

4. (30%) Let A, B, C and D be sets such that $A \neq \emptyset$ and $B \neq \emptyset$. Prove that if $(A \times B) \cup (B \times A) = C \times C$, then $A = C$.