$Musical\ Dice\ Game\ extbf{-}$ $Minuets\ I$

based on

Ludus Melothedicus ou le Jeu de Dez Harmonique

compiled by I. T. Author





Musical Dice Game - Minuets I

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le Jeu de Dez Harmonique

Author:
I. T. Author

Supervisor:
Dr. Communio Sanctorum

Wonders of the Musical World Series 8



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1 Introduction¹

"LUDUS MELOTHEDICUS OU LE JEU DE DEZ HARMONIQUE Contenat plusieurs Calculs Par lesquels toute personne Composera differents Menuets avec l'accompagnement de Basse en joüant avec de deux Dez même sans sçavior la Musique" "LUDUS MELOTHEDICUS OR
THE HARMONIC GAME OF DICE
Containing several Calculations
By which any person will
Compose different Minuets
with Bass accompaniment
while playing with two Dice themselves
without knowing Music."

Thus run the French title and corresponding English translation of the Musical Dice Game (MDG) that was anonymously authored and was published by Chevardiére: Paris in 1759 (Anonymous, 1759). Rightly and interestingly so, as the Rules provided in this work allow a non-professional musician to generate ("compose") nearly two quadrillions (2×10^{12}) of unique MDG minuets. More precisely, the total number of minuets that the rules of the *Ludus Melothedicus*, as we would refer to this MDG from here onward, yield is:

$$9^{16} = 1.853.020.188.851.841.$$

Of these, $(9^6 \times 8 \times 7) \times (9^7 \times 6) = 854,066,918,318,544$ are unique since three pairs of measures for Part I and three pairs of measures for Part II are identical (see Section 2.2 for more details).

A Musikalisches Würfelspiel (German for "musical dice game" or MDG) is a system for randomly "generating" (e.g., by using a die or two dice) musical compositions from precomposed options and was quite popular throughout Western Europe in the 18th century. The earliest known MDG is Johann Philipp Kirnberger's Der allezeit fertige Polonoisen- und Menuettencomponist (1st ed. 1757; rev. 2nd ed. 1783) (translated from German as "The Ever-Ready Minuet and Polonaise Composer"). Other well-known composers that are to known to have composed a MDG are C.P.E. Bach (Einfall, einen doppelten Contrapunct in der Octave von sechs Tacten zu machen, ohne die Regeln davon zu wissen (1758); translated from German as "A method for making six bars of double counterpoint at the octave without knowing the rules"), Abbé Maximillian Stadler (Table pour composer des minuets et des Trios à la infinie; avec deux dez à jouer (1780); translated from French as "A table for composing minuets and trios to infinity, by playing with two dice"), the latter MDG being also attributed to Franz Joseph Haydn.

Probably the most famous of MDGs is Musikalisches Würfelspiel K. 516f (1787). This MDG was first published by J.J. Hummel in 1793 in Berlin and was republished in 1796 by Nikolaus Simrock in Bonn (as K. 294d or K. Anh. C 30.01). Simrock attributed this work to Wolfgang Amadeus Mozart. It is also known under the title of Anleitung zum Componieren von Walzern so viele man will vermittelst zweier Würfel, ohne etwas von der Musik oder Composition zu verstehen (German for "Instructions for the composition of as many waltzes as one desires with two dice, without understanding anything about music or composition") and may have been based on Mozart's manuscript K. 516f, written in 1787, consisting of numerous two-bar fragments of music, that appear to be some kind of game or system for constructing music out of two-bar fragments, but contains no instructions nor hints as to the use of dice. An online article by Hideo Noguchi offers a possible explanation for this attribution.

For this book, we generate MDG minuets based on the rules given in the second edition of *Ludus Melothedicus*. Fifty (50) such MDG minuets are given toward the latter part of this book. The scores of these generated minuets were initially written using the abc environment of Chris Walshaw, then converted to Scalar Vector Graphics (SVG) images (with corresponding MIDIs) using abcm2ps and abcmidi, and then pre-processed with Inkscape to be included in LATEX to produce this book.

