Exploring the Effect of Different Behavior Characterizations in Atari Games

Justin Nguyen ihn545

2014 justinnguyen@gmail.com

Suhaib Abdulquddos sa39663

suhaib.abdulquddos@gmail.com

Abstract—The issue with using gradient-based approaches in the Atari game environment is that some games have deceptive gradient landscapes and sparse reward functions that often trap the agent in local minima. Although novelty search has been known to mitigate such deception, not much research has been done to apply novelty search toward the Atari game environment. In particular, little to no research has been done on the effect of different behavior characterizations (BCs) in Atari games. Thus, the main contribution of this paper is to study the effects of using custom, handcoded BCs for two different Atari games: Frostbite and Kangaroo. Additionally, we also study the impact of using similarity metrics other than Euclidean distance to compare BCs, such as normalized compression distance (NCD). Our results for the heatmap and pixel-count BCs showed that using much smaller BCs can achieve similar (or better) performance than using RAM state. This has led us to believe that many elements of the RAM state BC are extraneous do not aid in the search of behavior space.

I. INTRODUCTION

Atari games are a popular research domain for reinforcement learning (RL) since they provide a structured, modular learning environment [Mnih et al., 2013]. However, most reinforcement learning approaches use gradient-based approaches to maximize a reward function. The issue with using typical gradient-based approaches is that some games have deceptive gradient landscapes, sparse reward functions, and other local optima that can deceive agents and severely impede performance.

One of the most prominent methods of mitigating this deception is novelty search [Lehman and Stanley, 2011a]. Novelty search works by rewarding agents for discovering behaviors that are different from previous ones regardless of how well they perform. In order to determine the difference between behaviors, one must define a distance metric (e.g. Euclidean distance) and a "behavior characterization" (BC). Behavior characterizations are essentially task-specific behavior representations. They are analogous to state representations, except that they represent behaviors instead of states. For example, if an agent is trying to escape a maze and each behavior is a traversal through the maze for X timesteps, then the BC could simply be the ending location of the agent at the final timestep. Ultimately, by rewarding novelty instead of performance, novelty search encourages the agent to try new things instead of being driven toward performance and, in some cases, consequently being deceived into a local optima.

Novelty search has been shown to work well in certain domains with very deceptive gradient landscapes such as human locomotion and the maze environment in [Lehman and Stanley, 2011a]. Additionally, [Conti et al., 2018] have shown that a modified novelty search algorithm combined with evolutionary strategies can perform well in certain Atari games such as Frostbite when using the RAM state¹ of the game as the behavior characterization.

Despite existing research on novelty search, not much work has been tested using the Atari game environment. Specifically, to the authors' knowledge, it is not known how novelty search performs in Atari games when using custom, hand-coded BCs for each game. Instead of simply using the RAM state as the BC for each game, this paper will tackle the challenge of developing task-specific BCs for the highdimensional Atari game environment.

We hypothesize that the RAM state BC used in [Conti et al., 2018] contains extraneous information that is unhelpful with respect to discovering novel behaviors. We believe that using custom, hand-coded BCs for each game will result in higher performance and better direct the search

Additionally, we hypothesize that using similarity metrics other than Euclidean distance, such as normalized compression distance (NCD), when comparing BCs can improve performance as shown in [Gomez, 2009]. Gomez's work used the Tartarus problem, which has a relatively easy-todefine behavior space, but we propose to extend this work to the more complex Atari domain.

We tested our hypotheses by building off of the codebase² used in [Conti et al., 2018]. However, due to time and computational constraints, we were only able to test our hypotheses on two games: Frostbite and Kangaroo. We performed experiments for three different behavior characterizations as well as a separate experiment to compare NCD versus Euclidean distance.

