

# Learning to Augment: Non-Autoregressive Translation

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## Abstract

## 1 Introduction

**High level pitch** MLE is bad when the model is misspecified. Outside of language (ie in non-autoregressive image and audio synthesis), GANs have found success at training misspecified models. Within language, GANs are plagued by unstable training (high variance grad estimators). However, seq-KD approaches, which also serve to simplify data, have been successful. We seek to improve upon seq-KD, which does not take into account the model we wish to train. **/High level pitch**

Learned models of data are often misspecified. When the goal of modeling is not density estimation but some alternative objective, this misspecification may lead to undesirable behaviour under the maximum likelihood objective. In this note, we consider learned data augmentation techniques to edit each data point so that the augmented data is more amenable to a particular model class, while preserving the properties we care about.

A concrete example of a setup where maximum likelihood may not be desirable is non-autoregressive translation, which we focus on in this note. In translation, the goal is to translate a source sentence from one language into a sentence in a different target language. The success of translation is measured by the BLEU score between our generated translation and the true reference target sentence. As the BLEU score is not a function of distributional closeness to the true data, translation systems often discard distributional information and output a single translation of a source sentence. However, the training objective is still often maximum likelihood, a function of the model distribution.

In the case of non-autoregressive translation, this results in undesirable behaviour. As non-autoregressive models cannot model output dependencies, resulting models trained via maximum likelihood using the true distribution often have pathological errors due to misspecification, and therefore poor BLEU scores. We aim to resolve this via data augmentation.

Prior work shows that distillation is a successful data augmentation approach. We instead rely on neural editor models [Guu et al., 2017], which are a trainable alternative to data augmentation [Akyürek et al., 2021].



Figure 1: The graphical model for the generative model (left) and approximate posterior (right).

## 2 Problem Setup

Given a source sentence  $x$ , our goal in translation is to model the target sentence  $y$ . We approach this problem with the following generative model:

- Given the source sentence  $x$ , we choose a proposal translation from a nonautoregressive (NAR) translation model  $\hat{y} \sim p(\hat{y} | x)$
- We choose a noise vector  $z \sim p(z | x)$  from a conditional prior
- We choose a final translation  $y \sim p(y | \hat{y}, z, x)$  from an edit model

This yields the joint distribution

$$p(y, \hat{y}, z | x) = p(y | \hat{y}, z, x)p(\hat{y} | x)p(z | x)$$

The generative model is shown in Figure 1.

For training, optimizing the log marginal likelihood of the translation

$$p(y | x) = \sum_{\hat{y}} \int_z p(y, \hat{y}, z | x),$$

is intractable due to the combinatorial space of possible translations and the integral over  $z$ . We instead resort to approximate inference, in particular variational inference. We introduce the approximate posteriors  $q(z | y, x)$  and  $q(\hat{y} | z, y, x)$ , yielding the following lower bound

$$\begin{aligned} \log p(y | x) &= \log \sum_{\hat{y}} \int_z p(y, \hat{y}, z | x) \\ &= \log \sum_{\hat{y}} \int_z q(\hat{y} | z, y, x) q(z | x) \frac{p(y, \hat{y}, z | x)}{q(\hat{y} | z, y, x) q(z | x)} \\ &\geq \sum_{\hat{y}} \int_z q(\hat{y} | z, y, x) q(z | x) \log \frac{p(y, \hat{y}, z | x)}{q(\hat{y} | z, y, x) q(z | x)} \\ &= \mathbb{E}_{q(\hat{y}|z,y,x)q(z|x)} \left[ \log \frac{p(y, \hat{y}, z | x)}{q(\hat{y} | z, y, x) q(z | x)} \right] \\ &= \mathbb{E}_{q(\hat{y}|z,y,x)q(z|x)} [\log p(y | \hat{y}, z | x)] - D_{\text{KL}} [q(\hat{y} | z, y, x) || p(\hat{y} | x)] - D_{\text{KL}} [q(z | y, x) || p(z | x)]. \end{aligned}$$

**Approximate edit vector posterior** We parameterize  $q(z \mid y, x)$  with a Transformer and some continuous distribution, and estimate its gradient with a pathwise derivative estimator. Alternatively we can use a discrete distribution and REINFORCE (enumeration).