¹The information contained in the introduction were culled from the following online resources: *Ludus Melothedicus*, ou *Le eu de Dez Harmonique*, 2nd ed. (1759), Wikipedia: *Musikalisches Würferspiel* (2017), https://opus-infinity.org/, and Mozart's Melody Machine (Peterson, 2001)

2 Ludus Melothedicus

2.1 Rules

The Rules provided in *Ludus Melothedicus* generate minuets consisting of 16 bars/measures that may be divided into two parts of eight bars each. Each part is played with a repeat. All told, a total of $16 \times 2 = 32$ bars of music is played for each minuet.

The notes for each bar of the minuet are determined by rolling a nine-sided top or die 16 times to get a sequence of integers whose terms are elements of the set {1, 2, 3, 4, 5, 6, 7, 8, 9}. The first eight toss outcomes will be used to create the eight bars of Part I of the minuet, latter eight toss outcomes to create the eight bars of Part II of the minuet, according to the rules given below (not exactly the same as given in the *Ludus Melothedicus* as here, the Table of Measures for Parts I and II have already been constructed before hand; see Section 2.2 for more information).

- 1. To generate the notes for each of the eight bars of Part I of the minuet, simply look up the bar corresponding to the toss outcome (rows) and the current minuet bar number (column) in the Tables of Measures for Part I (Tables 1 and 2).
- 2. Similarly, to generate the notes for each of the eight bars of Part II of the minuet, repeat Step 1 but this time using the Tables of Measures for Part II (Tables 3 and 4).

For example, if we are in the process of creating the fifth bar (Bar 5) of Part I of the minute and the dice outcome was a 3, then we would use the notes in bar number 21 of Figure 1: [V:1] =B2G2=e2 for the G-clef and [V:2] G,2G,2G,2 for the F-clef.

The suggested accompaniments are a violin for the G-clef and bass or cello for the F-clef.

2.2 How to Generate the Table of Measures

To generate the Table of Measures $((9 \times 8) \times 2 = 144; 144 \times 2 = 288 \text{ bars in all, since there are nine (9)}$ possible die rolls, eight (8) bars for each part, two clefs (G and F) per part, and two parts: I and II) shown in Figure 1, 2, 3, and 4, these measures being that for minuets in the Key of D, the notes (drawn in clefs) given in pages 6 (G-clef) and 7 (F-clef), and the tables for note numbers given in pages 8 to 11 of *Ludus Melothedicus* are used.

For example if a 2 is rolled for the first bar, then we use the table of note numbers given on page 8 of Ludus Melothedicus (this particular table is reproduced below with annotations on how to obtain the note numbers that are to be used to find the notes from those given on pages 6 and 7; see Figure 1). Since we rolled a 2, we start at the first box (containing 66) and count this as the 3rd box, then count until the ninth box to land on the box containing 108, and use this as the first note number. We then take the numbers in every ninth box thereafter until there are no more boxes to be counted, keeping in mind that on even rows we go from right to left, we skip empty boxes, and that 0s are simply disregarded. When two numbers appear in a box, e.g., 75/71, two notes are obtained and a double string is played.

Hence, when a 2 is rolled for the first bar of Part I of the minuet to be written in the Key of D, the note numbers to be used are: 108, 103, 190, 108, 113, 195, 111, 114, and 189. Looking at the G- and F-clefs on pages 6 and 7 of *Ludus Melothedicus*, we obtain the notes (in abc notation): [V:1] dAd^f=eg and [V:2] D,2^F,2^C,2, where notes corresponding to note numbers less than 120 are assigned to the violin ([V:1]) and notes corresponding to note numbers greater than 119 are assigned to the bass/cello ([V:2]). In addition, whenever there is an excess of obtained notes to a bar, a succession of three (3) half notes may have to be played as a triplet or an eight note may have to be played as a grace note.

1st Measure 108 103 A

Table 1: Table of note numbers to be used when a 2 is rolled for bar 1, Part I of minuets in the Key of D. Thus when a 2 is rolled for the first bar of Part I of the minuet, the note numbers of the notes to be used are: 108, 103, 190, 108, 113, 195, 111, 114, and 189 (box highlighted with light green). The notes corresponding to these note numbers are obtained from the G- and F-clefs given in pages 6 and 7 of *Ludus Melothedicus*. These yield the notes (in abc notation): [V:1] dAd^f=eg and [V:2] D,2^F,2^C,2.

