

A Appendices

A.1 Hyperparameters

For Penn Treebank and Wikitext-2, we trained the following baselines: a two layer feed-forward 5-gram model and a two layer LSTM. The feedforward model is given by the following:

$$p(w_t | \mathbf{w}_{<t}) = W_x \text{ReLU}(\text{Conv}(\mathbf{E}_w(\mathbf{w}_{t-4:t-1}))) \quad (6)$$

where \mathbf{E}_w gives the word embeddings and $W_x \in \mathbb{R}^{|\mathcal{X}| \times h}$ is weight-tied to the embeddings.

For the feedforward model we use a batch size of 128 and a bptt length of 64, as we found the model needed a larger batch size to train. For the LSTM, we use a batch size of 16 and a BPTT length of 32. For both baseline models we use a learning rate of 1e-3 and a dropout rate of 0.3 on the activations in the model. Both models use a hidden dimension of 256 throughout. These same hyperparameters were applied on both Penn Treebank and Wikitext-2.

For the HMMs we use a batch size of 16 and a BPTT length of 32. We use state dropout with $\lambda = 0.5$. We use a learning rate of 1e-2 for Penn Treebank, and a learning rate of 1e-3 for Wikitext-2.

All weights are initialized with the Kaiming uniform initialization.

Hyperparameter search was performed manually, using validation perplexity.

A.2 HMM Parameterization

We use the following residual network:

$$\begin{aligned} f_i(E) &= g_i(\text{ReLU}(EW_{i1})) \\ g_i(D) &= \text{LayerNorm}(\text{ReLU}(DW_{i2}) + D) \end{aligned} \quad (7)$$

with $i \in \{\text{out}, \text{in}, \text{emit}\}$.

For the factored state embeddings in Sec. 4, we apply f to obtain

$$\begin{aligned} \mathbf{H}_{\text{out}} &= f_{\text{out}}(f_o([\mathbf{E}_m, \mathbf{E}_z])) \\ \mathbf{H}_{\text{in}} &= f_{\text{in}}(f_i([\mathbf{E}_m, \mathbf{E}_z])) \\ \mathbf{H}_{\text{emit}} &= f_{\text{emit}}(f_e([\mathbf{E}_m, \mathbf{E}_z])) \end{aligned} \quad (8)$$

A.3 Emission constraint ablation

Tbl. 3 shows the results from emission constraint ablations. For the ablations in this section, we do not use the factored state embedding and instead

Constraint	$ \mathcal{Z} $	$ \mathcal{C}_x $	m	Val PPL
Brown	16384	512	32	137
Brown	16384	256	64	138
Brown	16384	128	128	134
Brown	16384	64	256	136
None	1024	-	-	180
Brown	1024	256	4	182
Brown	1024	128	8	194
Uniform	8192	128	-	150
Brown	8192	128	64	142
Uniform	16384	128	-	146
Brown	16384	128	128	136

Table 3: Emission constraint ablations on Penn Treebank.

directly learn embeddings $\mathbf{E}_z \in \mathbb{R}^{|\mathcal{Z}| \times h}$. We examine the effect of factored state embeddings in the next section.

With a VL-HMM that has $|\mathcal{Z}| = 2^{14}$ states, the model is insensitive to the number of blocks M . However, with fewer states $|\mathcal{Z}| = 2^{10}$ where we are able to use fewer blocks to examine whether the block-sparsity of the emission results in a performance loss. With $M = 4$ blocks, the block-sparse HMM matches an unconstrained HMM with the same number of states. When $M = 8$, the block-sparse model underperforms, implying there may be room for improvement with the larger HMMs that use $M > 8$ blocks.

We additionally compare the blocks induced by Brown clustering with a uniform constraint that samples subsets of states of size n independently and uniformly from \mathcal{Z} . This does not admit a partitioning, which makes it difficult to apply state dropout. We therefore zero out half of the logits of the transition matrix randomly before normalization. In the bottom of Tbl. 3, we find that models with uniform constraints are consistently outperformed by models with Brown cluster constraints as measured by validation perplexity. The models with uniform constraints also had poor validation performance despite better training performance, a symptom of overfitting.

These ablations demonstrate that the constraints based on Brown clusters used in this work may not be optimal, motivating future work that learns sparsity structure.

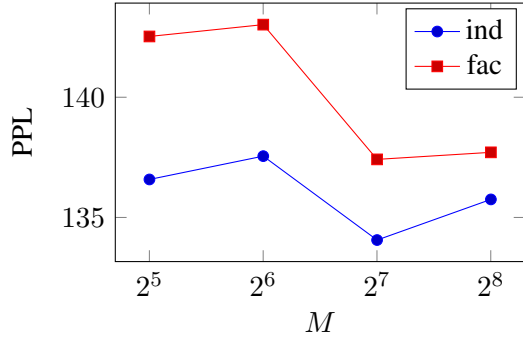


Figure 4: Perplexity on PTB by state size $|\mathcal{Z}|$ ($\lambda = 0.5$ and $M = 128$).

A.4 Factored state embedding ablation

The results of the factored state ablation are in Fig. 4. We find that the performance of independent state embeddings with is similar to a model with factored embeddings, until the number of blocks is ≤ 64 .