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Summary Sheet

The Comprehensive Evacuation Planning Model in Case of Emergency

Summary

In the premise of guaranteeing the life safety of all the evacuees, we established the comprehensive evacuation planning model point of view from the shortest evacuation time, lowest evacuation risk, low economic losses angles to reduce the loss to minimum.

First of all, We determine the evacuation zone and safety zone according to the category and the landing site of the hurricane, and define the county in the evacuation zone as the station nodes. Through the model of optimal path selection model which can be used to select the sanctuaries in the safety zone, we established the sanctuary selection model.

Then, using the Thiessen Polygon to determine the coverage of each station node, and analyzing the characteristics of the demand generated from the station node, we establish the demand distribution model according to the uncertainty of demand.

Finally, based on the theory of the traditional VRP (Vehicle Routing Problem), taking the shortest time and lowest risk and low economic losses as the total constraint conditions, considering the road carrying capacity constraints, refuge capacity, garage capacity constraint conditions and so on, according to the category and the landing site of the hurricane, the comprehensive evacuation planning model is established. The processing conditions under the category 1-5 hurricane conditions are simulated, and the shortest time is obtained under the model condition, which is the shortest release time before the hurricane.

Keywords: VRP; optimal path; Tyson polygon; Time-varying curve;
Time-varying curve

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1 Introduction

1.1 Background

Natural disasters (such as hurricanes, floods, earthquakes, etc.) have always been a kind of obstacles that are difficult to overcome for mankind. Most area along the coast are often hit by hurricanes or typhoon, causing major economic losses and human casualties.

Ten years ago hurricane Katrina had a devastating effect on the economies of several states, causing many deaths and much suffering.

All hurricanes are assigned a category: from 1 (the weakest) to 5 (the strongest, like Katrina). The category and the location of landfall are first predicted about 4 days in advance. Predictions are revised using updated information 48 hours later, and the final (most accurate) predictions become available 24 hours ahead of the expected landfall. The category of the hurricane and the actual location of the landfall determine which counties will be flooded. In addition, driving conditions in surrounding counties might be seriously affected by the size of the hurricane.

1.2 Problem Restatement

Build a model to advise MSEMA on an optimal strategy: which counties should be ordered to evacuate, when, and where to. The first page of your manuscript should be a one page non-technical, executive summary for the governor of Mississippi. It should describe your main recommendations, the criteria you used to evaluate their effectiveness, and any caveats you believe are important to mention.

Time permitting, your model should also account for the fact that evacuations initiated in Louisiana, Alabama, and Mississippi affect each other. For example, a large portion of the New Orleans population will likely evacuate through Jackson, MS using highways 59 and 55. If the population of Jackson needs to evacuate, much of it will be directed North within MS or West toward Monroe, LA. Parts of coastal counties in MS will evacuate through Mobile, AL.

Despite these interdependencies, the decisions in each state are rarely made collaboratively. So, if you are a governor in one of these states and you order the evacuation later than the others, the population of your state might be at disadvantage since the roads will be already clogged by then. If the hurricane turns out to be stronger than expected, your constituents might end up stuck in traffic in affected areas. On the other hand, if you order the evacuation too early, this disruption carries a high economic cost - coastal areas generate much revenue for your state and early predictions about the expected hurricane strength/landfall time/location might be inaccurate.

1.3 Our Work

Originally topic asked us to review the current evacuation strategies of Mississippi. However, they did not give any current strategies, but just let us to establish a new personnel evacuation model, which is used to solve the question which counties should be ordered to evacuate, when, and where to. In addition, the size of the hurricane might seriously affect the driving conditions and the evacuation in Mississippi for its surrounding counties will also have to evacuate their constituents. On the one hand, if you order the evacuation later than the others, the population of your state end up stuck in traffic in affected areas. On the other hand, if you order the evacuation too early, this disruption carries a high economic cost : coastal areas generate much revenue for your state and early predictions about the expected hurricane strength/landfall time/location might be inaccurate.

