

“FSA”  
Fisheries Stock Assessment Package



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# What does FSA do?

“A variety of simple fish stock assessment methods” ([Ogle 2013](#)).

Covers:

- Age comparisons
- Age-length relationships
- Size structures
- [Weight-Length Relationships](#) (`wrAdd`)
- Abundance from capture-recapture data
- [Depletion Methods for Estimating Abundance](#)
- Mortality rates
- Growth rates
- Recruitment (in partnership with other packages)
- [Catch Curve Estimates of Mortality](#) (`catchCurve`)

# What conservation problems can the package be used for?

## Package

Fisheries management,  
including:

- health of a fish population and its environment
- finding the population size of closed populations
- estimating mortality rate

## Model(s)

- `catchCurve` = linear regression
- `weight-length` = linear regression
- `depletion` = linear regression
- other functions use different models

# Unique Insight!

The FSAdat package can be used to get datasets that correspond to packages in FSA

- `help.search("Weight-Length",package=c("FSAdat","FSA"))`
- `help.search("Depletion",package=c("FSAdat","FSA"))`
- `help.search("Catch curve",package=c("FSAdat","FSA"))`
- `help.search("Size Structure",package=c("FSAdat","FSA"))`

# Weight-Length Model Overview

$$Wr = \frac{W}{Ws} * 100$$

Relative weight →

↑

Weight of individual fish

Standard weight (for fish of the same length)

# Weight-Length Data

	netID	fishID	species	length	weight	year
1	206	501	Bluegill	1.5	0.7	2008
2	205	502	Bluegill	1.7	1.4	2008
3	205	503	Bluegill	2.2	1.5	2008
4	205	504	Bluegill	2.1	1.4	2008
5	205	505	Bluegill	1.5	1.0	2008
6	205	506	Bluegill	1.9	1.8	2008

Data should look something like this: weight  
and length for individual fish in a species

# Weight-Length Example

Fisheries managers want to assess the health of a fish population and its environment for management

OR

They are concerned about how a fish population is doing

▲	netID	fishID	species	length	weight	year
1	17	199	Bluegill	5.6	59.0	2007
2	20	201	Bluegill	5.5	54.0	2007
3	15	203	Bluegill	5.6	40.0	2007
4	15	206	Bluegill	5.8	30.0	2007
5	15	207	Bluegill	4.7	20.0	2007
6	16	210	Bluegill	9.0	280.0	2007
7	16	211	Bluegill	8.8	260.0	2007
8	16	212	Bluegill	8.8	260.0	2007
9	16	213	Bluegill	8.8	240.0	2007
10	16	214	Bluegill	5.9	60.0	2007
11	16	215	Bluegill	5.4	60.0	2007
12	21	217	Bluegill	3.7	14.0	2007
13	21	219	Bluegill	5.1	38.0	2007
14	26	220	Bluegill	5.2	49.0	2007

# Weight-Length Example

```
#wrAdd() calculates the relative weight for each fish based on the standard weight equation for that species
bluegill_2007_weights <- wrAdd(weight~length_mm+species, data=bluegill_2007) #calculates relative weight

#add to the dataframe
bluegill_2007 <- bluegill_2007 %>%
  mutate(relative_weight = bluegill_2007_weights)
````
```

|   | netID | fishID | species  | length | weight | year | length_mm | relative_weight |
|---|-------|--------|----------|--------|--------|------|-----------|-----------------|
| 1 | 17    | 199    | Bluegill | 5.6    | 59.0   | 2007 | 142       | 101.82721       |
| 2 | 20    | 201    | Bluegill | 5.5    | 54.0   | 2007 | 140       | 97.68619        |
| 3 | 15    | 203    | Bluegill | 5.6    | 40.0   | 2007 | 142       | 69.03540        |
| 4 | 15    | 206    | Bluegill | 5.8    | 30.0   | 2007 | 147       | 46.16331        |
| 5 | 15    | 207    | Bluegill | 4.7    | 20.0   | 2007 | 119       | 62.01779        |
| 6 | 16    | 210    | Bluegill | 9.0    | 280.0  | 2007 | 229       | 99.07032        |
| 7 | 16    | 211    | Bluegill | 8.8    | 260.0  | 2007 | 224       | 98.98079        |
| 8 | 16    | 212    | Bluegill | 8.8    | 260.0  | 2007 | 224       | 98.98079        |

# Weight-Length Example

