$$G = V(G) + E(G)$$

 $v \in V(G) \leftrightarrow v \text{ is a node}$
 $ij \in E(G) \leftrightarrow i \text{ is adjacent to } j$

Cartesian Product Definition

$$(i,j) \in V(G \times H) \leftrightarrow (i \in V(G) \land i \in V(H))$$

Or

$$V(G \times H) = V(G) \times V(H)$$

$$(i,j)(k,l) \in E(G \times H) \leftrightarrow (i \in V(G) \land j \in V(H) \land k \in V(G) \land l \in V(H)) \land ((i = k \land jl \in E(H)) \lor (j = l \land ik \in E(G))$$