

# Personal Taxation and Behaviour

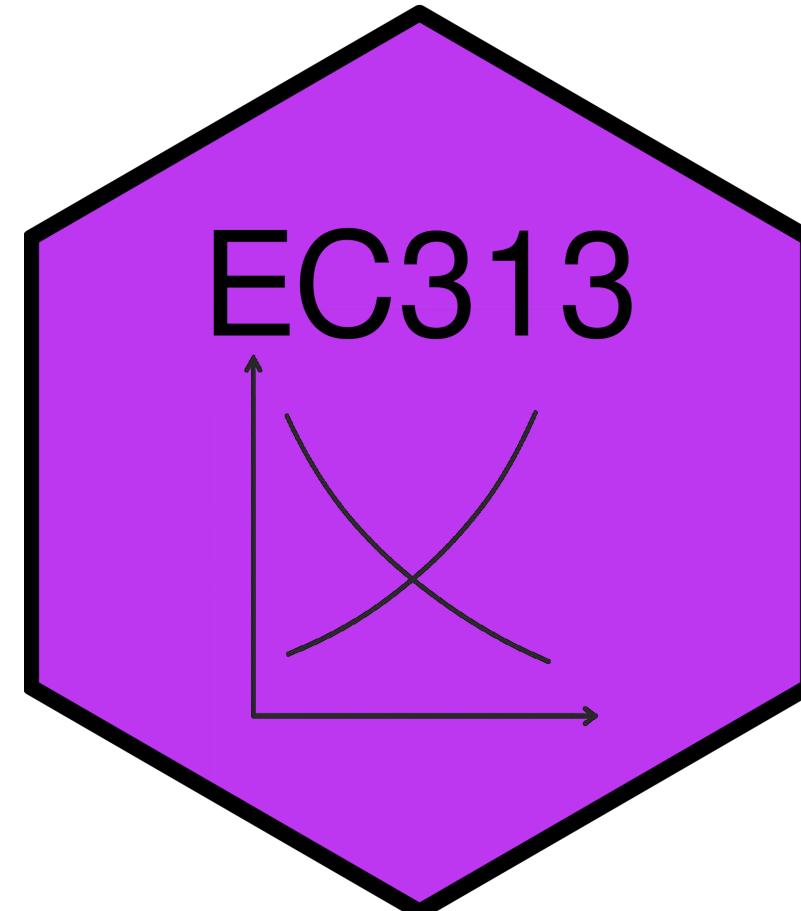
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EC313 - Public Economics: Taxation

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# Goals of This Section



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- Examine the effect of income taxation on labour supply
- Analyze how labour supply is related to tax revenues with the Laffer Curve
- Look at how taxation affects saving behaviour
- Discuss the preferential tax treatment of primary residences in Canada
- Examine taxation and portfolio allocation



# Taxation and Labour Supply



# Introduction

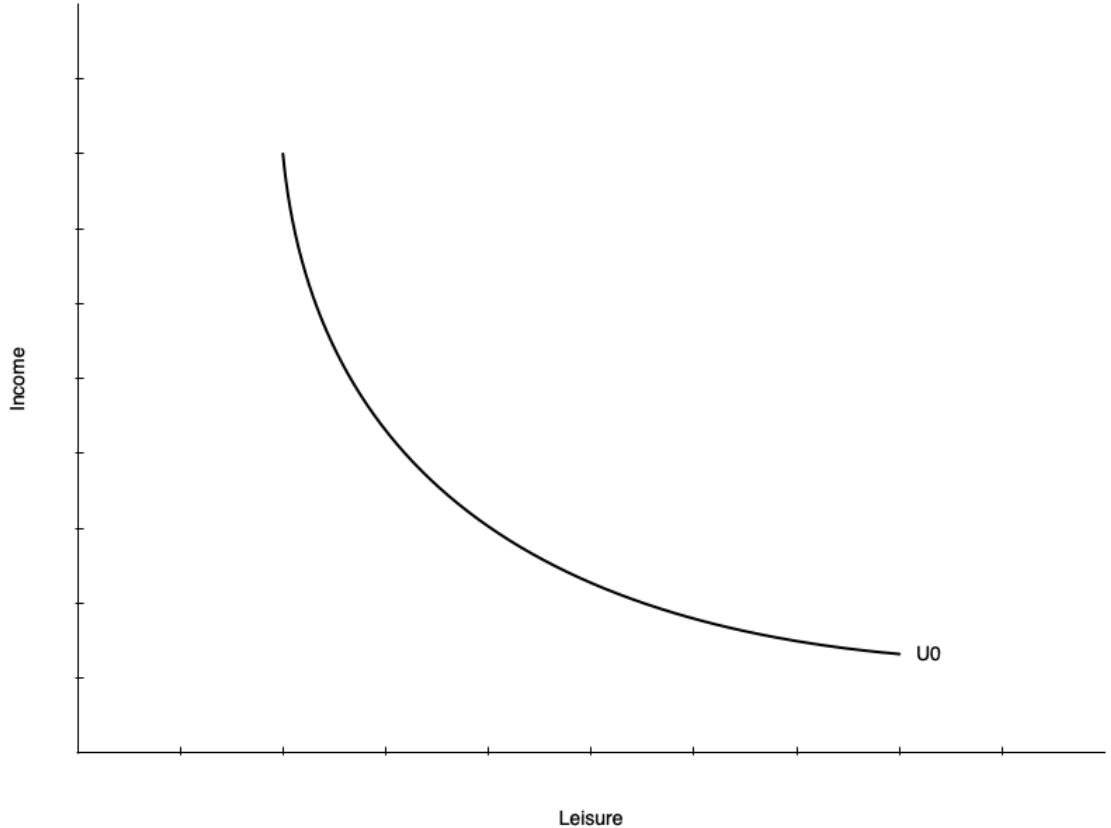
- In this section we introduce a model we use throughout the course
- The model helps us understand how individuals make decisions about work
- Individual choose between two goods
  - Income
  - Leisure
- Choices are constrained by time and wage rate
- There are a few wrinkles that make this market unique