```
#find the average relative weight by size class
```{r}
#for bluegill research groups them into the following classes:
## <8 cm
## <15 cm
## <20 cm
## <25 cm
## <30 cm
#approximate length at maturity for bluegill is 15cm, so the first two size classes are juveniles

#categorize each fish into its size class
bluegill_2007 <- bluegill_2007 %>%
  mutate(class = ifelse(length_mm < 80, "young_of_year", ifelse(length_mm < 150, "juvenile", ifelse(length_mm < 200, "adult_1", ifelse(length_mm < 250, "adult_2", "adult_3")))))

#the relative weight function doesn't work for fish in the young of year class for this species (they're too
short), so we can compare juveniles to different classes of adults

bluegill_2007_summary <- bluegill_2007 %>%
  group_by(class) %>%
  summarize(mean_relative_weight = mean(relative_weight, na.rm = TRUE))
```

# Weight-Length Example

class	mean_relative_weight
<chr>	<dbl>
adult_1	89.82584
adult_2	96.11699
juvenile	79.45157
young_of_year	NaN

Bluegills in different life phases in this particular lake differ in how healthy they are, and by extension how ideal their environment is for them

All Bluegill in this population are skinnier than expected for the species, so management may be necessary

# Catch Curve Overview

Linear Regression Basis:

$$C_t = vN_0 e^{-Zt}$$

Diagram illustrating the components of the catch curve equation:

- catch of fish at age t
- initial population size
- time
- instantaneous total mortality parameter
- proportion vulnerable to fishery (constant)

The diagram shows the catch curve equation  $C_t = vN_0 e^{-Zt}$  enclosed in a white box. Five arrows point from labels to specific parts of the equation:

- An arrow points from "catch of fish at age t" to the variable  $C_t$ .
- An arrow points from "initial population size" to the variable  $N_0$ .
- An arrow points from "time" to the variable  $t$ .
- An arrow points from "instantaneous total mortality parameter" to the coefficient  $-Z$ .
- An arrow points from "proportion vulnerable to fishery (constant)" to the coefficient  $v$ .