Overall, we have found that our approaches did not yield significant improvements over the results obtained from the code provided. However, we confirmed a hypothesis that many (if not the majority) of elements in the RAM state

¹Each game's RAM state is simply a vector of 128 bytes that, albeit describes the state of the game, is uninterpretable to human eyes

²https://github.com/uber-research/deep-neuroevolution

vector are extraneous in the sense that they do not contain information that is critical in aiding exploration of the behavior space for the game Frostbite. This is evidenced by the slightly superior results [Figure 9] obtained from an experiment wherein the BC used was simply the number of light blue pixels present in the screen at each frame, as compared to the same run where the BC was the entire 128-byte RAM state for each frame. This result is promising and paves an avenue for future work exploring what other BC's might yield even greater performance.

II. RELATED WORK

In this section, we discuss the works that are related to and inspired our research, including the works of [Conti et al., 2018] and [Gomez, 2009].

Similar to our research, [Conti et al., 2018] have tried to apply novelty search to the Atari game environment. In particular, they combined novelty search with evolutionary strategies (ES) to form new quality diversity (OD) algorithms that not only search for performance, but also novelty. Their results showed that these new QD algorithms (NS-ES, NSR-ES, and NSRA-ES) were able to outperform classical RL algorithms such as DQN and A3C on certain Atari games. Their results showed that the success of these QD algorithms is not ubiquitous across the entire suite of Atari games, rather that some games are more conducive to QD algorithms than others. To expand on their work, our research focuses on using more appropriate (domain-specific) behavior characterizations to enhance the efficiency of the behavior space search and ultimately result in agents with greater overall fitness.

Research by [Gomez, 2009] has shown that alternative similarity metrics, such as normalized compression distance (NCD), can perform better than Euclidean distance. Furthermore, [Liwei Wang et al., 2005] have shown that Euclidean distance is a poor choice for comparing images and that different similarity metrics that take into account the spatial relationship of the pixels perform much better. As a result, we decided to research the effect of using NCD to compare behavior characterizations and compare the results to those of Euclidean distance.

III. OUR APPROACH

In this section, we discuss our approach to designing behavior characterizations for two Atari games (Frostbite and Kangaroo) as well as our approach to implementing the NCD similarity metric.

First, we will give an overview of how each game works so that the reader can understand the intuition behind our BCs. Then, we will discuss each of the following ideas in turn.

- Two different BCs for Frostbite: pixel counting, and traversed path
- One BC for Kangaroo: heatmap
- One game for the NCD metric

A. Frostbite: Game Overview

The goal of the game Frostbite is to build an igloo for warmth before time runs out and the player freezes to death. To build the igloo, the player must acquire ice from the ice blocks that are floating horizontally across the screen as shown in Figure 1. Each time the player jumps onto a piece of ice, the entire row changes from white to blue and the player is awarded an ice block for their igloo. Once all of the ice block rows have turned blue, they will turn white again and the player must repeat the ice collection process until the igloo is complete. Additionally, there are enemies such as crabs, birds, and polar bears that the player must avoid or else lose one of his/her 3 lives.

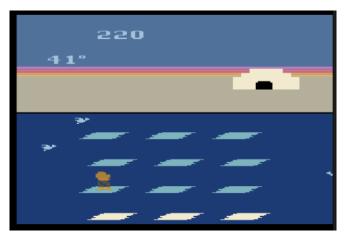


Fig. 1: A simple view of the Frostbite game. Note that the ice blocks turn from white to blue after stepping on them and that the blocks move from left to right. Also note the two birds on the left that must be avoided. Finally, note the igloo that has been built for shelter

We hypothesized that Frostbite would be a good candidate for novelty search since the reward function is rather sparse and the game has plenty of local minima where the player can get trapped.

For example, jumping onto an ice block rewards the player with ten points, but this is almost nothing compared to the few thousands of points rewarded for building and then entering the igloo. Furthermore, in order to actually build the igloo, the player has to already be pretty good at the game, making it hard for agents that receive almost no initial rewards to learn a good behavior in classical reinforcement learning. This intuition is backed by [Conti et al., 2018]'s results in Figure 2. The sparsity of rewards makes Frostbite a reasonable candidate for testing novelty search.