Additional examples are given in pages 4 and 5 of *Ludus Melothedicus*. These are summarized in Tables 2 and 3 below.

Bar	Roll	Note Numbers for Notes to be Used (Part I))
1	2	108, 103, 190, 108, 113, 195, 111, 114, and 189
2	8	114, 24, 190, 0, 189, 81, 0, 185, and 0
3	3	113, 117, 190, 195, 114, 111, 196, 105, and 111
4	2	77, 105, 107, 198, 73, 196, 195, and 0
5	9	233, 228, 224, 223, 17, 114, 113, 111, and 193
6	7	108, 19, 233, 230, 226, 224, 78, 223, and 218
7	9	111, 103, 84, 189, 113, 114, 117, 193, and 190
8	2	0, 0, 198, 51, 193, 185, and 0

Table 2: Examples for obtaining note numbers for the eight bars of Part I of the minuet in the Key of D (see page 4 of *Ludus Melothedicus*). Note that 0s are disregarded when looking up for notes.

Bar	Roll	Note Numbers for Notes to be Used (Part II)
1	5	27, 190, 195, 113, 103, 0, 190, 0, and 0
2	5	105, 101, 196, 100, 96, 190, 71, and 183
3	3	105, 111, 114, 119, 196, 232, 196, 0, and 78
4	4	107, 111, 102, 198, 193, 185, 15, and 0
5	6	75, 233, 224, 0, 221, 218, 25, 217, and 215
6	9	108, 19, 233, 226, 78, 224, 226, 223, and 218
7	8	105, 103, 101, 140, 100, 98, 96, 198, 95, 96, and 98
8	7	190, 233, 217, 213, 217, 37, and 0

Table 3: Examples for obtaining note numbers for the eight bars of Part II of the minuet in the Key of D (see page 5 of $Ludus\ Melothedicus$). Note that 0s are disregarded when looking up for notes.

2.3 Table of Measures

The Table of Measures for Part I of the minuets based on *Ludus Melothedicus* are given in Figures 1 and 2, that follow while that for Part II are given in Tables 3 and 4. The notes of the bars in these four tables were generated based on *Ludus Melothedicus*.

Roll Outcomes as Parts: 1.2.3.4.5.6.7.8.9

Paris: La Chevardière, 1759



Figure 1: Table of Measures - Part I (Page 1/2)



Figure 2: Table of Measures - Part I (Page 2/2)

Roll Outcomes as Parts: 1.2.3.4.5.6.7.8.9

Paris: La Chevardière, 1759



Figure 3: Table of Measures - Part II (Page 1/2)



Figure 4: Table of Measures - Part II (Page 2/2)

Note that except for Bars 4 and 8 for Part I, there are nine (9) possible choices for measures to be played. Furthermore,

- 1. for Bar 4 of Part I, the notes for die rolls 2 and 3 are the same.
- 2. for Bar 8 of Part I, the notes for die rolls 1 and 5, and those for rolls 2 and 7 are the same.

Thus, for Bar 4 of Part I has only 8 choices for bars to be played and Bar 8 of Part I has only 7 such choices.

For Part II, the first seven bars each have nine (9) possible choices for measures to be played. Bar 8 (final bar) of Part II has three pairs of identical measures: Bars 1 and 6 are the same, as are Bars 2 and 7, and Bars 4 and 9. These yield only six (6) possible choices for measures to be played for Bar 8, Part II. All told, the total number of unique MDG minuets based on *Ludus Melothedicus* is equal to

$$\underbrace{(9^6 \times 8 \times 7)}_{\text{Part II}} \times \underbrace{(9^7 \times 6)}_{\text{Part II}} = 854,066,918,318,544.$$

3 Related Links

The following are very interesting sites in that they allow the online rendering of MDGs:

