duration calculation.
- t_S - is the date when the policy takes effect.
- t_E - is the agreed date when the policy expires. This date is the usual expiration date of the insurance.
- t_C - is the premature date of expiration on behalf of insurance company or the policy holder. If for example the policy holder dies, or the insured object is destroyed due to an unforeseen event, or other reasons, the insurance contract might get canceled.

- t_T - is the date of insurance termination, either the end date of insurance or the date of its cancelation. It is the minimum (see 4.2) of these two dates and can be mathematically described as

$$t_T = \min(t_E, t_C)$$

- t_A - is the actual date of calculation. In this example, it is set to 2017.07.15, so t_A is equivalent to $t_{(2017.07.15)}$

Lets asume the the first customer signs his policy (P_A) signs the insurance contract on 2017.01.01 with the start date of 20017.01.01 and the end date of 2017.12.31. The second customer signs the contract on 2017.01.01 with the insurance start date of 2017.01.01, insurence end date of 2017.12.31, but whose policy is canceled on 2017.05.10. The third customer signs his contract on 2017.10.01, with contract start date 2017.01.01 and contract end date 2017.12.31. The fourth customer signs the contract on 2017.02.01, with insuracne begin on 2017.03.01 and insurance contract end on 2017.09.30 whereas the last customer signs the contract on 207.12.31 with the insurance start date of 2017.01.01 but cancels the insurance before it begins, so the cancel date is also the 2017.01.01.

Having all this information, we can construct the folloing table:

Table 1: Basic insurance date information

Attribute	P_A	P_B	P_C	P_D	P_E
t_I (Issue date)	2017.01.01	2017.01.01	2016.10.01	2017.02.01	2017.12.31
t_S (Policy start date)	2017.01.01	2017.01.01	2017.01.01	2017.03.01	2017.01.01
t_C (Policy cancellation date)		2017.05.10	2017.11.10		2017.01.01
t_E (Policy end date)	2017.12.31	2017.12.31	2017.12.31	2017.09.30	2017.12.31
t_T (Policy termination date)	2017.12.31	2017.05.10	2017.11.10	2017.09.30	2017.01.01
t_a (Today, as of 2017-07-15)	2017.07.15	2017.07.15	2017.07.15	2017.07.15	2017.07.15

Data in this table can be used to calculate the folloing policy metrics:

- **IY** (Insurance Years) is the gives the duration of an insurance contract in years. The main difference to CIY is that, if the date of calculation (t_A) is smaller then the contract termiantion date (t_T), then CI calculates the duration of ongoing contract since its beginning.

$$IY_t = \frac{\min(t_T, t_A) - t_S + 1}{365}$$

- **CIY** (Contract Insurance Years) gives the expected or factual duration of a contract, regardless on when the calculation itselgf is done.

$$CIY = \frac{t_T - t_S + 1}{365}$$

- NOTE: if $t_A \geq t_E \geq t_C$ then $IY = CIY$ means that if calculation is done after the termination of the contract, both IY and CIY yield the same result, otherwise $IY < CIY$.

The datbe can be updated with the two metrics and one additional columns, representing the sum:

Table 2: Time table

Attribute	P_A	P_B	P_C	P_D	P_E	SUM
t_I (Issue date)	2017.01.01	2017.01.01	2016.10.01	2017.02.01	2017.12.31	
t_S (Policy start date)	2017.01.01	2017.01.01	2017.01.01	2017.03.01	2017.01.01	
t_C (Policy cancellation date)		2017.05.10	2017.11.10		2017.01.01	
t_E (Policy end date)	2017.12.31	2017.12.31	2017.12.31	2017.09.30	2017.12.31	
t_T (Policy termination date)	2017.12.31	2017.05.10	2017.11.10	2017.09.30	2017.01.01	
t_a (Today)	2017.07.15	2017.07.15	2017.07.15	2017.07.15	2017.07.15	
IY	0.5	0.4	0.5	0.4	0.0	1.8
CIY	1.0	0.4	0.9	0.6	0.0	2.8

4 Premium

- **WP** (Written Premium) - is the amount the insured must pay in order to get insurance coverage in exchange. There are different methods how to calculate the WP, but in general the WP has to equal the expected pay outs of the insurance company and has the following form:

$$WP = \mu + OE + RC + COM + \pi$$

where μ is the expected loss, OE are the operating expenses, RC is the reinsurance cost, COM is the commission payment, π is the profit and

$$TotExp = OE + RC + COM + \pi$$

It is common to represent total expenses as a proportion of WP hence the formula can be rewritten to:

$$WP = \frac{\mu}{1 - \frac{TotExp}{WP}}$$

So if you expect, that your total expenses as share of written premium are about 40 per cent, then this implies, that

$$WP = \frac{\mu}{1 - 0.4} = \frac{\mu}{0.6}$$

Lets assume the following information is given:

