# NATIONAL TAIPEI UNIVERSITY OF TECHNOLOGY

### 2018 FALL

245765 - ADVANCED DIGITAL IMAGE PROCESSING

# HW#3 Grey Level Transformation & Histogram Equalization

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# Problem 1 Grey Level Transformation (C/C++) (40%)

a. Enhance the image cat\_bright.raw and cat\_dark.raw by Power-Law and Piecewise-Linear transformation that learned in class. Show the best parameters, the gray-level transform curve and output images. (Figure, 20%; Discussion, 10%)

#### Ans

The concept of **Piecewise-Linear transformation** is use pre-define Gamma function to transform, Equation (1) the pixel value.

$$s_r = c \cdot r^{\gamma} \tag{1}$$

Figure 1 shows the curves for difference Gamma value apply to Gamma function.

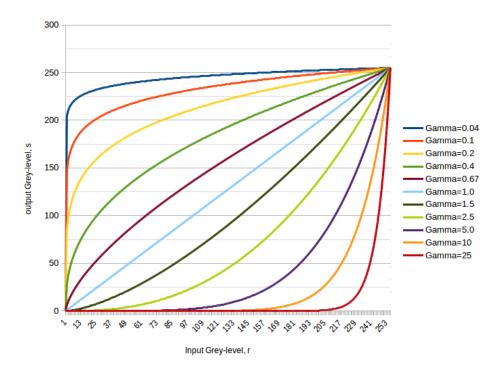


Figure 1: Power-Law Transformation in different Gamma.

The best gamma for cat\_bright.raw is **10.0**. According to Figure 1, the high pixel value apply Gamma=10 curve is more sensitive.



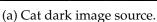


- (a) Cat bright image source.
- (b) Power-Law Transformation.

Figure 2: Power-Law Transformation bright image with best **Gamma 10.0**.

The best gamma for cat\_dark.raw is 0.2. For enhancing dark image the gamma value need to < 1 to make it sensitive on low pixel value.







(b) Power-Law Transformation.

Figure 3: Power-Law Transformation bright image with best Gamma 0.20.

In **Piecewise-Linear transformation** method, we define our linear curve by self, so in Figure 4 I define a curve for scale high grey level pixel value for bright image. The enhance result of cat\_bright.raw shows on Figure 5. The best values  $(r_1, s_1) = (20, 10)$  and  $(r_2, s_2) = (150, 50)$ .



Figure 4: Power-Law Transformation in different Gamma.

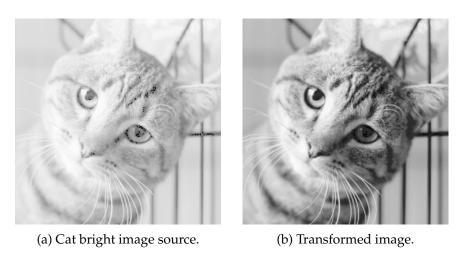


Figure 5: Piecewise-Linear transformation bright image with **Figure 4** curve.

Figure 6, I define a linear curve for scale low gray-level value. The best values  $(r_1, s_1) = (10, 150)$  and  $(r_2, s_2) = (50, 200)$ .

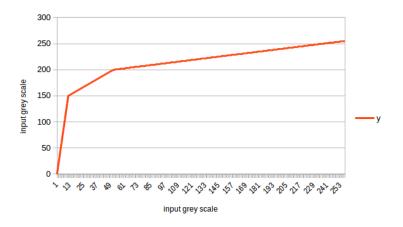


Figure 6: Power-Law Transformation in different Gamma.

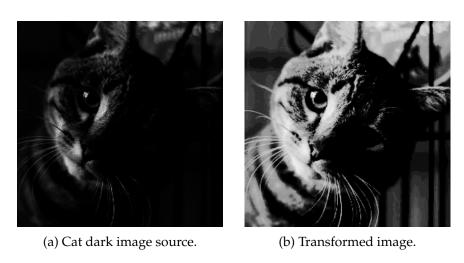


Figure 7: Piecewise-Linear transformation dark image with **Figure 6 curve**.

b. Compare and discuss the results obtained by the two methods and explain the difference.( Discussion, 10%)

#### Ans

The difference of Power-Low and Piecewise-Linear transformation is how we define the function. Power-Low method is very easy use but it is not good for deal with both low and high pixel value need to enhance at same time. However,

Piecewise-Linear transformation is more easy to do this but it is hard to find the best  $r_1$  and  $r_2$  values.