- Opus Infinity Collaborative work of Robbert Harms, Hein Moors, and Suus van Petegem whose goal is to unravel the mystery behind the tables used for generating MDGs. Site visitors can generate MDGs based on works of Kirnberger, Mozart, Stadler/Haydn, Bach, Gerlach, and Callegari (1st Cahier). Corresponding audio files (mid, ogg, and/or mp3) and image files (pdf or png) are also made available for listening, viewing, or downloading.
- Mozart A site maintained by John Chuang that allows the site visitor to generate MDGs based on the work of Stadler/Haydn.
- Mozart A site maintained by Marian Aldenhövel allows the visitor to generate a MDG (user-specified or randomly-generated) and the corresponding audio (midi, wav) and image files (pdf, png) based on *Musikalisches Würferspiel*, K. 516f.
- mozart.zip This is a Windows software (© 1995 VisionSoft) by John Chuang and Stephen Goodwin that generates MDG based on input from user and is available for *free* from Amaranth Publishing.
- "Mozart Musical Game in C K. 516f," Mozart Studies Online The site of Hideo Noguchi that offers an explanation linking Musikalisches Würferspiel, K. 516f, and K. 294d (K. Anh. C 30.01).

4 Acknowledgments

Special thanks to International Music Score Library Project for Ludus Melothedicus, ou Le Jeu de Dez Harmonique, 2nd ed. (1759), Opus Infinity for additional related information, and Amaranth Publishing for a copy of mozart.zip. My sincerest gratitude to Chris Walshaw et al. for the ABC music notation; Jean-Francois Moine for abcm2ps and the accompanying examples, templates, and pointers for the appropriate use of these resources; Guido Gonzato for the ABC Plus Project and the abcmidi resources available there, more especially for the ABC resource book Making Music with ABC 2; James R. Allwright and Seymour Shlien for abcmidi source and binaries; Artifex, Inc. for Ghostscript v.10.00.0 (includes the ps2pdf converter); Inkscape v.1.2.2 for the tool for converting SVGs to PDFs for inclusion into LATEX documents; William Schelter for Maxima v.5.47.0—used for computing the permutation number; Google Lens and Google Translate for aiding in producing the English versions of the text of Ludus Melothedicus; Colomban Wendling et. al for Geany 2.0 IDE; and User: Martin H for his reply to a TFX / LATFX Stack Exchange question on including SVGs into LATFX documents. Thanks to Ditto to Machtelt Garrels for the book Bash Guide for Beginners, Vivek Gite for the book Linux Script Shell Tutorial, and Steve Parker for the Unix/Linux Shell Cheatsheet. John Fogarty's GitHub Site: Latex CreateSpace BookCover and Peter Wilson's reply in TFX / LATFX Stack Exchange on designing a book cover, were sources of ideas, information, and materials for creating the book cover and title page, thanks to both of them; LibreOffice Calc for its use in the image creation of the book cover. Many thanks, too, to the Debian Project for the Debian 12 (Bookworm) GNU/Linux OS, TexLive for providing the T_FX distribution, and GitHub for its generosity in providing space for the project.

5 Fifty (50) Selected Minuets based on *Ludus Melothedicus*

This section contains an example of 50 minutes that were generated using the Rules in Section 2.1.

1-1-5-5-2-6-9-3-2-9-6-8-6-9-6-5



For audio (midi): ldmt-1-1-5-5-2-6-9-3-2-9-6-8-6-9-6-5.mid

1 - 4 - 8 - 8 - 6 - 7 - 2 - 3 - 2 - 1 - 4 - 8 - 5 - 4 - 7

ldmt::1:26:59:60:61:46:55:16::17:10:3:28:61:38:31:56::

Perm. No.: 198254246756761



For audio (midi): ldmt-1-4-8-8-8-6-7-2-3-2-1-4-8-5-4-7.mid

1 - 5 - 4 - 4 - 7 - 8 - 7 - 1 - 5 - 4 - 5 - 8 - 3 - 8 - 1 - 1

ldmt::1:34:27:28:53:62:55:8::33:26:35:60:21:62:7:8::

Perm. No.: 12854332336906



For audio (midi): ldmt-1-5-4-4-7-8-7-1-5-4-5-8-3-8-1-1.mid

1-9-2-9-5-5-2-9-2-8-5-6-9-2-6-2

ldmt::1:66:11:68:37:38:15:72::9:58:35:44:69:14:47:16::