Furthermore, the agent cannot simply follow the gradient and just jump onto the nearest ice block to get a small reward each time since doing so can result in the player getting stranded on an ice block in the middle of the ocean as shown in Figure 3. Following the gradient as such will obviously lead to local minima and result in suboptimal behavior. Instead, the agent also has to consider whether there is a path back to shore after jumping down. The need

GAME	ES	NS-ES	NSR-ES	NSRA-ES	DON	NoisyDON	A3C+
ALIEN	3283.8	1124.5	2186.2	4846.4	2404	2403	1848.3
AMIDAR	322.2	134.7	255.8	305.0	924	1610	964.7
BANK HEIST	140.0	50.0	130.0	152.9	455	1068	991.9
Beam Rider [†]	871.7	805.5	876.9	906.4	10564	20793	5992.1
Freeway [†]	31.1	22.8	32.3	32.9	31	32	27.3
Frostbite [†]	367.4	250.0	2978.6	3785.4	1000	753	506.6
Gravitar	1129.4	527.5	732.9	1140.9	366	447	246.02
MONTEZUMA	0.0	0.0	0.0	0.0	2	3	142.5
Ms. Pacman	4498.0	2252.2	3495.2	5171.0	2674	2722	2380.6
$Q*Bert^{\dagger}$	1075.0	1234.1	1400.0	1350.0	11241	15545	15804.7
Seaquest [†]	960.0	1044.5	2329.7	960.0	4163	2282	2274.1
ZAXXON	9885.0	1761.9	6723.3	7303.3	4806	6920	7956.1

Fig. 2: Comparing novelty search and RL performance in Frostbite. The novelty search algorithms combined with reward (NSR-ES and NSRA-ES) perform much better than traditional RL algorithms such as DQN and A3C+. See [Conti et al., 2018] for further details as these results were pulled from their paper

to avoid deception makes Frostbite a reasonable candidate for testing novelty search.

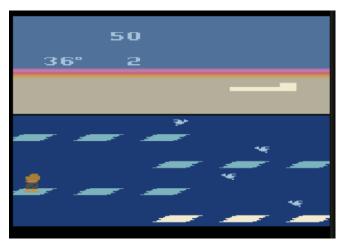


Fig. 3: Getting trapped by local minima in Frostbite. Here, we can see that the agent followed the reward gradient and jumped onto the 3rd row of ice blocks to receive 10 measly points each time. However, the agent is now trapped since there are no ice blocks above or below it. As a result, the agent can only jump up into the ocean, down into the ocean, or move right to fall into the ocean

B. Frostbite: Pixel Counting BC

The first BC we designed for Frostbite simply consisted of a single integer: the number of light blue ice pixels on the screen for each episode. The agent needs to step on ice blocks and turn them from white to light blue in order to make progress toward building the igloo. Thus, by making the BC the number of light blue ice pixels on the screen, we hoped to encourage the agent to find new behaviors that would result in collecting ice for the igloo.

We hypothesized that storing a single integer BC could be superior to the 128 byte RAM state BC. This is because the majority of the RAM state is likely to be useless in terms of discovering new behaviors. For example, one of the bytes might simply be the number of gray pixels on the shore (note

that the RAM state is uninterpretable and we could not find documentation on what each byte value represented so we do not know for sure what is in the RAM state). Additionally, we knew that having a smaller behavior space would help focus the search and hopefully result in faster discovery of relevant, novel behaviors.

C. Frostbite: Heatmap BC

Next, we made a heatmap of the locations visited by the agent during each episode and used that as the BC. After every observation, we ran a filter on the image looking for the agent's RBG colors to find its position and then incremented that location in the heatmap by a constant value.