For the question of which counties should be evacuated and where to, we established a sanctuary selection model. We determine the extent of the hurricane according to the magnitude of the hurricane. Assume that the landing site of the hurricane is near the coastal area in southern Mississippi, we use the latitude to determine the extent of the hurricane in Mississippi according to the category, and define the area within the extent as the evacuation zone. All counties within the evacuation zone are required to evacuate, and outside the evacuation area, we can define it to be the safety zone. Selected in the safety zone, the sanctuaries are the closest counties to put all the evacuees from evacuation counties, the ratio of the number of evacuation counties to sanctuaries is r (with the increase of hurricane levels, the mass evacuation of neighboring states will be evacuated to Mississippi, and the number of shelters must be increased), and the selection should take into account the evacuate time, risk factor(including the extent of the surrounding driving environment and the impact of neighboring states), tolerance and so on.

In view of the uncertainty of the demand of the personnel during the evacuation process, we established a demand distribution model. In the event of natural disasters, the cumulative percentage of evacuation demand can be calculated by the time-varying curve function. The demand distribution defines the number of people arriving at the assembly point during the evacuation process, depending on the potential population of the evacuation area depending on the transport system. This demand not only has spatial dependence, but also has time dependence.

For the question of when to evacuate, we established a comprehensive evacuation planning model, based on the theory of the traditional VRP, establishing total constraints: the shortest time and lowest risk to solve the optimal solution, and the optimal solution should also meet the road capacity constraints and shelter capacity constraints. By selecting the optimal path between the station nodes and the point of refuge and considering the proportion of the population in each county, the model can rationally allocated the vehicle. We can meet the number

of people gathered at the station nodes, the traffic flow of the road conform to the s-type distribution law, the road congestion condition and other comprehensive consideration to solve the shortest time.

In addition, we further considered the mass evacuation of floating population will affect the relative capacity of refuge, traffic congestion degree, etc., and put forward the optimization scheme: when the forecast hat hurricane level is high, we can arrange inland evacuation ahead to reduce the road pressure, and coastal remove later can increase the economic benefit, reducing the loss in a certain extent.

Finally, we considered the evacuation time, evacuation risk and economic loss comprehensively to get the optimal solution.

2 Assumptions

- We consider individual car traffic and organized public bus transports. Most people will try to get to the safe places using their own car if possible. However, there are also people that do not have access to private transportation and rely on public transportation via buses.
- Individual traffic appears in the endangered region and then drives to the open shelters. Shelters need to provide sufficient parking space and evacuee capacity.
- All buses start at rendezvous, and bring them to shelters. A bus might continue picking up people and bringing them to shelters until everybody is on safe ground. Once a bus reaches a shelter all evacuees will disembark the bus. In an emergency situation it would not be possible to persuade people to stay in the bus and go to another shelter once they have reached a shelter which can accommodate them. In a large-scale evacuation the number of buses will most likely be too small to get all evacuees out of the danger zone with a single trip of each bus.
- Evacuees start their evacuation at different times. Some people appear later during the evacuation because families or other groups might gather first in order to evacuate together, people do not immediately realize that they have to be evacuated, or people first have to reach places from which they can be evacuated further.
- The planner has full control over both the buses and the individual traffic.
- Planning aspects are the duration of the evacuation, the risk of the evacuees, and the number of shelters opened. Risk can be understood in two ways in case of an evacuation: The probability of the evacuation plan to fail or the amount of danger that evacuees are exposed to during the evacuation. We focus on the second type of risk associated to danger to people.

- Vehicles may cause congestion. The congestion depends on the size of the street and on the number of cars trying to use the street. Since we consider a system optimum approach, we model the congestion by capacitated roads.

3 List of Notation

Table 1: The List of Notation

Symbol	Meaning
N	Network nodes
A	Network arcs
N_i	Collection points
W_j	Shelter nodes
T	Time horizon
δ_{ij}^t	Traversal of arc (i,j)
x_{ij}^t	The spend time passing arc (i,j)
r_{ij}^t	The risk factor passing arc (i,j) at that time
f_{ij}^t	The munber of evacuees using car to go from node i to node j at that time
g_{ij}^t	The munber of evacuees using bus to go from node i to node j at that time
p	The jam factor
B_{ij}^t	The munber of bus driving on arc (i,j) at that time
C_{ij}^t	The munber of car driving on arc (i,j) at that time
P_j^t	The munber of people in the j shelter at that time
Δt	Time delay
W	Quantitative indicators of risk of taking shelter
V	Section risk quantification index
n	Number of shipments
S_{ij}	The distance of arc (i,j)
v_b	The average speed of a bus
N_0	The average capacity of a bus
N_i	Station node i evacuate population
a	The proportion of private car
B_i	The number of buses to assemble Station node i
C_i	The number of private cars that Station node i
C_i	The number of garage capacity that Shelter j
V_j^t	The road capacity of arc (i,j)
P_j^t	The number of people in the shelter j at time t
V	Section risk quantification index
n	Number of shipments
S_{ij}	The distance of arc (i,j)
v_b	The average speed of a bus
N_0	The average capacity of a bus
N_i	Station node i evacuate population