# Catch Curve Inputs

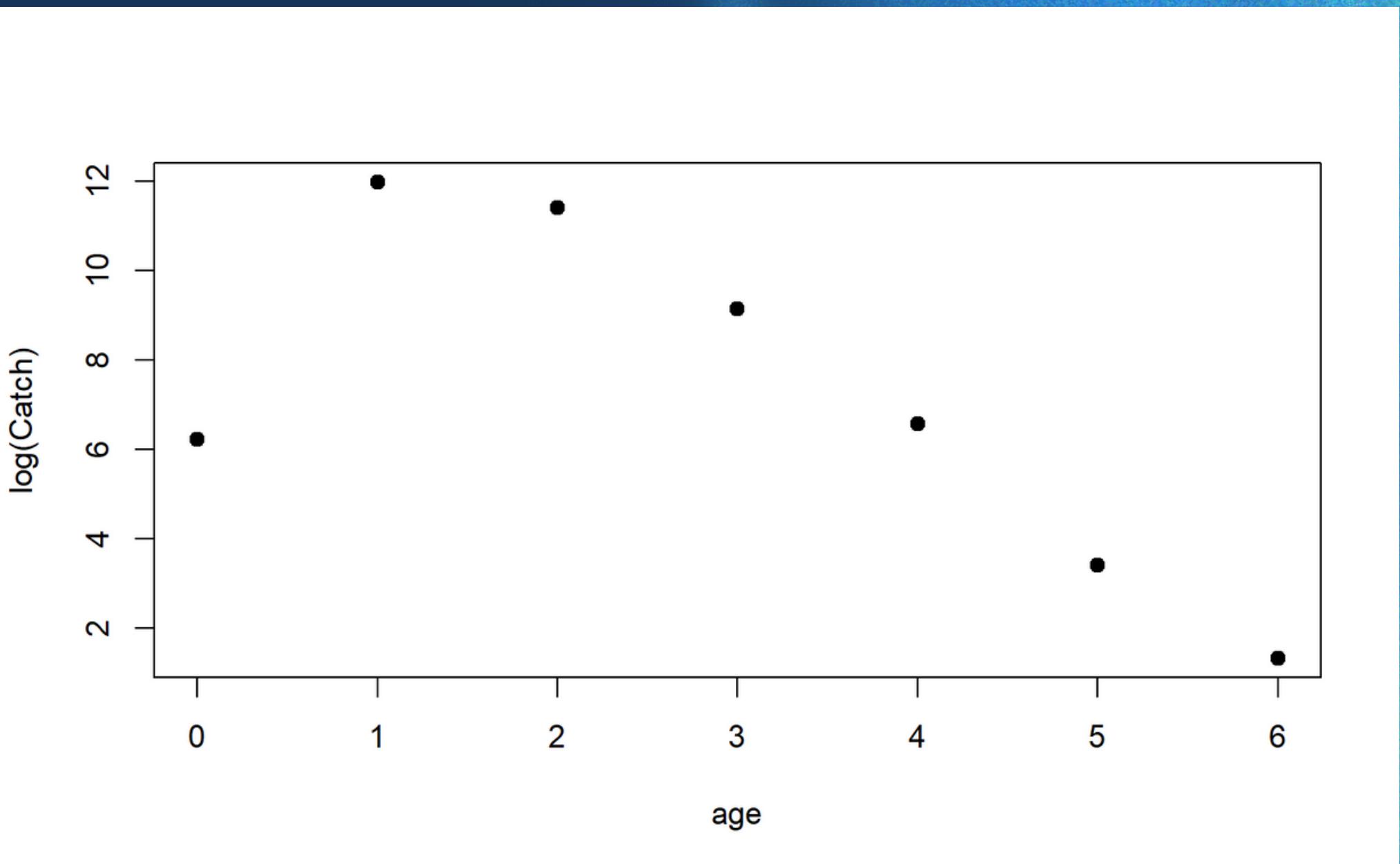
AGE	CATCH	LOG(CATCH)
0	501.9	6.2
1	161219.8	12.0
2	90815.0	11.4
3	9419.4	9.2

The dataframe should consist of two columns: age and catch per age class (both must be numeric), then you calculate log(catch) for plotting

# Catch Curve Example

Fisheries managers can use this to determine the annual mortality rate of a population

```
plot(logct~age,data=data,ylab="log(Catch)",pch=19)
```



# Catch Curve Example

weighted linear regression  
will reduce the relative  
impact of older ages with  
fewer fish

```
catchCurve(  
  x,  
  catch,  
  ages2use = age,  
  weighted = FALSE,  
  negWeightReplace = 0,  
  ... )
```

`x` = formula of the form `catch~age`  
`ages2use` = numeric vector of ages that  
define the descending limb of the catch curve  
`use.weights` = logical that indicates whether a  
weighted regression should be used