#### Source code for Problem 1

grey\_level\_transformation.hpp

```
#include <iostream>
2 #include <fstream>
3 #include <opencv2/opencv.hpp>
#include <opencv2/highgui/highgui.hpp>
6 const std::string SAVE_IMG_FOLDER = "../result_img/";
  const double GAMMAS[] = {0.04, 0.1, 0.2, 0.4, 0.67, 1.0, 1.5, 2.5, 5.0, 10.0,
       25.0};
  void loadRawFile(cv::Mat &dst_img, std::string file_path, int width, int
      height);
void showImage(std::string win_name, cv::Mat &show_img);
void saveImage(cv::Mat &img, std::string folder, std::string file_name);
double powerLaw(double L, double c, double r, double gamma);
void PowerLawTransformation(cv::Mat &src , cv::Mat &dst , double gamma);
void showAllImages(std::vector<cv::Mat> &list, std::string prefix);
  void saveAllImages(std::vector<cv::Mat> &list, std::string floder, std::
      string prefix);
 void plotCurves(cv::Mat &plot, std::vector<std::vector<cv::Point2f> >
      curvesPoints);
double linearFunc(uint8_t value, cv::Point2f r1s1, cv::Point2f r2s2, double L
  void piecewiseLinearTF(cv::Mat &src_img,
18
19
                         cv::Mat &dst_img,
                         cv::Point2f r1s1,
20
                         cv::Point2f r2s2);
21
void writeCSV( std::string folder,
                 std::string file_name,
23
                 std::vector<std::vector<cv::Point2f> > curvesPoints);
  void writeCSV( std::string folder,
25
                 std::string file_name,
                 std::vector<cv::Point2f> curvesPoints);
  grey_level_transformation.cpp
```

```
#include "grey_level_transformation.hpp"

void loadRawFile(cv::Mat &dst_img, std::string file_path, int width, int height)

to std::FILE* f = std::fopen(file_path.c_str(), "rb");

f/ std::vector<char> buf(width*height); // char is trivally copyable unsigned char buf[width][height];

std::fread(&buf[0], sizeof buf[0], width*height, f);
```

```
for (int i = 0; i < dst_img.rows; i++)
9
10
      for (int j = 0; j < dst_img.cols; j++)
11
12
        dst_img.at < char > (i, j) = buf[i][j];
13
14
15
    std::fclose(f);
16
17
18
  void showImage(std::string win_name, cv::Mat &show_img)
19
20
    static int win_move_x = 50;
21
    static int win_move_y = 50;
22
    cv :: namedWindow(win_name, 0);
23
    cv::resizeWindow(win_name, show_img.cols, show_img.rows);
24
    cv::moveWindow(win_name, win_move_x, win_move_y);
    cv::imshow(win_name, show_img); //display Image
    win_move_x += show_img.cols;
27
    if (win_move_x > 1920 - 256)
28
29
      win_move_x = 50;
30
      win_move_y += (show_img.rows+35);
31
32
33
34
35 void saveImage(cv::Mat &img, std::string folder, std::string file_name)
36
    std::string save_file = folder + file_name + ".png";
37
    cv::imwrite(save_file, img);
38
39
40
41 double powerLaw(double L, double c, double r, double gamma)
42 {
    return L * c * pow(r / L, gamma);
43
44
45
  void PowerLawTransformation(cv::Mat &src, cv::Mat &dst, double gamma)
46
47
48
    double c = 1.0;
    double L = 255;
49
    for (int i = 0; i < src.rows; i++)
50
51
       for (int j = 0; j < src.cols; j++)
52
53
54
        double src_value = src.at<unsigned char>(i, j);
        double dst_value = powerLaw(L, c, src_value, gamma);
55
        dst.at<char>(i, j) = (char) dst_value;
56
```

```
58
59 }
61 void showAllImages(std::vector<cv::Mat> &list, std::string prefix)