**Approximate translation proposal posterior** For  $q(\hat{y} \mid z, y, x)$ , we have a couple options for parameterization. Before we discuss those options, we note non-autoregressive models (both  $q(\hat{y} \mid z, y, x)$  and  $p(\hat{y} \mid x)$ ) require first predicting length, then each word independently, resulting in the following factorization:  $p(\hat{y}) = p(l) \prod_t (y_t \mid l)$ . We can now cover parameterizations and gradient estimators. There are two axes of variation: do we perform parameter sharing, and do we relax estimators. For parameter sharing, that means we can

- Introduce new parameters for  $q(\hat{y} \mid l, z, y, x)$
- Use the prior  $q(\hat{y} \mid l, z, y, x) = p(\hat{y} \mid l, x)$

Additionally, we can use either the REINFORCE gradient estimator or use Concrete relaxations of each  $p(\hat{y}_t \mid l)$ . The latter would allow us to estimate gradients with a pathwise derivative estimator. The former would require some care due to high variance. One approach to variance reduction could be to use a baseline (self-critical, LOO, RELAX), in combination with multi-sample estimators (Rao-Blackwellization or sampling without replacement or stochastic beam search).

**Fixing a fatal Flaw: constraining  $\hat{y}$**  The augmented data  $\hat{y}$  is completely unconstrained in this scenario, leading to the possibility that the model can learn an informative  $\hat{y}$  that is not useful for translation. Normally, this would be prevented by the likelihood  $p(y \mid \hat{y}, z)$ . However, if the likelihood is too flexible (as will likely be the case for us),  $\hat{y}$  must be constrained via other means. In particular, we can use posterior regularization. This could entail adding an expectation constraint that ensures that the approximate translation proposal posterior does not deviate too far from a pretrained translation model  $p^*(y \mid x)$  trained via normal means:

$$\mathbb{E}_{q(\hat{y} \mid z, y, x)} \left[ \log \frac{q(\hat{y} \mid z, y, x)}{p^*(\hat{y} \mid x)} \leq \epsilon \right].$$

Alternatively, we can fix a pretrained NAT prior  $p(\hat{y} \mid x)$  and train the edit model to completion, then train another model on the generated data.

## 3 Experiments

### Toy experiments

- Take set of strings and tie-break synonyms
- Augment PCFG-generated data into NAT (tree synonyms, movement)

**Improving distillation** Start with NAT model trained with distillation, and output of distillation’s teacher model as  $\hat{y}$ . Run variational EM and see if anything improves.

64 **Improving EM+Distillation** Start with NAT model trained with EM+distillation, and output of  
 65 distillation’s teacher model as  $\hat{y}$ . Run variational EM and see if anything improves.

66 **Denoising Data2Text** Data2Text datasets often contain noisy text that is not represented in the  
 67 data. Can we learn to filter that out? How would we measure success?

## 68 4 A Closer Look at Search

If we fix the teacher model, we can frame the problem following the formulation by Sun and Yang [2020]: Our goal is to find the dataset  $\hat{Y} = (\hat{y}_i)_i$  by solving

$$\begin{aligned} & \max_{\hat{Y}} \max_q \sum_i \log q(\hat{y}_i | x) \\ & \text{subject to } \log \frac{p(y_i | x)}{p(\hat{y}_i | x)} \leq \epsilon, \forall i, \end{aligned} \quad (1)$$

69 which looks for a dataset that is high probability under a non-autoregressive student model  $q(y | x)$ ,  
 70 but also high probability under a baseline autoregressive model  $p(y | x)$  (relative to the ground truth  
 71 translation).

We approach this bilevel optimization problem via an iterative method. At each iteration, we generate a new dataset  $\hat{Y}$  by, for each example  $x_i \in X$ , generating  $J$  translations  $y_{i,j}$  that satisfy the likelihood ratio constraint. We then solve the following problem to determine which examples to keep:

$$\begin{aligned} & \text{maximize } \max_q \sum_i \sum_j \alpha_{i,j} \log q(\hat{y}_{i,j} | x) \\ & \text{subject to } \log \frac{p(y_{i,j} | x)}{p(\hat{y}_i | x)} \leq \epsilon, \forall i, j, \\ & \sum_j \alpha_{i,j} = 1, \forall i, \\ & \alpha_{i,j} > 0, \forall i, j, \end{aligned} \quad (2)$$

72 where the parameter of interest  $\alpha$  is a vector of weights corresponding to each generated datapoint.  
 73 We can use methods in bilevel optimization to solve this problem. For the next iteration, we seed  
 74 search for each example  $x_i$  using the generated  $\hat{y}_{i,j}$  with the highest score  $\alpha_{i,j}$ .