For example, in Figure 4 you can tell that the agent spent some time in the shore area where it was spawned (see the first row of non-black pixels). Then it seemed to jump to the first row of ice blocks toward the right (see the second row of non-black pixels). In this episode, it seemed to spend more time jumping down to the right of the screen. You can also tell that it very rarely made it to the 3rd row of ice blocks and never seemed to make it to the 4th row for this particular episode.

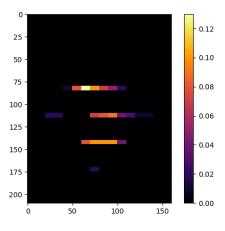


Fig. 4: An example Heatmap BC. You can see that the agent spends more time jumping down the right side of the screen and does not even make it to the 4th row of ice blocks this run

We hypothesized that this BC would perform better than the RAM state BC because this BC keeps track of where the agent has been and encourages it to visit other parts of the screen. This information is very relevant to solving the game. Eventually, if the agent has explored all parts of the screen, it should visit each of the ice block rows and collect enough ice to build the igloo.

D. Frostbite: Traversed Path BC

The last BC we tried for Frostbite consisted of a vector of (x,y) coordinates that represented the path taken during an episode. The difference between this BC and the heatmap BC is that the heatmap simply records where the agent

traversed but not how it actually arrived at those locations. For example, in the heatmap in Figure 4, it is impossible to exactly tell which path the agent took. Did the agent go right, down, down, or did the agent go right, left, right, left, right, down, down or something else? The idea behind this BC was to encode the sequence of locations visited and encourage the agent to try new path trajectories.

We hypothesized that this BC would perform better than the RAM state BC because this BC keeps track of the paths taken by the agent and encourages it to try new paths. This information is very relevant to solving the game. Eventually, if the agent has tried all the paths, it should visit each of the ice block rows and collect enough ice to build the igloo. Additionally, this BC is much smaller than a heatmap and should help direct the search better.

E. Kangaroo: Game Overview

In Kangaroo, the goal for each level is to rescue your kangaroo child at the top of the screen without being hit by enemy projectiles from both above and to the side. The agent needs to move left and right and climb the ladders to the top of the screen while also jumping and ducking to avoid enemy projectiles.

We hypothesized that Kangaroo would be a good candidate for novelty search since the reward function is rather sparse and the game has plenty of local minima where the player can get trapped.

For example, collecting fruit rewards the player with 100 points, but this is almost nothing compared to the 2000 points received for reaching the top and rescuing the kangaroo's child. In order to actually see this large reward, however, the agent has to be very good at the game. It has to know when to jump to avoid enemy projectiles from the side, when to duck because sometimes the side projectiles are thrown at your head instead of your feet, when to dodge left or right when projectiles or coming from above, and when to punch the enemies out of the way.

Furthermore, the agent cannot simply follow the gradient and go up the ladders as quickly as possible. This is because enemies are often waiting to throw the projectiles at you as soon as you are going up the ladder as shown in Figure 5. In this scenario, you are completely vulnerable to their attack since there is no way to dodge once you are on the ladder. Instead, the agent needs to bait the enemy's attack before trying to go up the ladder. The need to avoid such deceptive local minima makes Kangaroo a reasonable candidate for testing novelty search.

F. Kangaroo: Heatmap BC

Unlike the simple maze problem explored in [Lehman and Stanley, 2011a], the amount of time that the agent spends at each location in the map is important. Specific locations may be dangerous at certain times in the episode, whereas at other times those same locations might be crucial stepping stones for reaching the goal.

We hypothesize that using a frequency heatmap BC to keep track of the number of frames spent at each 2D location



Fig. 5: Getting trapped by local minima in Kangaroo. Here, we can see that the agent followed the gradient to start climbing up the ladder. However, the agent is now trapped since it is on the ladder and cannot dodge the enemy projectile. Note that the top red box was drawn to show the projectile and the bottom red box was drawn to show the agent climbing the ladder.