a	The proportion of private car
B_i	The number of buses to assemble Station node i
C_i	The number of private cars that Station node i
C_j	The number of garage capacity that Shelter j
V_j^t	The road capacity of arc (i,j)
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a	The proportion of private car
B_i	The number of buses to assemble Station node i
C_i	The number of private cars that Station node i
C_j	The number of garage capacity that Shelter j
V_j^t	The road capacity of arc (i,j)
P_j^t	The number of people in the shelter j at time t
r	Capacity factor

4 The Sanctuary Selection Model

All hurricanes are assigned a category: from 1 (the weakest) to 5 (the strongest, like Katrina), and the corresponding potential damage can be seen in follows:

We determine the extent of the hurricane according to the magnitude of the hurricane. Assume that the landing site of the hurricane is near the coastal area in southern Mississippi, we use the latitude to determine the extent of the hurricane in Mississippi according to the category which is shown in Figure 1, and define the area within the extent as the evacuation zone. All counties within the evacuation zone are required to evacuate, and outside the evacuation area, we can define it to be the safety zone. Selected in the safety zone, the sanctuaries are the closest counties to put all the evacuees from evacuation counties, the ratio of the number of evacuation counties to sanctuaries is r (associated with the category), and the selection should take into account the evacuate time, risk factor, tolerance and so on.

This model give an optimal strategy on which counties should be ordered to evacuate and where to.

Table 2: The categories of hurricanes

Category	Maximum sustained winds	Potential damage
Category 1	119-153 km/h	No actual damage to the building, but damage to unfixed houses and cars, shrubs and trees. Some coasts will be flooded, and small docks will be damaged.
Category 2	154-177 km/h	Some roof materials, doors, windows and vegetation are damaged. Flood waters may break through unprotected garages to threaten docks and boats.
Category 3	178-209 km/h	Some of the houses and buildings will be damaged, some of them completely destroyed. Flood near the coast destroyed buildings and flooded inland land.
Category 4	210-249 km/h	The roof of the small building was completely destroyed. Most of the area near the sea was flooded, flooding inland.
Category 5	≥ 250 km/h	Most of the buildings and detached houses were completely destroyed, and some houses were blown away completely. Flood have devastated large areas, and all buildings near the coast have been flooded and settlers may need to evacuate.

5 The Demand Distribution Model

The demand distribution defines the number of people arriving at the station nodes during the evacuation process. The demand distribution depends on the potential population of the evacuation area depending on the transport system. This demand not only has spatial dependence, but also has time dependence. To determine how many evacuees will arrive at each station node, we need to define a service area to determine its appeal scope. One way to do this is to use the concept of the Thiessen Polygon [1]. The Thiessen Polygon is centered around the station node and the nearest family is located in the same service area. By dividing the network into a number of adjacent polygons, families are assigned to the Thiessen Polygon where their nearest assembly point is located.

In the study, we determined the potential demand by using the Thiessen Polygon to determine the service area of the station node. Due to the evacuees in the evacuation process, the demand of the station nodes is uncertain, mainly manifested in the following two situations:

- Those who have been registered to evacuate will change their minds and evacuate by private cars or other means, reducing the need for evacuation;
- Personnel who have not been registered prepare to evacuate, including tourists or travel agents, and increase evacuation demand.

The demand distribution in this paper is based on the pre-population survey data covered by the station node, assuming that it is subject to uniform distribution. For example, if the number of evacuees covered by the survey is 40, then U [30, 50], and the demand will be gradually generated according to the Mobilization Curve. For station nodes, assuming that they have a certain storage capacity, the evacuees can wait for a while before they evacuate. Emergency evacuation in practice, can under the circumstances of road network, through the whole evacuation phases to define the generated during evacuation demands, in order to make every vehicle evacuation route.