62 {
    for (int i = 0; i < list.size(); i++)</pre>
63
64
       std::string gamma = std::to_string(GAMMAS[i]);
65
      gamma.erase ( gamma.find_last_not_of('0') + 2, std::string::npos );
66
       showImage(prefix + " " + gamma + "gamma", list[i]);
67
68
69
70
71 void saveAllImages(std::vector<cv::Mat> &list, std::string floder, std::
      string prefix)
72
    for (int i = 0; i < list.size(); i++)</pre>
73
74
       std::string gamma = std::to_string(GAMMAS[i]);
75
      gamma.erase ( gamma.find_last_not_of('0') + 2, std::string::npos );
       std::string save_file = floder + prefix + gamma + ".png";
       cv::imwrite(save_file, list[i]);
79
80
  }
81
  void plotCurves(cv::Mat &plot, std::vector<std::vector<cv::Point2f> >
82
      curvesPoints)
83
    for (int i = 0; i < curvesPoints.size(); i++)</pre>
84
85
       cv::Mat curve(curvesPoints[i], true);
       curve.convertTo(curve, CV_32S); //adapt type for polylines
87
       polylines(plot, curve, false, cv::Scalar(255), 2, CV_AA);
88
89
90 }
91
  double linearFunc(uint8_t value, cv::Point2f r1s1, cv::Point2f r2s2, double L
       = 255)
93
    if (value  >= 0 \&\& value < r1s1.x)
94
95
       double m = r1s1.y / r1s1.x;
96
97
       return m*value;
    else if (value >= r1s1.x \&\& value < r2s2.x)
100
       double m = (r1s1.y - r2s2.y) / (r1s1.x - r2s2.x);
101
       double c = r1s1.y - m * r1s1.x;
102
       return m * value + c;
```

```
104
     else if (value >= r2s2.x)
105
106
       double m = (L - r2s2.y) / (L - r2s2.x);
107
       double c = r2s2.y - m * r2s2.x;
108
       return m * value + c;
109
     }
110
     else
111
112
113
       return -1;
114
115
116
   void piecewiseLinearTF(cv::Mat &src_img,
                             cv::Mat &dst_img,
118
                             cv::Point2f r1s1,
119
                             cv::Point2f r2s2)
120
121
     for (int i = 0; i < src_img.rows; i++)
122
       for (int j = 0; j < src_img.cols; j++)
124
125
          dst_img.at < char > (i, j) = linearFunc(src_img.at < char > (i, j), r1s1, r2s2)
126
127
128
129
130
   void writeCSV( std::string folder,
131
132
                    std::string file_name,
                    std::vector<std::vector<cv::Point2f> > curvesPoints)
133
134 {
     std::ofstream myfile(folder+file_name+".csv");
135
     myfile << "x";
136
     for (int i = 0; i < curvesPoints.size(); i++)</pre>
137
138
       myfile << ",y" + std::to_string(i);
139
140
     myfile << std::endl;
141
     for (int i = 0; i < curvesPoints[0].size(); i++)</pre>
142
143
       myfile << curvesPoints[0][i].x << ",";</pre>
144
        for (int j = 0; j < curvesPoints.size(); <math>j++)
145
146
          myfile << curvesPoints[j][i].y;
147
          if (curvesPoints.size()-1 != j)
148
149
            myfile << ",";
150
151
```

```
152
       myfile << std::endl;
153
154
155
     myfile.close();
156 }
   void writeCSV( std::string folder,
157
                    std::string file_name,
158
                    std::vector<cv::Point2f> curvesPoints)
159
160
     std::ofstream myfile(folder+file_name+".csv");
161
     myfile << "x,y" << std::endl;
162
     for (int i = 0; i < curvesPoints.size(); i++)</pre>
163
164
       myfile << curvesPoints[i].x << "," << curvesPoints[i].y << std::endl;</pre>
165
166