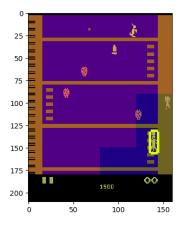


Fig. 6: Kangaroo heatmap. The darker regions of the game (purple regions) correspond to locations where the agent spent the most time.

in the map will encourage greater exploration of the map while also encouraging the agent to spend varying amounts of time in different areas.

As in Frostbite, the agent's location is computed by applying a filter over the image and looking for specific RGB values. For the heatmap BC, the screen is discretized into a 4x7 grid and each region of the grid has a value corresponding to the amount of time spent in that location. A visual aid of the heatmap is shown in Figure 6.

G. New Similarity Metrics: NCD

Normalized compression distance is a similarity metric that has proven to be quite effective at comparing discrete pieces of data represented as bytes [Cilibrasi and Vitanyi, 2005]. Given the prior success

achieved in [Gomez, 2009] for the Tartarus problem, a natural extension is to apply this NCD metric to the results of [Conti et al., 2018] and compare RAM state BCs using NCD instead of Euclidean distance.

NCD is defined as

$$NCD(x,y) = \frac{C(xy) - min(C(x), C(y))}{max(C(x), C(y))}$$
(1)

where x and y represent the pieces of data being compared, xy represents the union of x and y, and C(a) is the length of a after being compressed by a compression function, where the compression function used is up to the user [Gomez, 2009].

The compression function used in the present work is called a run length encoding (RLE) [Pountain, 1987]. The idea behind run length encoding is that consecutive repeated elements of a feature vector can be combined into two elements: the first element represents the frequency and the second element represents the identity of the element being repeated. When appending two different RAM states together, we chose to interleave the RAM states such that the *i*'th element of the first feature vector is next to the *i*'th element of the second feature vector. Thus, if the two corresponding elements of each vector are the same, the RLE score will reward this similarity and yield a better (shorter) encoding length of the appended feature vector.

Furthermore, we provide an additional extension to RLE: a threshold value for similarity within the RLE routine. That is, we only create a new frequency-value pair when the next element is different from the preceding element by some threshold value Δ . For the purpose of actual encoding, this would result in lossy compressions, but for our purposes, this gives some leeway when comparing RAM states that are only slightly dissimilar. Whereas standard Euclidean distance penalizes all non-zero differences regardless of magnitude, with a sufficiently large threshold value, our RLE scheme will not penalize two feature vectors for being only slightly dissimilar. We believe this distinction to be important when comparing discrete RAM states.

IV. EXPERIMENTS AND RESULTS

We observe in Figure 7 that NCD provides greater consistency in the mean reward achieved per episode. Although euclidean distance achieves a greater maximum mean episode reward than NCD over 50 episodes, we note that this comes at the cost of inconsistency. We believe the consistency of NCD can be attributed to the more lenient approach that NCD has with regards to comparing two behavior characterizations. As mentioned in the similarity metrics section of this paper, NCD only looks at the differences in compression length between two BC's. This means that two BC's are only considered different if they have different underlying structures. For our purposes this means that for a given pair of BC's a and b, NCD may have considered these BC's to be more similar than euclidean distance would have. This may have resulted in increased difficulty with regards to making progress with respect to discovering more

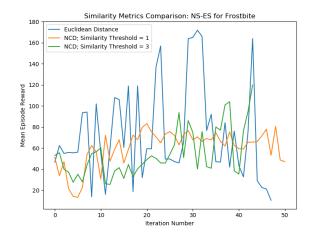


Fig. 7: Comparison of performances of the various similarity metrics used. The game being played is Frostbite, and the algorithm used is NSE-ES.

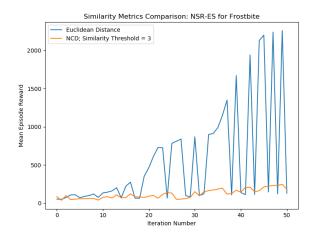


Fig. 8: Comparison of performances of the various similarity metrics used. The game being played is Frostbite, and the algorithm used is NSR-ES.

novel behaviors. Unlike euclidean distance, NCD is not a differentiable function, therefore following a gradient is much more difficult. We see in Figure 8 that NCD used with the RLE compression function results in significantly worse performance than euclidean distance. It should be noted however, that NCD could still yield better results with a different compression function. Due to compute limitations we were ultimately unable to test compression functions other than RLE with NCD. This remains an avenue for future work.