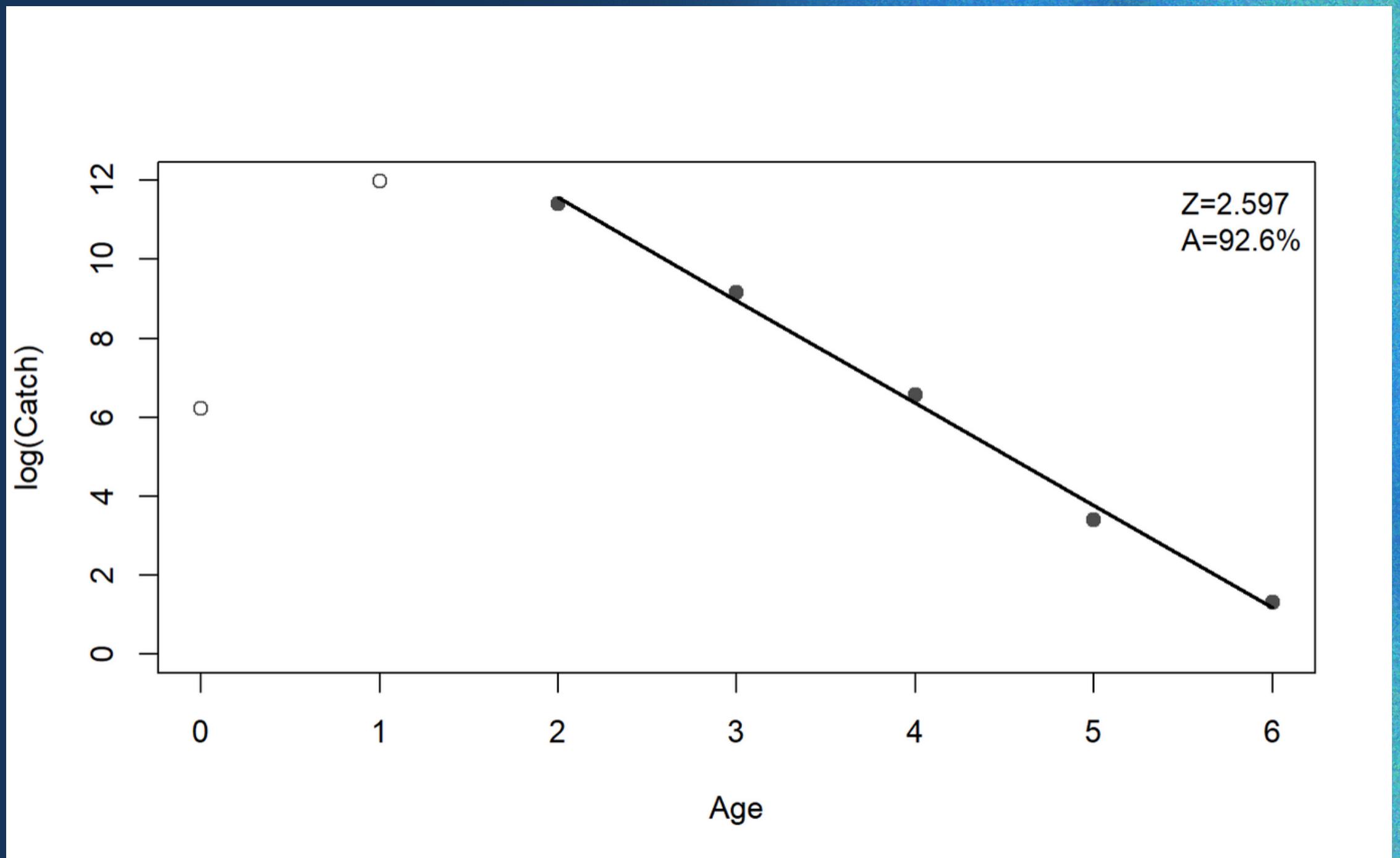
## Example:

```
weighted_results <- FSA::catchCurve(catch~age, data=data,  
ages2use=2:6, use.weights=TRUE)
```

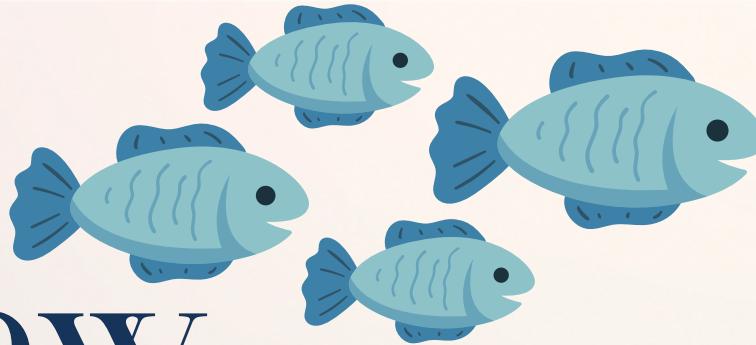
# Catch Curve Example

Annual mortality rate  
for this population is  
92.6%

**Z** = instantaneous  
mortality rate  
**A** = annual  
mortality rate



# Depletion Model Overview



## What does it do?

- Estimates the total population size for a closed population
- The ‘depletion’ refers to the removal of fish from the population