- long term average claim μ is estimated to equal 1400 euro
- OE (Operating Expenses) are 300 euro per policy
- RC (Reinsurance Cost) is 300 euro per policy
- COM (Commission) paid to an agent or broker is equal to 200 euro
- π (Profit) that insurance company intends to make is 160 euro per policy
- average premium written $\overline{WP} = 2400$

This allows to calculate total expenses $TotExp$ and thus in two different ways the WP

- $TotExp = OE + RC + COM + \pi = 300 + 300 + 200 + 160 = 960$
Either:

- $WP_{base} = 1440 + 960 = 2400$
- $WP_{base} = \frac{1440}{1 - \frac{960}{WP}} = \frac{1440}{0.6} = 2400$

This WP is calculated for a full-year policy (= 365 days). So the WP at time t_I (assuming $t_E = t_C$) is :

$$WP_{t_I} = WP_{base} \times CIY$$

- **CP** (Canceled Premium) - is the premium amount that has been or has not been paid in for the the period between cancelation and policy end date. Is calculated as:

$$CP = \frac{END - CANCEL + 1}{END - START + 1} \times WP$$

$$CP_A = \frac{2017.12.31 - 2017.10.30 + 1}{2017.12.31 - 2017.01.01 + 1} \times 2400 = \frac{61}{365} \times 2400 = 401.10$$

- **GWP** (Gross Written Premium) - is the difference between written premium (WP) and canceled premium (CP) at the end of the insurance period.

$$GWP = WP - CP$$

If the policy is not canceled, then $CP = 0$ and $GWP = WP$.

It can also be expressed as $GWP = EP + UPR$

- **UPR** (Unearned Premium Reserve) - is the ammount of premium that is reserved as not yet earned and if policy is cancelled, this amouont would be returned to policy holder/payer.

$$UPR = \frac{t_T - \min(t_T, t_n)}{t_T - t_S + 1} \times (WP - CP)$$

with

$$\frac{UPR}{GWP} \in [0, 1]$$

Means that UPR must be equal from 0 to 1 (0-100 % of GWP depending on period when the calculation is done (TODAY)).

$$UPR_C = \frac{2017.11.10 - \min(2017.11.10, 2017.05.10)}{2017.11.10 - 2017.01.01 + 1} \times (2400 - 341.9) =$$

$$= UPR_C = \frac{2017.11.10 - 2017.07.15}{2017.11.10 - 2017.01.01 + 1} \times 2058.1 =$$

$$= UPR_C = \frac{118}{314} \times 2058.1 = 773.4$$

- **EP** (Earned Premium) - is the ammont of earned premium to date of cancelation.

$$EP = GWP - UPR$$

$$EP_B = (2400 - 335.34) - 901.91 = 1162.75$$

4.1 Claims

- **CLAIMS** - is defined as the monetary value already paid out for policy holder / beneficiary person in a reported claim event
- **RESERVES** - is defined as the monetary value reserved to be possibly paid out in a reported claim event
- **IBNR** (Incurred But Not Reported) - are reserves for losses that have happened but have not been reported yet, in other words, IBNR is the expected pay out in the future.
- **REGRESS** - is defined as a monteray value regressed (regained) in a reported claim event.

4.2 Functions

- NA is the equivalent of "missing value", or an empty cell in a spread sheet
- Function $\min(a, b)$ chooses the smallest value between a and b . So function $\min(21, 12)$ returns 12 as the result. If function $\min(10, NA, 12)$ evaluates the smallest value, out of three entries, then NA will not be evaluated so that this function returns 10 as the smallest value.

5 Formulas

1. **IL** (Incurred Losses) -

$$IL = CLAIMS + RESERVES - REGRESS + IBNR$$

important to note here, that $IBNR$ changes over times, with its maximum at t_S and with 0 at t_E

2. **LR** (Loss Ratio) - is the ratio between total claims and total premium collected. LR changes over time, as IL can decrease with decreasing $IBNR$ and EP increases towards the end of insurance period.

$$LR_t = \frac{IL_t}{EP_t}$$

3. **CC** (Claims Count) - is the number of claims occurred
4. **AC** (Average Claim) - is the average claim size of all claims occurred.

$$AC_t = \frac{IL_t}{CC_t}$$

5. **CF** (Claim Frequency) - $CF = \frac{CC}{IY}$
6. \emptyset **EP** (average Earned Premium) - $\emptyset EP = \frac{EP}{IY}$
7. \emptyset **GWP** (average Gross Written Premium) - $\emptyset GWP = \frac{GWP}{CIY}$
8. **BC** (Burning Cost) - Average claim x Claim frequency
9. **TLR** (Target Loss Ratio) - is manually set every year, for example "66.2"
10. **TP** (Target Premium) - $TP = \frac{BC}{TLR}$
11. Price increases are needed if: $LR > TRL$ or if $TP > \emptyset GWP$