Perm. No.: 224864226457921



For audio (midi): ldmt-1-9-2-9-5-5-2-9-2-8-5-6-9-2-6-2.mid

1-9-3-1-4-3-2-2-8-6-1-6-3-1-3-4

ldmt::1:66:19:4:29:22:15:16::57:42:3:44:21:6:23:32::

Perm. No.: 459166117237795



For audio (midi): ldmt-1-9-3-1-4-3-2-2-8-6-1-6-3-1-3-4.mid

1 - 9 - 8 - 9 - 4 - 9 - 8 - 9 - 7 - 3 - 1 - 6 - 9 - 1 - 9 - 5

ldmt::1:66:59:68:29:70:63:72::49:18:3:44:69:6:71:40::



For audio (midi): ldmt-1-9-8-9-4-9-8-9-7-3-1-6-9-1-9-5.mid

2 - 1 - 8 - 5 - 4 - 4 - 5 - 9 - 5 - 3 - 8 - 8 - 5 - 8 - 2 - 2

ldmt::9:2:59:36:29:30:39:72::33:18:59:60:37:62:15:16::

Perm. No.: 171412380959996



For audio (midi): 1dmt-2-1-8-5-4-4-5-9-5-3-8-8-5-8-2-2.mid

2-2-1-9-8-4-6-7-9-4-8-8-5-1-6-2

ldmt::9:10:3:68:61:30:47:56::65:26:59:60:37:6:47:16::

Perm. No.: 222375587894498



For audio (midi): ldmt-2-2-1-9-8-4-6-7-9-4-8-8-5-1-6-2.mid

√= 120

2 - 4 - 1 - 8 - 2 - 2 - 7 - 9 - 2 - 2 - 4 - 5 - 5 - 7 - 7 - 5

ldmt::9:26:3:60:13:14:55:72::9:10:27:36:37:54:55:40:: Perm. No.: 675693685589627



For audio (midi): ldmt-2-4-1-8-2-2-7-9-2-2-4-5-5-7-7-5.mid

3-1-5-1-9-1-4-8-3-5-2-9-6-4-1-5

ldmt::17:2:35:4:69:6:31:64::17:34:11:68:45:30:7:40::

Perm. No.: 575803391815983



For audio (midi): ldmt-3-1-5-1-9-1-4-8-3-5-2-9-6-4-1-5.mid

3-2-1-4-4-1-6-4-1-7-4-2-4-7-2-2

ldmt::17:10:3:28:29:6:47:32::1:50:27:12:29:54:15:16::

Perm. No.: 169320905846958



For audio (midi): ldmt-3-2-1-4-4-1-6-4-1-7-4-2-4-7-2-2.mid

3-2-8-5-9-1-8-7-9-2-2-5-6-5-1-7

ldmt::17:10:59:36:69:6:63:56::65:10:11:36:45:38:7:56::

Perm. No.: 150439849716558



For audio (midi): ldmt-3-2-8-5-9-1-8-7-9-2-2-5-6-5-1-7.mid

3-4-1-7-9-3-7-6-8-7-7-3-2-7-5-2

ldmt::17:26:3:52:69:22:55:48::57:50:51:20:13:54:39:16::

Perm. No.: 216407688704499



For audio (midi): ldmt-3-4-1-7-9-3-7-6-8-7-7-3-2-7-5-2.mid

3-4-3-1-4-2-7-8-5-1-4-3-4-1-2-6

ldmt::17:26:19:4:29:14:55:64::33:2:27:20:29:6:15:48::

Perm. No.: 16452599971152



For audio (midi): ldmt-3-4-3-1-4-2-7-8-5-1-4-3-4-1-2-6.mid

3-6-9-6-1-6-5-2-7-4-2-8-6-4-6-8

ldmt::17:42:67:44:5:46:39:16::49:26:11:60:45:30:47:64::

Perm. No.: 797206287751572



For audio (midi): ldmt-3-6-9-6-1-6-5-2-7-4-2-8-6-4-6-8.mid

4-4-2-2-9-7-7-6-5-3-9-9-6-1-7-9

ldmt::25:26:11:12:69:54:55:48::33:18:67:68:45:6:55:72::