In Figure 9 we note that the hand-crafted pixels behavior characterization performs slightly better after 50 iterations than euclidean distance. This is significant because this indicates that a single metric per frame can replace a 128-element RAM state without incurring significant performance degradation. Recall that in the pixels BC, for each frame we

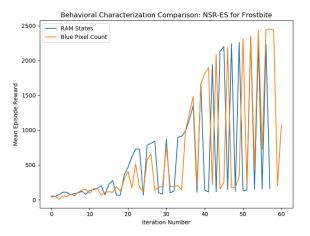


Fig. 9: Comparison of performances of two BCs used. The game being played is Frostbite, and the algorithm used is NSR-ES.

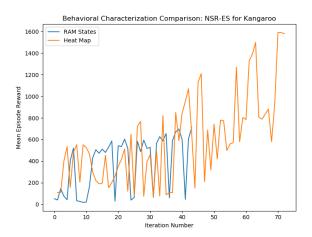


Fig. 10: Comparison of performances of two BCs used. The game being played is Kangaroo, and the algorithm used is NSR-ES.

only use the number of light blue pixels in that frame to represent the state of the game at that frame. That we are able to achieve the same or slightly better performance using two orders of magnitude less information implies that the majority of the elements in the RAM state vector carry extraneous information.

In figure 10 we observe a similar trend which shows that our handcoded BC performs better than the RAM state BC for the same number of iterations. It should be noted that the reason behind there being more data for the heatmap BC is simply that we ran out of compute time when generating results for the RAM state trial. However, we can still analyze differences in the training curves until around 44 iterations, during which time data for both experiments is available. One major advantage of the heatmap approach is that the BC is a fixed length 28 element vector, and does not depend on

the number of timesteps that the agent survives per episode. We believe this much smaller BC contributed to the superior performance observed in the heatmap experiment.

V. DISCUSSION

In this section, we discuss some of the issues we faced along the way, the limitations of our results, and how our work was able to contribute to the state of the art.

A. Irreproducibility of [Conti et al., 2018]'s Results

Though we started our project from [Conti et al., 2018]'s codebase, we were never able to reproduce the results reported in their paper. For example in Frostbite, their results reported an average score of 367.4 for ES, but we achieved an average score of about 1800 using their same code. Contrastingly, they were able to achieve a score of 2978.6 using NSR-ES with their RAM state BC while we only got an average score of about 200. Note that we checked the experiments and codebase and tested with other games as well only to find similar differences.

One of the main differences between our team and theirs is the amount of computational power available to them. Though [Conti et al., 2018] were able to train their models for 2 billion frames in about 2 hours, we estimate that it would take approximately 12 days to achieve a similar amount of training time on our machines (which was infeasible for obvious reasons). Though we did try to replicate their results by training the models for over 12 hours, due to the difference in training time, we cannot conclusively say that their code works or not.

However, since we were trying to build off of their code and improve on their codebase, this also means that it is hard to trust our own results if we cannot trust the underlying starter code.

B. Problems With Results

The results obtained from the approaches discussed in this paper are not significant improvements over the results obtained from prior work [Conti et al., 2018], and we believe this to be due to issues in the codebase upon which our approaches were developed. Due to time limitations and especially due to scarce access to compute resources, we were ultimately unable to troubleshoot the reasons behind the discrepancies between the results obtained, and those reported in the literature using the code provided. Despite this, we believe that a correct implementation of the approaches presented in this paper will result in incremental improvements to the results published in [Conti et al., 2018].