     myfile.close();
167
168
169
   int main(int argc, char **argv)
170
     cv::Mat cat_b_src(256, 256, CV_8UC1);
     cv::Mat cat_d_src(256, 256, CV_8UC1);
173
     loadRawFile(cat_b_src, "../images/cat_bright.raw", 256, 256);
loadRawFile(cat_d_src, "../images/cat_dark.raw", 256, 256);
174
176
     // Power-Law Transformation
177
     std::vector<cv::Mat> cat_b_img_lst;
178
     std::vector<cv::Mat> cat_d_img_lst;
179
180
     std::vector<std::vector<cv::Point2f>> curvesPoints;
181
     for (int i = 0; i < sizeof(GAMMAS)/sizeof(double); i++)
182
       cv::Mat cat_b_transformed(256, 256, CV_8UC1);
183
       cv::Mat cat_d_transformed(256, 256, CV_8UC1);
184
       PowerLawTransformation(cat\_b\_src\ ,\ cat\_b\_transformed\ ,\ GAMMAS[\ i\ ])\ ;
185
       PowerLawTransformation(cat_d_src , cat_d_transformed , GAMMAS[i]);
       cat_b_img_lst.push_back(cat_b_transformed);
       cat_d_img_lst.push_back(cat_d_transformed);
       // insert data to curve
189
       std::vector<cv::Point2f> curvePoints;
190
       for (int j = 0; j < 256; j++)
192
         cv::Point2f point(j, powerLaw(255, 1.0, j, GAMMAS[i]));
193
194
         curvePoints.push_back(point);
195
       curvesPoints.push_back(curvePoints);
196
197
     cv::Mat plot_img(256, 256, CV_8UC1, cv::Scalar(0));
198
     plotCurves(plot_img, curvesPoints);
199
200
```

```
// Piecewise-Linear Transformation
201
      cv::Mat cat_b_plt(256, 256, CV_8UC1);
202
203
      cv::Mat cat_d_plt(256, 256, CV_8UC1);
      piecewiseLinearTF(cat_b_src, cat_b_plt, cv::Point2f(20,10), cv::Point2f
      piecewiseLinearTF(cat_d_src, cat_d_plt, cv::Point2f(10,150), cv::Point2f
205
        (50,200));
      std::vector<cv::Point2f> piecewise_curve_bright;
206
      std::vector<cv::Point2f> piecewise_curve_dark;
207
      for (int i = 0; i < 256; i++)
208
        piecewise_curve_bright.push_back(cv::Point2f(i, linearFunc(i, cv::Point2f
        (20, 10), cv::Point2f(150,50)));
        piecewise_curve_dark.push_back(cv::Point2f(i, linearFunc(i, cv::Point2f
211
        (10, 150), cv :: Point2f(50,200)));
212
213
      // showImage("Power Law", plot_img);
214
      // showAllImages(cat_b_img_lst, "cat b");
215
      // showAllImages(cat_d_img_lst, "cat d");
216
      // showImage("src cat bright", cat_b_src);
217
      // showImage("PLT cat bright", cat_b_plt);
218
      // showImage("src cat dark", cat_d_src);
// showImage("PLT cat dark", cat_d_plt);
219
220
      writeCSV("../result_plot_data/", "Power-Law", curvesPoints);
writeCSV("../result_plot_data/", "piecewise_curve_bright",
221
222
        piecewise_curve_bright);
      writeCSV("../result_plot_data/", "piecewise_curve_dark",
223
        piecewise_curve_dark);
      saveAllImages(cat_b_img_lst, "../result_img/problem1/power_law/", "
        cat_bright");
      saveAllImages(cat_d_img_lst , "../result_img/problem1/power_law/", "cat_dark
225
        ");
      saveImage(cat_b_src, "../result_img/problem1/", "cat_bright_src");
226
      saveImage(cat_b_stc, .../result_img/problem1/", "cat_bright_stc");
saveImage(cat_b_plt, "../result_img/problem1/", "cat_bright_plt");
saveImage(cat_d_src, "../result_img/problem1/", "cat_dark_src");
saveImage(cat_d_plt, "../result_img/problem1/", "cat_dark_plt");
227
228
229
      cv :: waitKey (0);
230
231
      return 0;
232 }
```