75 In order to generate  $\hat{Y}$  for each iteration, we perform DFS using the teacher model  $p(y | x)$ .  
 76 At each iteration, sample a subset of indices  $I \subset \mathcal{I}$  (sorry, undefined notation). For that subset,  
 77 perform DFS until  $J$  examples that satisfy the likelihood ratio constraint are found (throw in some  
 78 random samples from past search). Save the stack (memory!). Resume from the given stack when  
 79 further examples are needed.

80 While we can prune the search space using the likelihood ratio constraint, there will likely be  
 81 many examples that satisfy the constraint but are not suitable for the student model  $q$ . Additionally,  
 82 the student model  $q$  ties the datapoints  $\hat{y}_i$  together globally, meaning that an example may not have

83 been good given the other examples, but changing the other examples may lead to a globally better  
 84 dataset. Unfortunately, solving this exactly is intractable, so we are stuck with our heuristic.

85 **added** We look to search to solve this problem. However, in practice, the search space is  
 86 exponentially large and infinite, consisting of all translations  $y$  for each source sentence  $x$ . However,  
 87 we can use the log-odds constraint to prune much of the search space. Similar to the admissible  
 88 heuristic used by Stahlberg and Byrne [2019] to perform exact search, we hope that the constraint  
 89 prunes enough of the search space to make optimization tractable. **Get this empirically: find out**  
 90 **how much of the beam /proposals satisfy constraint.**

91 **Is there a way to formalize modes?**

92 **Exploring modes with editor model**

93 One issue with this is that the score under a model may not be a good indication of an equivalent  
 94 translation. Possible fix: NLI?

## 95 **5 Optimizing BLEU**

Formulate the following optimization problem

$$\begin{aligned} & \text{maximize } \max_q \sum_i \log q(\hat{y}_i | x) \\ & \text{subject to } \text{BLEU}(y, \hat{y}) \geq \delta. \end{aligned} \quad (3)$$

96 Unfortunately, neither the objective nor the constraint are separable. The objective contains a nested  
 97 optimization problem, so decoupling that will not be fruitful. However, we can decouple an approx-  
 98 imation of the constraint.

## 99 **6 Problem Setup: Bilevel Optimization (not updated)**

100 Source sentence  $x$ , target sentence  $y$ . True translation distribution  $p(y | x)$ .

101 We propose to, given a family of student models  $q_\theta(y | x)$ , learn an edit model  $q_\phi(\hat{y} | y, x)$   
 102 whose conditional distribution over  $\hat{y}$  is easier for the student model  $q_\theta$  to learn. Learning an inter-  
 103 mediate distribution will allow the student model to focus on only modeling the important aspects  
 104 of the true distribution.

To accomplish this, we propose to solve the following optimization problem

$$\operatorname{argmin}_{\phi} D_{\text{KL}} \left[ p(y | x) \parallel \sum_y q_\phi(\hat{y} | y, x) p(y | x) \right] + \min_{\theta} D_{\text{KL}} [q_\phi(\hat{y} | y, x) \parallel q_\theta(\hat{y} | x)]. \quad (4)$$

This is a bilevel optimization problem, where we want to find the edit model that is able to balance  
 faithfulness to the true data (the first term) as well as learnability of the student model (the second  
 term). We refer to Equation 4 as the outer problem, and the second term as the inner problem:

$$\operatorname{argmin}_{\theta} D_{\text{KL}} [q_\phi(\hat{y} | y, x) \parallel q_\theta(\hat{y} | x)]. \quad (5)$$

The first term of the outer problem, the KL divergence between the true distribution and the marginal posterior of the edit distribution, serves as a regularizer and encourages the marginal distribution of the edit distribution combined with the data distribution to be close to the original data distribution. As this setting may be both too restrictive as well as not example-specific, we also consider the following variation:

$$\operatorname{argmin}_{\phi} \sum_y \Omega(y, q_{\phi}(\hat{y} \mid y, x)) + \min_{\theta} D_{\text{KL}} [q_{\phi}(\hat{y} \mid y, x) \parallel q_{\theta}(\hat{y} \mid x)], \quad (6)$$

105 allowing us to perform instance-level regularization rather than distributional.

