



$$\rho(w') \leq \rho(w)$$

$$\bullet \quad \mathcal{W} = \bullet \cdots \bullet s_i s_{i+1} \bullet \cdots \bullet$$

- Each letter  $s_i$  appears in a tree in exactly one of two ways:

oLead from code

- Removed by conjugate node  $s_i v s_i^{-1} \rightarrow v$

• Enumerate all possible cases. Show there is a node of interest  $v = \cdots s_i s_i^{-1} \cdots$

- Replace subtree at  $v$  with a tree for the reduced word  $v'$  without adding leaf nodes.



$$\rho(w') \leq \rho(w)$$

- $w = \cdots s_i s_{i+1} \cdots$
- Each letter  $s_i$  appears in a tree in exactly one of two ways:
  - Leaf node
  - Removed by conjugate node  $s_i w s_i^{-1} \rightarrow w$
- Enumerate all possible cases. Show there is a node of interest  $v = \cdots s_i s_i^{-1} \cdots$
- Replace subtree at  $v$  with a tree for the reduced word  $v'$  without adding leaf nodes.

# Example Case 1

$s_i$  and  $s_{i+1}$  are removed by the same conjugation node:

$$v = s_i s_{i+1}$$

$$\rho(v) = C(s_i s_{i+1}) = 0$$

After reduction:

$$\rho(v') = 0$$

$s_i s_{i+1}$



*empty*