## How does it do it?

3 Methods for Estimating Abundance

1. Leslie Method
2. DeLury Method
3. K-Pass Method

## Why is this useful?

- For management
- Species-habitat relationships
- Measuring recovery status
- How removal of fish affect relative abundance

# Leslie Method

$$\frac{C_t}{f_t} = qN_0 - qK_t$$

initial number of fish in the population

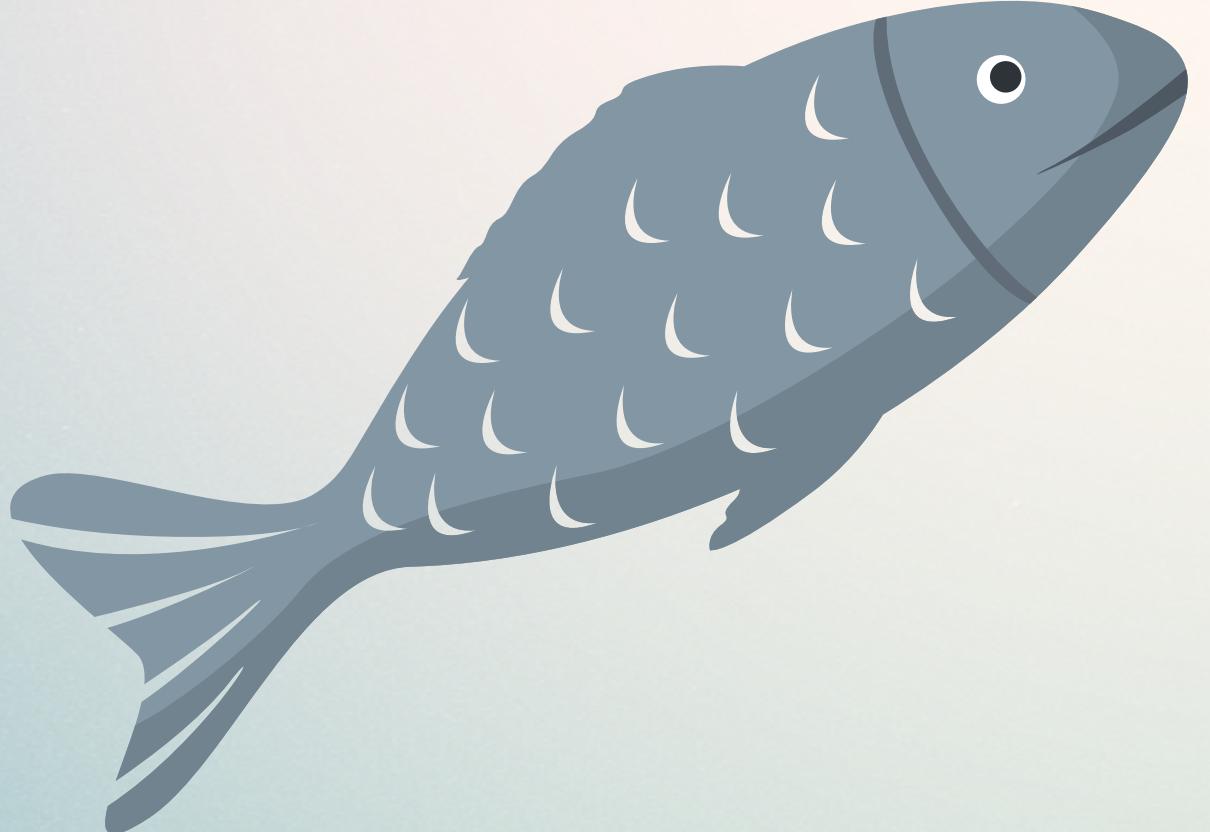
amount of current catch

catch-per-unit-effort (CPUE)

level of effort for the  $t$ th removal (last removal)

catchability coefficient

cumulative catch prior to the  $t$ th removal



# Leslie Method Broken Down

Before actually using the package, it is important to understand how to calculate everything!