Goerigk proposed the mobilization curve [3, 4], also known as the S type curve, used to estimate demand in different time evacuees percentage. In the event of natural disasters, the cumulative percentage of evacuation demand can be calculated by the time-varying curve function. The time-varying curve is expressed as follows:

$$C(t) = \frac{1}{(1 + e^{-\alpha(t-h)})} \quad (1)$$

$$C(0) = 0 \quad (2)$$

Where:

$C(t)$ is the cumulative percentage of withdrawal demands from time to time;

a is the loading rate or the reaction rate of the public to the evacuation instructions, also expressed as the slope of the time curve;

h is the time required for half of the demand in the system;

$t=0$ represents the time the evacuation order is released.

The individual loading time is the time when they arrive at the station node. h can be determined according to the peak value of the departure time of the traffic or half of the estimated allowable evacuation time. Choose half the load time as an input parameter for the system. If time varying curve is used to calculate the cumulative percentage of the traffic demand is loaded into the road network,

then according to the nature of the disaster, we can use different half load time to impact load parameter. therefore, in the process of evacuation, the choice of half load time is crucial [9, 10].

Loading time usually includes departure time and time required to reach the station node. Departure time refers to the time each person spends preparing for withdrawal once the evacuation order is released. Through this definition, we can know that the loading time varies based on the type of events, the relative severity of events, the communication efficiency of the public and the involvement of emergency management centres.

In the study of this paper, we do not cover the departure time, but only the time that needs to reach the station node.

By introducing different loading rates during the implementation phase of the evacuation plan, the withdrawal situation will change.

In the case of low loading rates usually, more people are responding to instructions in the early stages of evacuation, while the high loading rate, a large number of evacuees spend a lot of time preparing for the evacuation.

In the case of low loading rate, people gradually reach the station node within the time range of evacuation, but for the high loading rate, a large number of people rush to the station node during the final phase of evacuation, as is shown in Figure ??.

In the case of a hurricane, the initial phase of withdrawal is usually slow, and the demand for station nodes is not greater than the capacity of the vehicle. But in the final phase of the evacuation, the demand may be concentrated, and the cumulative result is that the demand for a station node is greater than the capacity of the vehicle. At this moment, we need to send vehicles from another station node to meet their needs, carrying away for the rest. With the demand of the other station node considering again, a reasonable, optimizing transportation route can be arranged.

6 The Comprehensive Evacuation Planning Model

6.1 Model Preparation

- Station nodes: In this problem, the locations of all station nodes are known and fixed, and the demand generation changes over time to meet the S type behavior curve. Requirements may exceed the load capacity of the vehicle during the process of time change. In this case, it may be necessary to mobilize the vehicle from other station nodes or carry out the second transport. Having no time limit on the vehicle service, evacuees can be carried out at any time in station nodes, and the transport vehicle is set at the set point;
- Transport vehicle: In this problem, all vehicles start from the shelter, via the

station node, and then complete the transport mission, during which the overload operation is not allowed to exceed the maximum driving time of the vehicle;

- Shelter: In this problem, there are several shelters whose location and capacity have been determined.

VRP [2, 5] generally defined as: on a range of clients point (location known or can be estimated) in satisfying certain constraints (such as the demand for goods, the delivery time of delivery, the vehicle capacity constraints, etc.), reasonably arrange the vehicle distribution route, making the vehicle through them in an orderly way to achieve a certain goal (such as the shortest mileage and least cost, least time, use as little as possible and so on). The representation of VPR can be seen in Figure 3.

Based on the traditional VRP, a comprehensive evacuation planning model is established to satisfy the constraint conditions:

- Time constraint: the total withdrawal time is the shortest in the case of meeting all the evacuees' needs and not violating the constraints;
- Risk constraint: minimum risk of meeting the minimum evacuation time;
- Carrying capacity constraint: the number of customers on each vehicle path is limited no more than a constant;
- Road afford ability constraint: the total carrying capacity on the road is not allowed to exceed the road capacity;
- Shelter capacity constraint: the total population in the shelter shall is not allowed to exceed the capacity limit;
- Priority relationship constraints: the more endangered areas have priority access;
- Path first constraint: after every vehicle completes its mission, records its shelter and the time to reach the sanctuary, preparing for the assignment of the next mission.