## 106 7 Method 1: The Exact Setting

107 We first make the simplifying assumption that we can solve the inner problem exactly. In order to  
108 then solve the full outer problem, we will differentiate through the solution of the inner problem. In  
109 full generality, this would require an application of the implicit function theorem, or approximations  
110 through sampling or incomplete optimization.

### 111 7.1 Experiment: Length-2 Binary Strings + Non-autoregressive Student

112 Our first experiment will determine whether training an edit model is possible in a very simple  
113 setting, where we can compute the solution to the inner problem (training the student model given  
114 an edit model) in closed form, and subsequently differentiate through that procedure.

We restrict our attention to distributions over target sentences that are binary strings of length 2 without conditioning on a source sentence. In particular, our true distribution takes the form

$$y = b_1 \cdot 00 + b_2 \cdot 01 + b_3 \cdot 10 + b_4 \cdot 11,$$

where  $b \sim \text{Cat}(\lambda)$ , represented as a one-hot sample (meaning only one of  $b_i$  can be 1, while the rest must be 0). As we are interested in disambiguation, we first focus on the case where  $b_1, b_4 \approx 0$ , and  $b_2 < b_3$ . The edit model then takes the form

$$q_{\phi}(\hat{y} \mid y) = [\phi]_{\hat{y}, y},$$

where  $\hat{y}, y \in \{0, 1\}^2 = \mathcal{Y}$  and  $\phi \in [0, 1]^{\mathcal{Y} \times \mathcal{Y}}$ . The student is nonautoregressive, and has the form

$$q_{\theta}(\hat{y}) = \prod_t q_{\theta}(\hat{y}_t) = [\theta]_{1, \hat{y}_1} \cdot [\theta]_{2, \hat{y}_2},$$

115 where  $\theta \in [0, 1]^{2 \times \mathcal{Y}}$ .

In this setting, we can exactly compute the solution of the inner problem,

$$\operatorname{argmin}_{\theta} \mathbb{E}_y [D_{\text{KL}} [q_{\phi}(\hat{y} \mid y) \parallel q_{\theta}(\hat{y})]] = \operatorname{argmin}_{\theta} \mathbb{E}_y \left[ \sum_{\hat{y}} q_{\phi}(\hat{y} \mid y) (\log q_{\phi}(\hat{y} \mid y) - \log q_{\theta}(\hat{y})) \right],$$

and differentiate through it. The minimizer is given by

$$\begin{aligned} [\theta]_{1,0} &= \sum_y \sum_{\hat{y}} p(y) q_{\phi}(\hat{y} | y) 1(\hat{y}_1 = 0) \\ [\theta]_{2,0} &= \sum_y \sum_{\hat{y}} p(y) q_{\phi}(\hat{y} | y) 1(\hat{y}_2 = 0) \\ [\theta]_{t,1} &= 1 - [\theta]_{t,0}, \end{aligned}$$

116 which is differentiable wrt  $\phi$ .

117 **Results** We find that the editor model is able to disambiguate the true data and produces a new  
 118 data distribution with no dependencies across time, resulting in a distribution that is easier for the  
 119 student to match. We see the results of training the editor model with the following conditions:

- 120 •  $b = [0.001, 0.45, 0.54, 0.001]$
- 121 • Editor is initialized to uniform everywhere except the transitions from  $[0,1]$  and  $[1,0]$ , where  
 122 transitions to  $[0,0]$  and  $[1,1]$  are given low mass in order to speed up training
- 123 • We recompute the parameters of the student by solving the inner problem at every iteration
- 124 • We solve the outer problem via gradient descent (1k iterations, learning rate of  $1e-3$ )

125 We see in Figure 2 (right) that the editor learns to bias the data further towards  $[1, 0]$ . This results  
 126 in the student model being very certain, as seen in Figure 3 (right). In this very simple setting, the  
 127 bilevel optimization formulation successfully increases the asymmetry of the data.

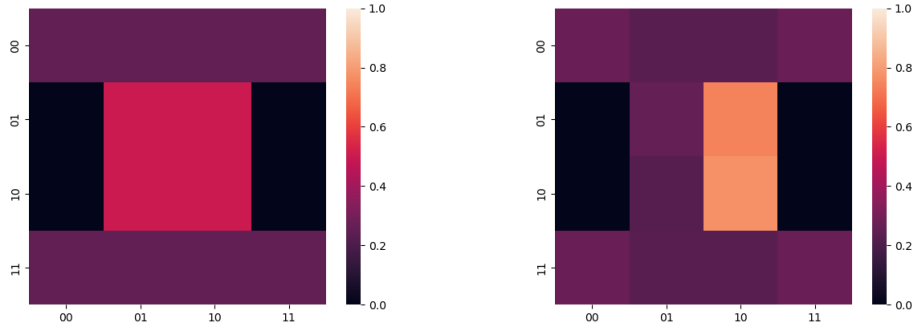


Figure 2: The emission probabilities for the editor model at the start of training (left) and end of training (right).