VI. FUTURE WORK

Despite the work in this paper on researching the effects of custom, handcoded BCs for different Atari games, there is much future work that can be done. This section will discuss the following potential extensions to our research:

- Tuning novelty search parameters
- Different methods of combining novelty and fitness
- Combining multiple BCs

- Implementing actual quality diversity algorithms
- · Driving search for novelty using human input
- · Learning BCs instead of handcoding them
- Using NCD with a different compression function

First of all, there are several parameters of novelty search that can be tuned for better performance as shown in [Gomes et al., 2015]. These parameters include the size of the archive, the number of nearest neighbors used, and varying the underlying evolution algorithm used (e.g. genetic algorithms, NEAT, etc.).

Secondly, one could try different methods of combining novelty and fitness scores. For example, the results of [Conti et al., 2018] combined novelty and fitness by simply weighting each score by 50% for their NSR-ES implementation. For their NSRA-ES implementation, they dynamically weighted the two based on the stagnation of performance. In their implementation, they start with a 100% weighting for performance until performance has not increased in the past X iterations. At this point, they decrease the performance weighting and increase the novelty weighting until performance starts to go back up again and then reset the performance weighting back to 100%. Instead of these arbitrary weighting schemes, one can try using a multi-objective optimization approach with pareto-based ranking such as NSGA-II [Deb et al., 2002].

Thirdly, one can try a different approach to BCs. Instead of painstakingly altering the underlying BC to make it more aligned with performance, one can accept the fact that BC are likely to be unaligned anyway and just try to drive the search using multiple combined BCs. The results of [Pugh et al., 2016] have shown that combining multiple BCs can improve robustness against deception while still maintaining diversity provided that one BC targets diversity and the other BC drives the search.

Fourthly, the implementations in [Conti et al., 2018] simply hack together novelty and performance to approximate quality diversity through weighted averages. It would be very interesting to see how well-known quality diversity (QD) algorithms [Pugh et al., 2015] such as novelty search with local competition (NSLC) [Lehman and Stanley, 2011b] and multi-dimensional archive of phenotypic elites (MAP-Elites) [Mouret and Clune, 2015] perform instead.

Fifthly, one could try using human input to direct the search for novelty instead of fully automating it. The results of [Woolley and Stanley, 2014] are similar to typical interactive evolutionary computation (IEC), where the user helps direct the evolution process by choosing from an onscreen population of behaviors, except that the user can now decide to choose to produce 'novel' descendants. Their work showed that human input can help novelty search find good solutions significantly faster than purely automated searches.

Finally, one can even try learning the behavior characterizations instead of handcoding them. One approach is by using autoencoders to automatically learn which state representations actually matter (though of course they can also learn things that do not matter or even worse things disregard important features). Or, one could try the approach

used in [Meyerson et al., 2016]. This approach uses stochastic policy induction (SPIRIT) to learn new BCs from generic BCs. The results were shown to work well on the classic maze domain, but it would be interesting to see how this approach fares on the Atari game domain.

VII. CONCLUSION

We present a number of potential modifications to the original work of [Conti et al., 2018] which applies novelty search to evolutionary strategies in the domain of Atari games, specifically with regards to the composition and comparison of behavior characterizations. Per our experiments, the results obtained [Figures 9, 10] support our initial hypothesis that the RAM state is a sub-optimal behavior characterization that contains additional data which is non-critical for behavior space traversal. We are able to achieve slightly superior results by using much smaller behavior characterizations that are derived from analysis of screenshots of the Atari game state. We believe that smaller behavior characterization vectors are beneficial for behavior space exploration as the reduce the dimensionality of the space to be traversed.

We experiment with another similarity metric with which BCs are compared, NCD (as opposed to euclidean distance which is used in [Conti et al., 2018]). This approach yields results that are significantly worse than those obtained from the original algorithm using euclidean distance. It remains to be seen however whether NCD used with a compression algorithm other than RLE might yield better results.