Perm. No.: 523099607297449



For audio (midi): ldmt-4-4-2-2-9-7-7-6-5-3-9-9-6-1-7-9.mid

4-4-3-9-9-4-3-1-4-4-5-7-6-1-3-6

ldmt::25:26:19:68:69:30:23:8::25:26:35:52:45:6:23:48::

Perm. No.: 32749117443040



For audio (midi): ldmt-4-4-3-9-9-4-3-1-4-4-5-7-6-1-3-6.mid

4 - 4 - 4 - 9 - 3 - 7 - 8 - 8 - 7 - 4 - 4 - 1 - 4 - 3 - 9 - 4

ldmt::25:26:27:68:21:54:63:64::49:26:27:4:29:22:71:32::

Perm. No.: 557670588806785



For audio (midi): ldmt-4-4-9-3-7-8-8-7-4-4-1-4-3-9-4.mid

4-4-7-8-7-5-3-4-2-6-2-3-3-4-2-5

ldmt::25:26:51:60:53:38:23:32::9:42:11:20:21:30:15:40::

Perm. No.: 590903722108219



For audio (midi): ldmt-4-4-7-8-7-5-3-4-2-6-2-3-3-4-2-5.mid

4-5-5-1-9-5-9-4-7-7-8-1-9-5-7-1

ldmt::25:34:35:4:69:38:71:32::49:50:59:4:69:38:55:8::

Perm. No.: 103506437768764



For audio (midi): ldmt-4-5-5-1-9-5-9-4-7-7-8-1-9-5-7-1.mid

4 - 5 - 6 - 4 - 7 - 4 - 3 - 1 - 8 - 8 - 1 - 4 - 6 - 5 - 7 - 9

ldmt::25:34:43:28:53:30:23:8::57:58:3:28:45:38:55:72::



For audio (midi): ldmt-4-5-6-4-7-4-3-1-8-8-1-4-6-5-7-9.mid

4 - 6 - 6 - 1 - 8 - 4 - 8 - 6 - 2 - 9 - 3 - 4 - 8 - 8 - 4 - 4

ldmt::25:42:43:4:61:30:63:48::9:66:19:28:61:62:31:32:: Perm. No.: 488221917057310



For audio (midi): ldmt-4-6-6-1-8-4-8-6-2-9-3-4-8-8-4-4.mid

4 - 7 - 2 - 1 - 6 - 6 - 6 - 7 - 1 - 1 - 3 - 7 - 5 - 6 - 9 - 1

ldmt::25:50:11:4:45:46:47:56::1:2:19:52:37:46:71:8::

Perm. No.: 136231170162115



For audio (midi): ldmt-4-7-2-1-6-6-6-7-1-1-3-7-5-6-9-1.mid

5 - 2 - 6 - 8 - 5 - 2 - 8 - 7 - 8 - 2 - 3 - 7 - 3 - 4 - 9 - 1

ldmt::33:10:43:60:37:14:63:56::57:10:19:52:21:30:71:8::

Perm. No.: 132326448537785



For audio (midi): ldmt-5-2-6-8-5-2-8-7-8-2-3-7-3-4-9-1.mid

5-3-4-7-2-6-5-6-3-1-8-3-4-4-8-3

ldmt::33:18:27:52:13:46:39:48::17:2:59:20:29:30:63:24::

Perm. No.: 401319492965735



For audio (midi): ldmt-5-3-4-7-2-6-5-6-3-1-8-3-4-4-8-3.mid

5-4-5-4-8-2-6-2-2-9-7-6-7-2-5-5

ldmt::33:26:35:28:61:14:47:16::9:66:51:44:53:14:39:40::

Perm. No.: 635696181288878



For audio (midi): ldmt-5-4-5-4-8-2-6-2-2-9-7-6-7-2-5-5.mid

5 - 5 - 2 - 2 - 9 - 2 - 5 - 3 - 8 - 8 - 8 - 5 - 9 - 2 - 9 - 5

ldmt::33:34:11:12:69:14:39:24::57:58:59:36:69:14:71:40::