# Problem 2 Histogram Equalization (C/C++) (60%)

a. Plot the histogram of livingroom\_bright.raw and livingroom\_dark.raw. Discuss the difference among these histograms. (Figure, 10%; Discussion, 10%)

#### Ans

The difference between bright and dark image histogram are distributed on different mean and variance. For example, the histogram of bright image, The most pixel are locate in high value area (see Figure 8a). On the other, dark image pixel value are concentrate on low value part (see Figure 8b).

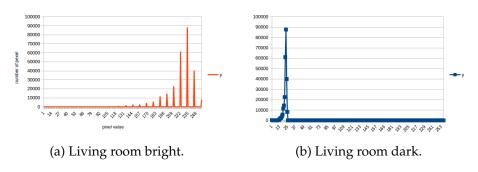


Figure 8: Histofram of living room images

b. Perform histogram equalization on livingroom\_bright.raw and livingroom\_dark.raw. Plot their histograms after equalization and compare the results, will the result be the same and why? (Figure, 10%; Discussion, 10%)

#### Ans

The result of bright and dark living room images show on Figure 9. We can see after histogram equalization, both of dark and bright are get the same histogram distribution.

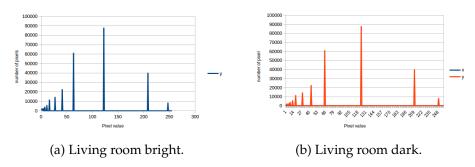


Figure 9: Histofram of living room image

c. If you perform histogram equalization on cat\_bright.raw and cat\_dark.raw, will the result look good? Show the output images and explain what causes this situation and how to improve it. (Figure, 10%, Discussion, 10%)

#### Ans

In Figure 10 and Figure 11 are the images which is performed histogram equalization. The result images looks very similar. In the result images, we can see there are some false contouring effect. For solving this problem, we can thought low-pass to make images more smooth.



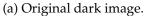


(a) Original bright image.

(b) Equalize image.

Figure 10: Living room bright histogram equalization







(b) Equalize image.

Figure 11: Living room dark histogram equalization

#### Source code for Problem 2

histogram\_equalization.hpp

```
#include <iostream>
#include <fstream>
3 #include <opencv2/opencv.hpp>
#include <opencv2/highgui/highgui.hpp>
6 class HistogramEq
7 {
    public:
    std::vector<int> histogram;
9
10
    std::vector<int> cdf;
    std::vector<int> v_map;
11
    int cdf_min;
12
    int L;
13
    int pixel_num;
14
    HistogramEq(cv::Mat &src_img, int L);
15
    std::vector<int> getHistogram(cv::Mat &src_img, int L);
16
    std::vector<int> getCDF();
17
    int getHv(int v);
18
19
    std::vector<int> getEqHistofram();
20
    void ComputeVmap(std::vector<int> &v_map);
    cv::Mat getEqImage(cv::Mat &img_src);
21
22 };
```

