**3.** (30%) Prove that P1, P2, P3  $\vdash$  C.

P1:  $(\forall x)(\forall y)((P(x) \land Q(y)) \Rightarrow R(x,y))$ 

P2:  $(\exists x)(\forall y)((P(x) \land S(x,y)) \Rightarrow Q(y))$ 

P3:  $(\forall x)(\exists y)(P(x) \land \sim R(x,y) \land T(x,y))$ 

 $C: (\exists x)(\exists y)(P(x) \land \sim S(x,y) \land T(x,y))$