Perm. No.: 699331546884443



For audio (midi): ldmt-5-5-2-2-9-2-5-3-8-8-5-9-2-9-5.mid

5-5-8-6-8-9-2-9-3-4-4-2-7-3-5-4

 ${\tt ldmt::33:34:59:44:61:70:15:72::17:26:27:12:53:22:39:32::}$

Perm. No.: 495013730468468



For audio (midi): ldmt-5-5-8-6-8-9-2-9-3-4-4-2-7-3-5-4.mid

6 - 1 - 4 - 8 - 6 - 6 - 9 - 5 - 4 - 3 - 5 - 3 - 1 - 3 - 2 - 6

ldmt::41:2:27:60:45:46:71:40::25:18:35:20:5:22:15:48::

Perm. No.: 19384395329391



For audio (midi): ldmt-6-1-4-8-6-6-9-5-4-3-5-3-1-3-2-6.mid

6 - 3 - 3 - 3 - 4 - 1 - 8 - 4 - 4 - 3 - 8 - 6 - 3 - 7 - 3 - 9

ldmt::41:18:19:20:29:6:63:32::25:18:59:44:21:54:23:72::

Perm. No.: 469726116232587



For audio (midi): ldmt-6-3-3-3-4-1-8-4-4-3-8-6-3-7-3-9.mid

6-4-1-6-6-4-5-3-8-9-5-9-8-3-4-2

ldmt::41:26:3:44:45:30:39:24::57:66:35:68:61:22:31:16::

Perm. No.: 194859715198389



For audio (midi): ldmt-6-4-1-6-6-4-5-3-8-9-5-9-8-3-4-2.mid

6 - 5 - 9 - 8 - 3 - 3 - 2 - 3 - 7 - 5 - 7 - 2 - 7 - 7 - 5 - 6

ldmt::41:34:67:60:21:22:15:24::49:34:51:12:53:54:39:48::

Perm. No.: 75017230051128



For audio (midi): ldmt-6-5-9-8-3-3-2-3-7-5-7-2-7-5-6.mid

6 - 8 - 3 - 1 - 3 - 7 - 7 - 5 - 2 - 5 - 6 - 5 - 9 - 4 - 6 - 9

ldmt::41:58:19:4:21:54:55:40::9:34:43:36:69:30:47:72::

Perm. No.: 513047766378255



For audio (midi): ldmt-6-8-3-1-3-7-7-5-2-5-6-5-9-4-6-9.mid

6-9-1-6-4-8-8-1-7-6-1-5-7-7-4-5

ldmt::41:66:3:44:29:62:63:8::49:42:3:36:53:54:31:40::

Perm. No.: 628630006941546



For audio (midi): ldmt-6-9-1-6-4-8-8-1-7-6-1-5-7-7-4-5.mid

6-9-9-4-3-8-5-3-7-8-3-2-8-6-9-8

ldmt::41:66:67:28:21:62:39:24::49:58:19:12:61:46:71:64::

Perm. No.: 848432961493368



For audio (midi): ldmt-6-9-9-4-3-8-5-3-7-8-3-2-8-6-9-8.mid

7 - 7 - 9 - 1 - 8 - 5 - 2 - 9 - 6 - 5 - 3 - 1 - 7 - 3 - 9 - 1

ldmt::49:50:67:4:61:38:15:72::41:34:19:4:53:22:71:8::

Perm. No.: 131220738232765



For audio (midi): ldmt-7-7-9-1-8-5-2-9-6-5-3-1-7-3-9-1.mid

$7\hbox{-}8\hbox{-}2\hbox{-}1\hbox{-}5\hbox{-}6\hbox{-}5\hbox{-}7\hbox{-}9\hbox{-}5\hbox{-}7\hbox{-}6\hbox{-}8\hbox{-}6\hbox{-}3\hbox{-}7$

ldmt::49:58:11:4:37:46:39:56::65:34:51:44:61:46:23:56::

Perm. No.: 184254367980823



For audio (midi): ldmt-7-8-2-1-5-6-5-7-9-5-7-6-8-6-3-7.mid

8-1-6-7-6-4-6-5-9-1-6-6-5-9-9-3

ldmt::57:2:43:52:45:30:47:40::65:2:43:44:37:70:71:24:: Perm. No.: 426177930984002