Step 1: Enter catch and effort into R as data frames

```
> mac <- data.frame(catch=c(7,7,4,1,2,1),effort=c(10,10,10,10,6,10))
```

Step 2: Calculate CPUE or CPE

- catch/effort

```
> mac$cpe <- mac$catch/mac$effort  
> mac  
  
  catch effort    cpe  
1     7      10 0.7000  
2     7      10 0.7000  
3     4      10 0.4000  
4     1      10 0.1000  
5     2       6 0.3333  
6     1      10 0.1000
```

Step 3: Find K

- This is just the cumulative sum of the catch which is the addition of all prior values

```
> mac$K <- cumsum(mac$catch)-mac$catch  
> mac  
  
  catch effort    cpe    K  
1     7      10 0.7000    0  
2     7      10 0.7000    7  
3     4      10 0.4000   14  
4     1      10 0.1000   18  
5     2       6 0.3333   19  
6     1      10 0.1000   21
```

# Leslie Method Broken Down

Step 4: Set up the regression

```
> lm1 <- lm(cpe~K,data=mac)
```

Step 5: Slope and intercept are extracted from the model

```
> coef(lm1)
(Intercept)          K
0.78643      -0.03019
```

Step 6: Calculate q (which is K) and N0 (the intercept)

```
> ( q.hat <- -coef(lm1)[2] )
K
0.03019
> ( N0.hat <- coef(lm1)[1]/q.hat )
(Intercept)
26.05
```

**There are an estimated 26 age-0 largemouth bass in the 0.11 ha enclosure!**

# Leslie Method with depletion()

Skipped defining the catch and effort data frame here since it was already done previously (this could also be loaded in through an excel file)

Immediately get NO and q!

There are between 17 and 36 age-0 largemouth bass in the enclosure and the catchability coefficient is between 0.009 and 0.061.

Can then plot it!

```
> lm2 <- with(mac,depletion(catch,effort,ricker.mod=TRUE))
> summary(lm2)

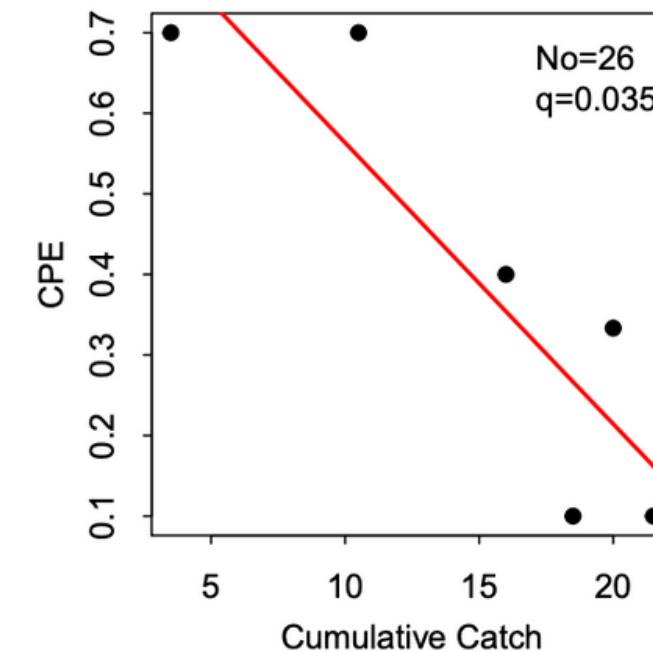
The Leslie method was used.

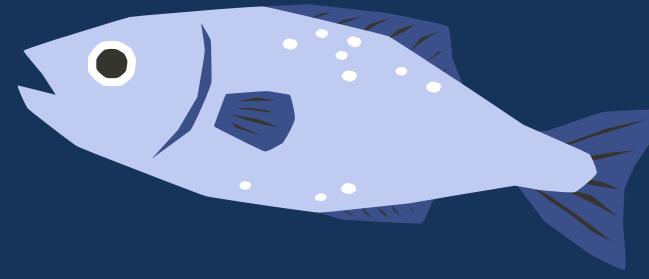
Estimate Std. Err.
No 26.14071 3.383672
q   0.03491  0.009253

> confint(lm2)

      95% LCI 95% UCI
No 16.746130 35.5353
q   0.009217  0.0606
```

```
> plot(lm2)
```