histogram\_equalization.cpp

```
1 #include "histogram_equalization.hpp"
2
  void loadRawFile(cv::Mat &dst_img, std::string file_path, int width, int
      height)
4 {
    std::FILE* f = std::fopen(file_path.c_str(), "rb");
                                              // char is trivally copyable
    // std::vector<char> buf(width*height);
6
    unsigned char buf[width][height];
    std::fread(&buf[0], sizeof buf[0], width*height, f);
9
    for (int i = 0; i < dst_img.rows; i++)
10
      for (int j = 0; j < dst_img.cols; j++)
11
        dst_{img.at}< char>(i, j) = buf[i][j];
14
15
    std::fclose(f);
16
17 }
18
19 void showImage(std::string win_name, cv::Mat &show_img)
20 {
static int win_move_x = 50;
```

```
static int win_move_y = 50;
22
    cv :: namedWindow(win_name, 0);
23
24
    cv::resizeWindow(win_name, show_img.cols, show_img.rows);
    cv::moveWindow(win_name, win_move_x, win_move_y);
    cv::imshow(win_name, show_img); //display Image
    win_move_x += show_img.cols;
27
    if (win_move_x > 1920 - 256)
28
29
      win_move_x = 50;
30
      win_move_y += (show_img.rows+35);
31
32
33
34
  void writeCSV( std::string folder,
35
                   std::string file_name,
36
                  std::vector<int> curvesPoints)
37
38
    std::ofstream myfile(folder+file_name+".csv");
    myfile << "x,y" << std::endl;
40
    for (int i = 0; i < curvesPoints.size(); i++)</pre>
41
42
      myfile << i << "," << curvesPoints[i] << std::endl;</pre>
43
44
45
    myfile.close();
46
47
  void saveImage(cv::Mat &img, std::string folder, std::string file_name)
48
49
    std::string save_file = folder + file_name + ".png";
50
    cv::imwrite(save_file, img);
51
52 }
53
54 HistogramEq::HistogramEq(cv::Mat &src_img, int L=256)
55 {
    this ->histogram = this ->getHistogram(src_img, L);
    this ->cdf = this ->getCDF();
57
    this \rightarrow L = L;
    this ->pixel_num = src_img.cols * src_img.rows;
59
    this ->ComputeVmap(this ->v_map);
60
61
62
  std::vector<int> HistogramEq::getHistogram(cv::Mat &src_img, int L=256)
63
64
    std::vector < int > his(L, 0.0);
65
    for (int i = 0; i < src_img.rows; i++)
66
67
       for (int j = 0; j < src_img.cols; j++)
68
69
         his[src_img.at < uint8_t > (i, j)] += 1.0;
70
```

```
71
72
73
     return his;
74 }
75
76 std::vector<int> HistogramEq::getCDF()
77
     std::vector<int> his_src = this->histogram;
     std::vector<int> cdf(his_src.size());
     int cdf_count = his_src[0];
80
     int cdf_min = 0;
81
     for (int i = 0; i < his_src.size(); i++)</pre>
82
83
       cdf[i] = cdf_count;
84
       if (cdf_min == 0 && cdf_count != 0) cdf_min = cdf_count;
85
       cdf_count += his_src[i];
86
87
     this ->cdf_min = cdf_min;
88
     return cdf;
89
90
91
   int HistogramEq::getHv(int v)
92
93
     return ((double)(this->cdf[v] - this->cdf_min) / (double)(this->pixel_num))
94
        * (this \rightarrow L - 1);
95
96
97 std::vector<int> HistogramEq::getEqHistofram()
98
     std::vector<int> eq_his(this->histogram.size());
99
     for (int i = 0; i < eq_his.size(); i++)
100
101
       eq_his[this->getHv(i)] = this->histogram[i];
102
103
     return eq_his;
104
105
   void HistogramEq::ComputeVmap(std::vector<int> &v_map)
107
108
     v_map.resize(this->histogram.size());
109
     for (int i = 0; i < this->histogram.size(); i++)
110
       v_map[i] = this -> getHv(i);
112
113
114 }
115
cv::Mat HistogramEq::getEqImage(cv::Mat &img_src)
117
     cv::Mat eq_img(img_src.rows, img_src.cols, CV_8UC1);
```

```
for (int i = 0; i < img_src.rows; i++)
119
120
121
       for (int j = 0; j < img_src.cols; j++)
         eq_img.at<char>(i, j) = this->v_map[img_src.at<uint8_t>(i, j)];
124
     return eq_img;
126
127
128
   int main(int argc, char **argv)
129
130
     cv::Mat lvroom_b_src(512, 512, CV_8UC1);
131
     cv::Mat lvroom_d_src(512, 512, CV_8UC1);
132
     loadRawFile(lvroom_b_src, "../images/livingroom_bright.raw", 512, 512);
loadRawFile(lvroom_d_src, "../images/livingroom_dark.raw", 512, 512);
134
135
     HistogramEq hiseq_living_b = HistogramEq(lvroom_b_src);
     HistogramEq hiseq_living_d = HistogramEq(lvroom_d_src);
     writeCSV("../result_plot_data/", "livingRoomBrightHis", hiseq_living_b.
137
       histogram);
     writeCSV("../result_plot_data/", "livingRoomDarkHis", hiseq_living_d.
138
       histogram);
     writeCSV("../result_plot_data/", "livingRoomBrightEqHis", hiseq_living_b.
139
       getEqHistofram());
     writeCSV("../result_plot_data/", "livingRoomDarkEqHis", hiseq_living_d.
140
       getEqHistofram());
     cv::Mat lvroom_b_eq_img = hiseq_living_b.getEqImage(lvroom_b_src);
141
     cv::Mat lvroom_d_eq_img = hiseq_living_d.getEqImage(lvroom_d_src);
142
     saveImage(lvroom_b_src, "../result_img/problem2/", "livingroom_bright_src")
143
     saveImage(lvroom_b_eq_img, "../result_img/problem2/", "
       livingroom_eq_bright_src");
     saveImage(lvroom_d_src, "../result_img/problem2/", "livingroom_dark_src");
145
     saveImage(lvroom_d_eq_img, "../result_img/problem2/", '
146
       livingroom_eq_dark_src");
     showImage("livingroom bright", lvroom_b_src);
147
     showImage("livingroom eq bright", lvroom_b_eq_img);
148
     showImage("livingroom dark", lvroom_d_src);
149
150
     showImage("livingroom eq dark", lvroom_d_eq_img);
151
     cv :: waitKey (0);
     return 0;
152
153 }
```