For audio (midi): ldmt-8-1-6-7-6-4-6-5-9-1-6-6-5-9-9-3.mid

8 - 3 - 2 - 2 - 6 - 2 - 6 - 5 - 1 - 2 - 8 - 9 - 2 - 2 - 8 - 2

ldmt::57:18:11:12:45:14:47:40::1:10:59:68:13:14:63:16::

Perm. No.: 255200172935948



For audio (midi): ldmt-8-3-2-2-6-5-1-2-8-9-2-2-8-2.mid

8-5-4-7-6-1-8-4-8-1-7-9-1-6-4-6

ldmt::57:34:27:52:45:6:63:32::57:2:51:68:5:46:31:48::

Perm. No.: 56423111315948



For audio (midi): ldmt-8-5-4-7-6-1-8-4-8-1-7-9-1-6-4-6.mid

8-5-9-6-9-8-4-6-7-2-3-6-5-5-8-6

ldmt::57:34:67:44:69:62:31:48::49:10:19:44:37:38:63:48::

Perm. No.: 118636539579872



For audio (midi): ldmt-8-5-9-6-9-8-4-6-7-2-3-6-5-5-8-6.mid

8 - 6 - 4 - 6 - 5 - 5 - 8 - 3 - 4 - 8 - 5 - 8 - 2 - 4 - 7 - 2

ldmt::57:42:27:44:37:38:63:24::25:58:35:60:13:30:55:16::

Perm. No.: 242871576134228



For audio (midi): ldmt-8-6-4-6-5-5-8-3-4-8-5-8-2-4-7-2.mid

8-8-6-6-2-2-7-9-3-3-6-3-8-7-2

ldmt::57:58:59:44:45:14:15:56::65:18:19:44:21:62:55:16::

Perm. No.: 250046783420570



For audio (midi): ldmt-8-8-6-6-2-2-7-9-3-3-6-3-8-7-2.mid

8-9-1-7-5-2-3-8-7-7-4-6-2-5-5-5

ldmt::57:66:3:52:37:14:23:64::49:50:27:44:13:38:39:40::

Perm. No.: 639984296506085



For audio (midi): ldmt-8-9-1-7-5-2-3-8-7-7-4-6-2-5-5.mid

9 - 2 - 2 - 1 - 9 - 7 - 2 - 1 - 2 - 8 - 9 - 3 - 5 - 2 - 4 - 8

ldmt::65:10:11:4:69:54:15:8::9:58:67:20:37:14:31:64::



For audio (midi): ldmt-9-2-2-1-9-7-2-1-2-8-9-3-5-2-4-8.mid

9-2-5-1-2-6-5-8-2-6-9-1-5-9-3-9

ldmt::65:10:35:4:13:46:39:64::9:42:67:4:37:70:23:72:: Perm. No.: 473525998994646



For audio (midi): ldmt-9-2-5-1-2-6-5-8-2-6-9-1-5-9-3-9.mid

9-3-3-9-3-8-8-5-6-9-4-2-3-8-2-3

ldmt::65:18:19:68:21:62:63:40::41:66:27:12:21:62:15:24::

Perm. No.: 313228144696644



For audio (midi): ldmt-9-3-3-9-3-8-5-6-9-4-2-3-8-2-3.mid

9 - 5 - 8 - 3 - 5 - 5 - 8 - 8 - 5 - 8 - 7 - 2 - 2 - 6 - 6 - 4

ldmt::65:34:59:20:37:38:63:64::33:58:51:12:13:46:47:32::

Perm. No.: 515133864002205



For audio (midi): ldmt-9-5-8-3-5-5-8-8-5-8-7-2-2-6-6-4.mid

9-6-6-7-3-6-6-5-8-6-7-8-4-8-5-3

 ${\tt ldmt::} 65:42:43:52:21:46:47:40::} 57:42:51:60:29:62:39:24::$

Perm. No.: 361008226816992



For audio (midi): ldmt-9-6-6-7-3-6-6-5-8-6-7-8-4-8-5-3.mid

9-7-6-2-6-1-4-3-3-7-8-4-1-6-9-6

ldmt::65:50:43:12:45:6:31:24::17:50:59:28:5:46:71:48::

Perm. No.: 135398766540357



For audio (midi): ldmt-9-7-6-2-6-1-4-3-3-7-8-4-1-6-9-6.mid

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