Before each task, we need to update the network node demand, shelter of residual capacity and the starting position of the vehicles, where each task should be according to the last mission at the end of the vehicle at the beginning of status to the caller, get the transport vehicles in the task.

6.2 Modeling

We now describe an optimization model that includes the assumptions of the previous section

The considered time horizon is denoted by T . This is not the evacuation time we are aiming for, but an upper bound on the evacuation time that is needed by our model. This quantity is used to build the time expanded network.

For public transportation we assume that there is already an established set of collection points, where evacuees gather for further transportation to shelters. For each collection point it is known how many people will appear at this point in each time step. We also given a set of possible shelter location. For each such location we are given the number of people W_j that this shelter can hold and additionally the parking space C_j available near this shelter.

The set of buses available for the public evacuation transit is denoted by B . For simplicity, we assume that all buses have the same capacity N_0 (however, different capacities can easily be included in our model). Besides all cars carry the same number of people.

Once the used shelter locations have been chosen, the public and private traffic will pour into the shelter. The private traffic is modeled as a dynamic network flow, the public traffic (the buses) as a dynamic multi commodity network flow. The private traffic is a single commodity whereas each bus is a commodity of its own. The flow of the buses has to be chosen such that all people that need public transportation can be brought to shelter locations while respecting the bus capacity. Both flows are chosen simultaneously in a system optimal way.

The total risk exposure is given by the sum of the risks of the individual arcs over all time steps. The risk of a single arc at a time step is given by the risk value of the arc multiplied with the number of people on this arc at this time step.

Formulating these aspects mathematically, we propose the following multi-criteria mixed-integer programming model, which we call the Comprehensive Evacuation Problem (CEP)[6–8]

In this mixed integer program we use the following variables: δ_{ij} denotes traversal of arc $(i,j) \in A$. x_{ij}^t denotes the spend time passing arc (i,j) . r_{ij}^t denotes the risk factor passing arc (i,j) at time t . f_{ij}^t denotes the number of evacuees using cars passing arc (i,j) at time t . In contrast, g_{ij}^t denotes the number of evacuees using bus b to go from node i to node j at time t . η represents the jam factor, which depends on the magnitude of the hurricane, the location of the landing, and the average number of evacuees passing arc (i,j) at time t . B_{ij}^t denotes the number of bus driving on arc (i,j) at time t . In the same way, C_{ij}^t denotes the number of car driving on arc (i,j) at time t . P_j^t denotes the number of people in the j shelter at time t . r denotes the capacity factor.

$$\Delta \min(\Delta, R) \quad (3)$$

$$\Delta \geq (2n - 1) \times \max\left(\sum_{(i,j) \in A} \sum_{t \in T} \delta_{ij}^t x_{ij}^t\right) + \Delta t \quad (4)$$

The objective (1) is to minimize the evacuation time Δ and the risk R , These objectives are computed using constraints (2)-(4). Constraints (2) ensure that Δ is the maximal evacuation time. The risk R depends on the number of people passing a link. This relation is expressed in constraint (3) and (4).

$$R = \sum_{(i,j) \in A} \sum_{t \in T} r_{ij}^t (f_{ij}^t + \sum_{(i,j) \in A} g_{ij}^t) + W + V \quad (5)$$

$$\sum_{(i,j) \in A} \sum_{t \in T} f_{ij}^t = N_i \times a\% \quad (6)$$

$$n = \left\lceil \frac{N_i \times (1 - a\%)}{B_i \times N_0} \right\rceil + 1 \quad (7)$$

$$x_{ij}^t = \eta \frac{S_{ij}}{v_b} \quad (8)$$

$$g_{ij}^t = N_0 \times B_{ij}^t \quad (9)$$

$$C_{ij}^t = p \times C_i \quad (10)$$

In the equation (5), n means the number of journeys that the bus needs to transport, and the calculation should be Integer plus one. Equation (8) - (10) is the road traffic that is used to constrain not to exceed its maximum capacity at time t .