# Assumptions and Downfalls of Leslie

## ASSUMPTIONS

1. Population is closed
2. Catchability is constant
3. Enough fish are removed to reduce catch-per-unit-effort
4. The catches remove 2% of the population
5. All fish will be caught by method of capture
6. The units of effort are independent

## POPULAR VIOLATIONS

1. Closed population
2. Catchability
3. Human error

# DeLury Method

Use this method when the fraction of the stock removed by unit of fishing effort is really small ( less then 2%)

$$\log\left(\frac{C_t}{f_t}\right) = \log(qN_0) - qE_t$$

log of CPUE

log of catchability  
coefficient and  
initial population  
size

cumulative effort  
prior to time t

# DuLury Method with depletion()

Used catch and effort data frame that was made earlier.

Again, you get NO and q as well as the confidence intervals.

```
> lm4 <- with(mac,depletion(catch,effort,"Delury",ricker.mod=TRUE))  
> summary(lm4)
```

The Delury method was used.

Estimate Std. Err.

No 23.66606 5.84805

q 0.04165 0.01489

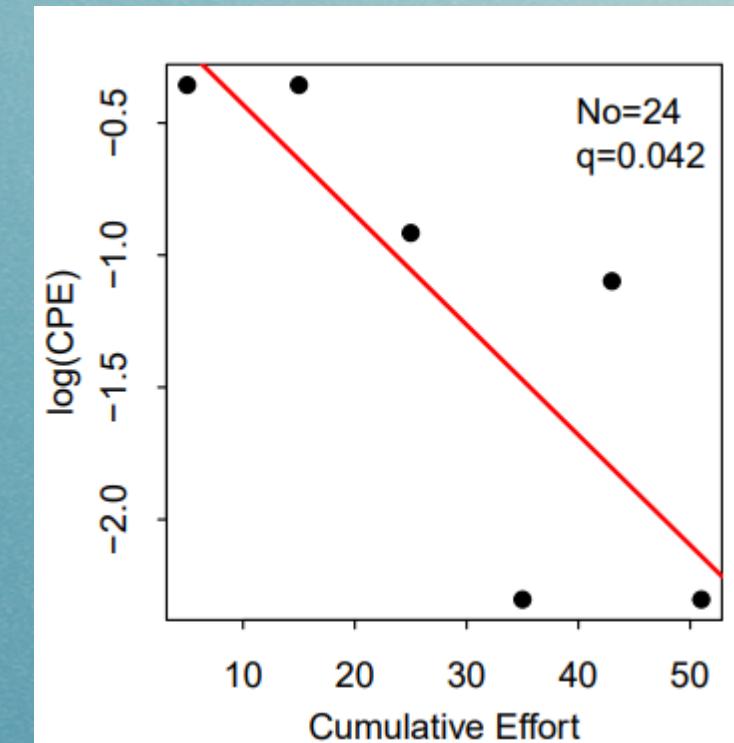
```
> confint(lm4)
```

95% LCI 95% UCI

No 7.4292678 39.90285

q 0.0003136 0.08298

```
> plot(lm4)
```



# K-Pass Method

Most accurate depletion method for estimating population size!!

successive captures

probability of capture

$q = 1-p$  or the probability of escape

$$L(\vec{C} | N_0, p) = \frac{N_0! p^T q^{kN_0 - X - T}}{(N_0 - T)! \prod_{i=1}^k C_i!}$$

initial population size

total number of removal periods

number of individuals captured in the first removal period

$$X = \sum_{i=1}^k (k - i) C_i$$

$$T = \sum_{i=1}^k C_i$$

total number of individuals captured

# K-Pass Method Broken Down

Before actually using the package, it is important to understand how to calculate everything!

