2. (15%) Given P1:
$$(\forall x)(\forall y)((P(x) \land Q(y)) \Rightarrow R(x,y))$$

P2:
$$(\exists x)(\forall y)((P(x) \land S(x,y)) \Rightarrow Q(y))$$

P3:
$$(\forall x)(\exists y)(P(x) \land \sim R(x,y) \land T(x,y))$$

C:
$$(\exists x)(\exists y)(P(x) \land \sim S(x,y) \land T(x,y))$$

Prove that P1, P2, P3 \vdash C.