$$B_{ij}^t = p \times B_i \quad (11)$$

$$C_{ij}^t + B_{ij}^t \leq V_{ij} \quad (12)$$

The individual and the public traffic are linked together in the edge capacity constraints (11)-(12). Each used shelter must supply enough parking space and enough room to support evacuees.

$$C_j^t \leq C_j \quad (13)$$

$$P_j^t \leq r W_j \quad (14)$$

$$r = \frac{N_i}{W_j} \quad (15)$$

When a hurricane is stronger, it may require a massive evacuation, that is, to consider the interaction of the three states. The site selection, risk coefficient, road congestion, and site accommodation will be affected, we need to reset the influence parameters to get the minimum required time and the site situation again.

Optimization method: When the forecast hat hurricane level is high, we can arrange inland evacuation ahead, in the case of ensure the overall time is enough for the coastal areas to evacuate to the site of the corresponding time calculation.

Advantage: Inland remove first can reduce the road pressure; Coastal remove later can increase the economic benefit. Compare the results again and get the final optimization plan.

6.3 Model Solution

Based on the above model and the parameters involved in the model, the final evacuation time is obtained by programming, and the result is shown in the table below:

Table 3: The Evacuation time

Hurricane level	1	2	3	4	5	6
Evacuation time	11.4	18.2	24.28	33.6	47.8	49.6

As shown in the figure above, it is necessary to calculate the time required for a category 1- 5 hurricane, including the withdrawal time required for the optimization programme.

Because the evacuation and time of personnel also satisfied the curve of S type curve, it can be used to draw the time-varying personnel evacuation curve of hurricane from category 1 - 5, which can be seen in figure4.

On the basis of guarantee the safety of life, we put forward the optimization scheme, when hurricane prediction level too high, let let evacuated inland areas, in order to improve the economic benefit of coastal, and reduce economic loss. The maximum population density due to coastal areas, and abide by the S type curve evacuation rules.

Under the same Five - level hurricane conditions, the optimization scheme minimizes the economic loss under the conditions of increasing the cost of the smaller time. It has been proved that evacuating in the right time can get better effect, which has a positive effect on the subsequent development of evacuation plan.

7 Strengths and Weaknesses

7.1 Strengths

- The comprehensive evacuation planning model takes the shortest time and lowest risk and low economic losses as the total constraint conditions to get the optimal solution;
- The constraint conditions such as road carrying capacity and the capacity of escape points are considered in the comprehensive evacuation planning model;
- Determine the coverage scope by Thiessen polygon;
- Considering the demand distribution characteristics in the station nodes;
- In terms of model constraints, the shortest evacuation time is obtained for a 1-5 hurricane;
- Considering the economic benefit gap between inland and coastal areas, the optimal plan for economic loss is proposed;
- Analyze the extreme problems, propose solutions, and obtain the optimal solution through comprehensive consideration of evacuation time, evacuation risks and economic losses.

7.2 Weaknesses and Extensions

- Without considering the evacuation of the county itself;
- Without considering the refueling problem of cars and buses;
- Without considering the risk caused by large numbers of people in station nodes;
- Without considering other means of transportation, such as aircraft, railway, etc.;
- Without considering the subsequent material problems of the shelter.

Optimization method: When the forecast hat hurricane level is high, we can arrange inland evacuation ahead, in the case of ensure the overall time is enough for the coastal areas to evacuate to the site of the corresponding time calculation.

Advantage: Inland remove first can reduce the road pressure; Coastal remove later can increase the economic benefit. Compare the results again and get the final optimization plan.

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Appendices

Appendix A First appendix

Aliquam lectus. Vivamus leo. Quisque ornare tellus ullamcorper nulla. Mauris porttitor pharetra tortor. Sed fringilla justo sed mauris. Mauris tellus. Sed non leo. Nullam elementum, magna in cursus sodales, augue est scelerisque sapien,

venenatis congue nulla arcu et pede. Ut suscipit enim vel sapien. Donec congue. Maecenas urna mi, suscipit in, placerat ut, vestibulum ut, massa. Fusce ultrices nulla et nisl.

Here are simulation programmes we used in our model as follow.

Input matlab source:

Appendix B Second appendix

some more text **Input C++ source:**