#### UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level and GCE Advanced Level

# MARK SCHEME for the May/June 2010 question paper for the guidance of teachers

## 9709 MATHEMATICS

9709/43

Paper 43, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• CIE will not enter into discussions or correspondence in connection with these mark schemes.

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### **Mark Scheme Notes**

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking g equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only – often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
sos	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

## **Penalties**

- MR −1 A penalty of MR −1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR −2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

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1	$[7.3 \sin \alpha = 5.5]$	M1		For using $R_y = 0$
	$\alpha = 48.9$	A1		Ear using D = D
	$[R = 6.8 - 7.3 \cos 48.9^{\circ}]$ Magnitude of regultant is 2 N	M1 A1		For using $R = R_x$
	Magnitude of resultant is 2 N	AI	[4]	
			[4]	
2	[1.2 - 0.24t = 0.6]	M1		For using $a = dv/dt$ and attempting to solve $a = 0.6$
	t = 2.5	A1		
	$[s = 0.6t^2 - 0.04t^3]$	M1		For using $s = \int v dt$
	$s = (0.6 \times 2.5^2 - 0.04 \times 2.5^3) - (0 - 0)$	DM1		For using limits 0 to 2.5 or equivalent (dependent on integration)
	Displacement is 3.125 m	A1		Accept 3.12 or 3.13
	•		[5]	•
3	(i) $[WD = 25 \times 40 \cos 30^{\circ}]$	M1		For using $WD = Fd\cos\theta$
	Work done is 866 J	A1		
			[2]	
	(ii) $[50 \times 40 \cos 30^{\circ} = 866 + KE \text{ gain}]$	M1		For using WD by P = WD against resistance + KE gain
	KE gain is 866 J	A1ft		ft incorrect ans (i)
	TEL gam is ooo s	M1		For using KE gain = $\frac{1}{2}$ m( $v^2 - u^2$ )
	$\frac{1}{2} 35(v^2 - 1.2^2) = 866$	A1ft		ft incorrect KE
	Speed is 7.14 ms <sup>-1</sup>	A1		
	1		[5]	
				SR (max 2/3 for the last three marks) for using Newton's second law and constant acceleration formula $50 \cos 30^{\circ} - 25 \cos 30^{\circ} = 35a$ and $v^{2} = 1.2^{2} + 2 \times 40a$ M1 $\Rightarrow$ speed is 7.14 ms <sup>-1</sup> A1
4	(i) $0.36g \sin 60^{\circ} - T = 0.36 \times 0.25$	B1		
	Tension is 3.03 N	B1		AG
			[2]	
	(ii)	M1		For applying Newton's second law to B.
	$T \pm F - 0.24g \sin 60^{\circ} = 0.24 \times 0.25$	A1		Tot applying Newton's second law to B.
	$F = 3.03 - 0.24g \sin 60^{\circ} - 0.24 \times 0.25$			
	(F = 0.889)	A1		
	$R = 0.24g \cos 60^{\circ}$ (R = 1.2)	B1		
		M1		For using $\mu = F/R$
	Coefficient is 0.74	A1		
			[6]	
5	(i)			For using $s = \frac{1}{2}(u + v)t$ to find AB
	$[s = \frac{1}{2}(1.4 + 1.1) \times 1.2; 1.1 = 1.4 + (-d) \times 1.2]$	M1		or $v = u + at$ to find d
	AB = 1.5  m or  d = 0.25	A1		
	d = 0.25 or $AB = 1.5$ m	B1ft	[2]	
			[3]	

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	(ii)	$[0 = u^{2} + 2(-0.25)2;$ $2 = 0 - \frac{1}{2}(-0.25)t^{2}]$	M1		For using $0 = u^2 + 2(-d)s$ to find u <b>or</b> $s = 0 - \frac{1}{2}(-d)t^2$ to find t
		Speed is 1 ms <sup>-1</sup> or time is 4 s	A1		
		Time is 4 s <b>or</b> speed is 1 ms <sup>-1</sup>	B1ft		
				[3]	
	(iii)	For line joining (0, 1.4) and (1.2, 1.1)	B1		
		For line joining $(1.2, -1)$ and $(5.2, 0)$	B1ft	[2]	ft wrong answer(s) in (ii)
				[2]	
					SR (max 1/2)
					For two correct lines and values missing B1ft
					Ditt
6	(i)	[2a = 3.5]	M1		For using $v = 0 + at$
		Acceleration is 1.75 ms <sup>-2</sup> $[1.75 = g \sin \alpha]$ or	A1 M1		For using $a = g \sin \alpha$
		$[0.5 \times 3.5^2 = \text{gh; s} = 0.5 \times 3.5 \times 2 \text{ and}]$	IVII		or for using $\frac{1}{2}mv^2 = mgh$ , $s = \frac{1}{2}vt$ and
		$\sin\alpha = h/s$			$\sin \alpha = h/s$
		Angle is 10.1° or 0.176°	A1	[4]	
				[ <del>+</del> ]	
	(ii)	$[s_P = \frac{1}{2}a2^2 + \{(a2)t + \frac{1}{2}at^2\}]$	M1		For constructing an expression in t for $s_p$
		or $[s_P = \frac{1}{2} a (t + 2)^2]$ $[s_P - s_Q = \frac{1}{2} a 2^2 + (a2)t + \frac{1}{2} a t^2 - \frac{1}{2} a t^2]$	M1		For constructing an expression in t for
		[sp - s() - /2 az + (az)t + /2 at - /2 at]	1111		$S_P - S_O$
		$2 \times 1.75 + 2 \times 1.75t$	A1		Correct expression for $s_P - s_Q$
		[4.9 = 2a + 2at]	M1		For using $s_P - s_Q = 4.9$ to construct an equation in t
		t = 0.4	A1		equation in t
				[5]	
7	(i)	R = 4500 N	B1		
	( )	$3150 = \mu 4500$	M1		For using limiting equilibrium of boxes
		Coefficient is 0.7	۸ 1		$\rightarrow P = \mu R$
		Coefficient is 0.7	A1	[3]	
	(ii)		M1		For resolving forces horizontally on A
		$0.2 \times 200$ g = $200$ a	A1		when A is about to slide AG
		No sliding $\rightarrow$ a $\leq 2$	A1		
		-		[3]	
	(iji)	$[P - F = 450a; P - F - F_2 = 250a]$	M1		For applying Newton's second law to A
	(111)				and B combined or to B
		$P_{\text{max}} = 3150 + 450 \times 2 \text{ or}$	A1		
		$\begin{aligned} P_{max} &= 3150 + 0.2 \times 2000 + 250 \times 2 \\ P_{max} &= 4050 \text{ N} \end{aligned}$	A1		
		1 max TOJOIN	$\Lambda_1$	[3]	