128 However, in settings where the true data distribution is less skewed, the objective does not allow  
 129 the edit model to deviate too far. Figures 4 and 5 show the results when  $b = [1e-3, 0.5, 0.5, 1 - e3]$ .  
 130 In this setting, both the data distribution and edit distribution are symmetric, resulting in the student  
 131 remaining at a standstill. This is because any movement away from the true distribution would incur  
 132 too large a penalty in the first term of the objective,  $D_{\text{KL}} \left[ p(y) || \sum_y q(\hat{y} | y) p(y) \right]$ .

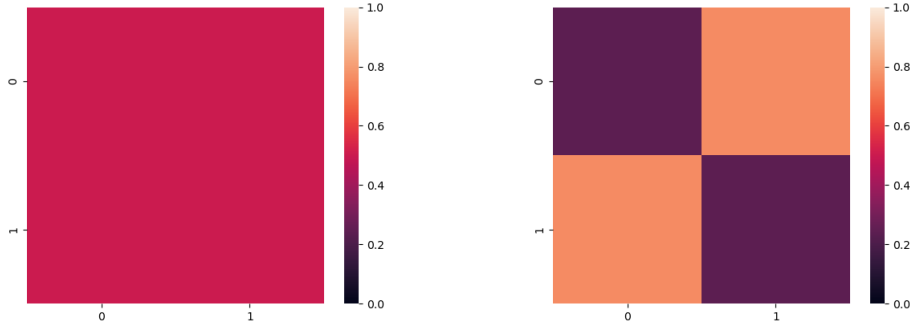


Figure 3: The emission probabilities for the student model at the start of training (left) and end of training (right).

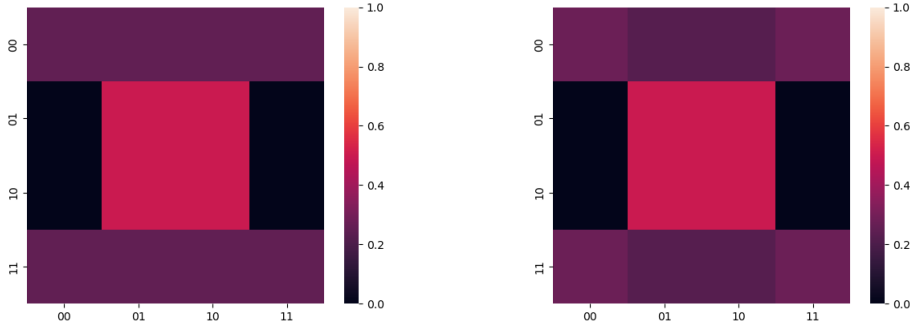


Figure 4: The emission probabilities for the editor model at the start of training (left) and end of training (right) with an even true data distribution.

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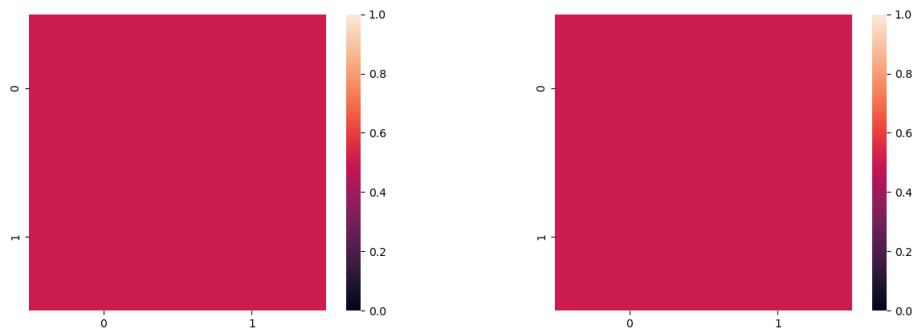


Figure 5: The emission probabilities for the student model at the start of training (left) and end of training (right) with an even true data distribution.