Lastly, we offer a number of future avenues that follows from the work presented in this paper. Although the data collected for this paper is rather limited due to time and compute constraints, the data obtained in this project provides a decent starting point for further exploration of more behavior characterizations.

REFERENCES

[Cilibrasi and Vitanyi, 2005] Cilibrasi, R. and Vitanyi, P. M. (2005). Clustering by compression. IEEE Trans. Inf. Theor., 51(4):1523–1545.

[Conti et al., 2018] Conti, E., Madhavan, V., Such, F. P., Lehman, J., Stanley, K. O., and Clune, J. (2018). Improving exploration in evolution strategies for deep reinforcement learning via a population of noveltyseeking agents. In *Proceedings of the 32Nd International Conference* on Neural Information Processing Systems, NIPS'18, pages 5032–5043, USA. Curran Associates Inc.

[Deb et al., 2002] Deb, K., Pratap, A., Agarwal, S., and Meyarivan, T. (2002). A fast and elitist multiobjective genetic algorithm: Nsga-ii. *IEEE transactions on evolutionary computation*, 6(2):182–197.

[Gomes et al., 2015] Gomes, J., Mariano, P., and Christensen, A. L. (2015). Devising effective novelty search algorithms: A comprehensive empirical study. In *Proceedings of the 2015 Annual Conference on Genetic and Evolutionary Computation*, pages 943–950. ACM.

[Gomez, 2009] Gomez, F. J. (2009). Sustaining diversity using behavioral information distance. In *Proceedings of the 11th Annual Conference on Genetic and Evolutionary Computation*, GECCO '09, pages 113–120, New York, NY, USA, ACM.

[Lehman and Stanley, 2011a] Lehman, J. and Stanley, K. O. (2011a). Abandoning objectives: Evolution through the search for novelty alone. Evol. Comput., 19(2):189–223.

[Lehman and Stanley, 2011b] Lehman, J. and Stanley, K. O. (2011b). Evolving a diversity of virtual creatures through novelty search and local competition. In *Proceedings of the 13th Annual Conference on Genetic and Evolutionary Computation*, GECCO '11, pages 211–218, New York, NY, USA. ACM.

- [Liwei Wang et al., 2005] Liwei Wang, Yan Zhang, and Jufu Feng (2005). On the euclidean distance of images. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 27(8):1334–1339.
- [Meyerson et al., 2016] Meyerson, E., Lehman, J., and Miikkulainen, R. (2016). Learning behavior characterizations for novelty search. In *Proceedings of the Genetic and Evolutionary Computation Conference* 2016, pages 149–156. ACM.
- [Mnih et al., 2013] Mnih, V., Kavukcuoglu, K., Silver, D., Graves, A., Antonoglou, I., Wierstra, D., and Riedmiller, M. (2013). Playing atari with deep reinforcement learning. In NIPS Deep Learning Workshop.
- [Mouret and Clune, 2015] Mouret, J.-B. and Clune, J. (2015). Illuminating search spaces by mapping elites. arXiv preprint arXiv:1504.04909.
- [Pountain, 1987] Pountain, D. (1987). Run-length encoding. *Byte* 12(6):317–319.
- [Pugh et al., 2016] Pugh, J. K., Soros, L. B., and Stanley, K. O. (2016). Searching for quality diversity when diversity is unaligned with quality. In *International Conference on Parallel Problem Solving from Nature*, pages 880–889. Springer.
- [Pugh et al., 2015] Pugh, J. K., Soros, L. B., Szerlip, P. A., and Stanley, K. O. (2015). Confronting the challenge of quality diversity. In Proceedings of the 2015 Annual Conference on Genetic and Evolutionary Computation, pages 967–974. ACM.
- [Woolley and Stanley, 2014] Woolley, B. G. and Stanley, K. O. (2014). A novel human-computer collaboration: combining novelty search with interactive evolution. In *Proceedings of the 2014 annual conference on genetic and evolutionary computation*, pages 233–240. ACM.