Step 1: Enter the three capture amounts

```
> ( ct <- c(187,77,35) )  
[1] 187 77 35
```

Step 2: Can then compute k, T and X

```
> ( k <- length(ct) )      # number of removals  
[1] 3  
> ( T <- sum(ct) )        # total catch  
[1] 299  
> i <- seq(1,k)           # needed to compute X below  
> ( X <- sum((k-i)*ct) )  
[1] 451
```

# K-Pass Method Broken Down

Step 3: Can then plug everything into the really scary equation

```
> mle <- function(N0) { (N0+0.5)*((k*N0-X-T)^k) - (N0-T+0.5)*((k*N0-X)^k) }
```

Step 4: You then continue to plug in different variations of N0 into the function until you get an answer that is negative

```
> mle(300) # must start >T  
[1] 878409227  
  
> mle(330) # arbitrarily picked this  
[1] -363778799  
  
> mle(320) # between 320 and 330  
[1] 132897577  
  
> mle(325) # between 320 and 325  
[1] -105113899  
  
> mle(322) # between 322 and 325  
[1] 40171398  
  
> mle(323) # first negative >T, done  
[1] -7430898
```

**There are an estimated 323 rainbow trout less than 85 mm in this stretch of stream**

# K-Pass Method with removal()

Still used data frame from before.

Now get NO and p.

```
> pr1 <- removal(ct)
> summary(pr1)

The Zippin's K-Pass Removal Method method was used.

      Estimate Std. Error
No 323.0000    8.41582
p   0.5772    0.03557

> confint(pr1)

      95% LCI  95% UCI
No 306.5053 339.4947
p   0.5075  0.6469
```

# Advantages & Limitations

## Depletion

**Advantages:** efficient package, has multiple ways of finding the total population size, each method requires slightly different types of data, can be used for more than just fish

**Limitations:** can be biased, human error is easily achieved, assumptions are often not met

## FSA

**Advantages:** lots of documentation and accessible data; wide array of common fisheries assessment methodologies; coding is relatively straightforward

**Limitations:** weight-length needs pre-existing standard weight function; so many functions it can be hard to find what you need; doesn't do recruitment on its own; documentation is old

# Resources

## Package

- [Package documentation](#)
- [Book with R scripts for various functions](#)
- [Weight-length vignette](#) (Ogle 2013)
- [Catch Curve Estimates of Mortality Vignette](#) (Ogle 2013)
- [Depletion Vignette](#) (Ogle 2013)

## Applications

- Brett T. Miller, Ernesto Flores, D. Scott Waters, Ben C. Neely; An Evaluation of Goldeye Life History Characteristics in Two Kansas Reservoirs. *Journal of Fish and Wildlife Management* 1 June 2022; 13 (1): 243–249. doi: <https://doi.org/10.3996/JFWM-21-090>
- Maceina, M. J., S. J. Rider, and D. R. Lowery. 1993. Use of a catch-depletion method to estimate population density of age-0 largemouth bass in submersed vegetation. *North American Journal of Fisheries Management* 13:847–851. doi:[10.1577/1548-8675\(1993\)0130847:UOACDM2.3.CO;2](https://doi.org/10.1577/1548-8675(1993)0130847:UOACDM2.3.CO;2)

# Portfolio Assignment

## **Depletion:**

Grab a new set of data and use the Leslie, DeLury, and K-Pass methods to calculate the initial population size! Answer the following questions:

1. Compare and contrast the initial population sizes between the three methods
2. Why are the Leslie and DeLury methods not valid at estimating NO?
3. What values can you look at to determine the reliability of the data? (Hint: Think back to what we learned about statistics in 206)

## **Catch Curve:**

1. How do the estimates of Z and A change between the weighted and non-weighted regressions? How does the confidence interval change?