# Preferences

- Individuals have preferences over Income (I) and leisure (L)
  - People like having income to consume goods/services
  - Also like having non-work time
    - Includes fun activities but also non-work tasks like chores, education, etc.
- The tradeoffs people are willing to make between I and L are represented by indifference curves
  - At every point along the curve the individual is equally happy
  - Curves further from the origin represent higher levels of utility

# Preferences



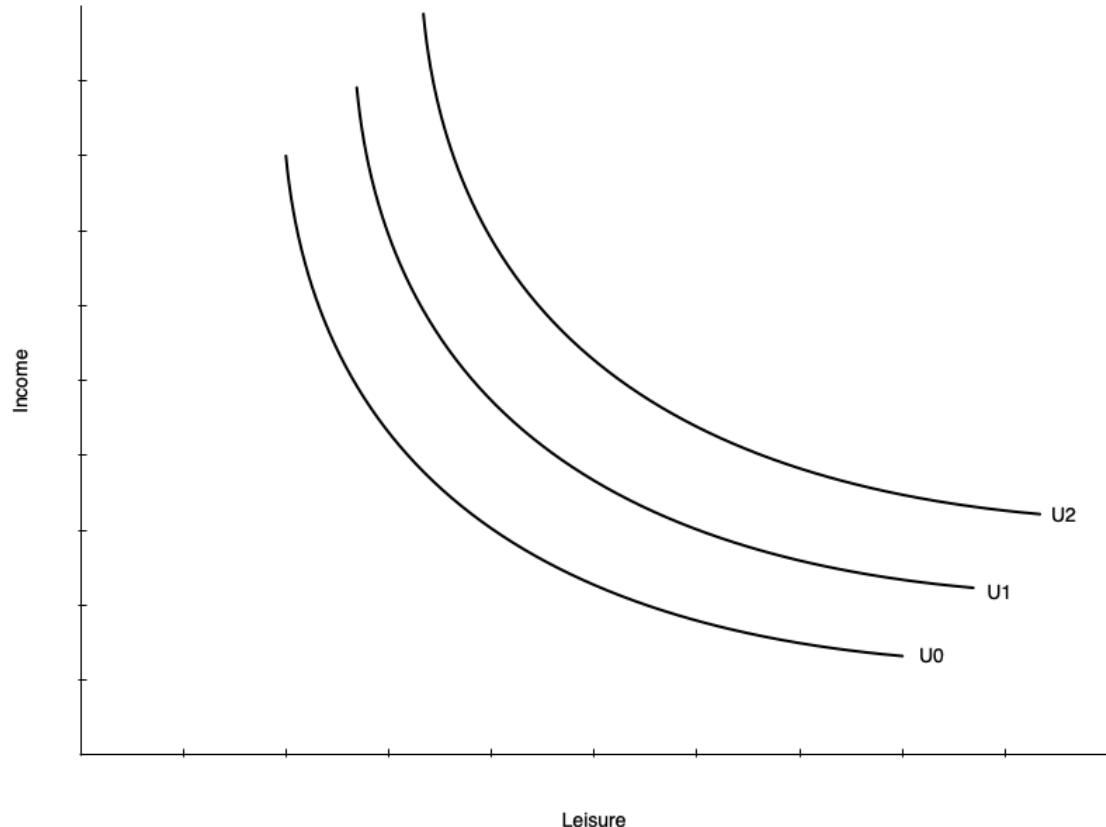
- On the left is a single indifference curve
- Any point represents equal utility ( $U_0$ )
- **Marginal Rate of Substitution (MRS):** the rate at which a person is willing to trade income for leisure while remaining equally happy
- The MRS is the slope of the indifference curve at a point
- Individuals have diminishing MRS
  - Willing to give up less income for additional leisure the more leisure they already have
  - Slope gets shallower with more leisure

# Preferences

- Indifference curves do not have to be smooth curves like the one shown
- Could be straight lines
  - Means the tradeoff between income and leisure is constant
  - Willingness to trade away leisure for income does not depend on leisure
- Could be “L” shaped
  - Income and leisure must be consumed in fixed proportions
- Mostly we will deal with smooth preferences



# Preferences



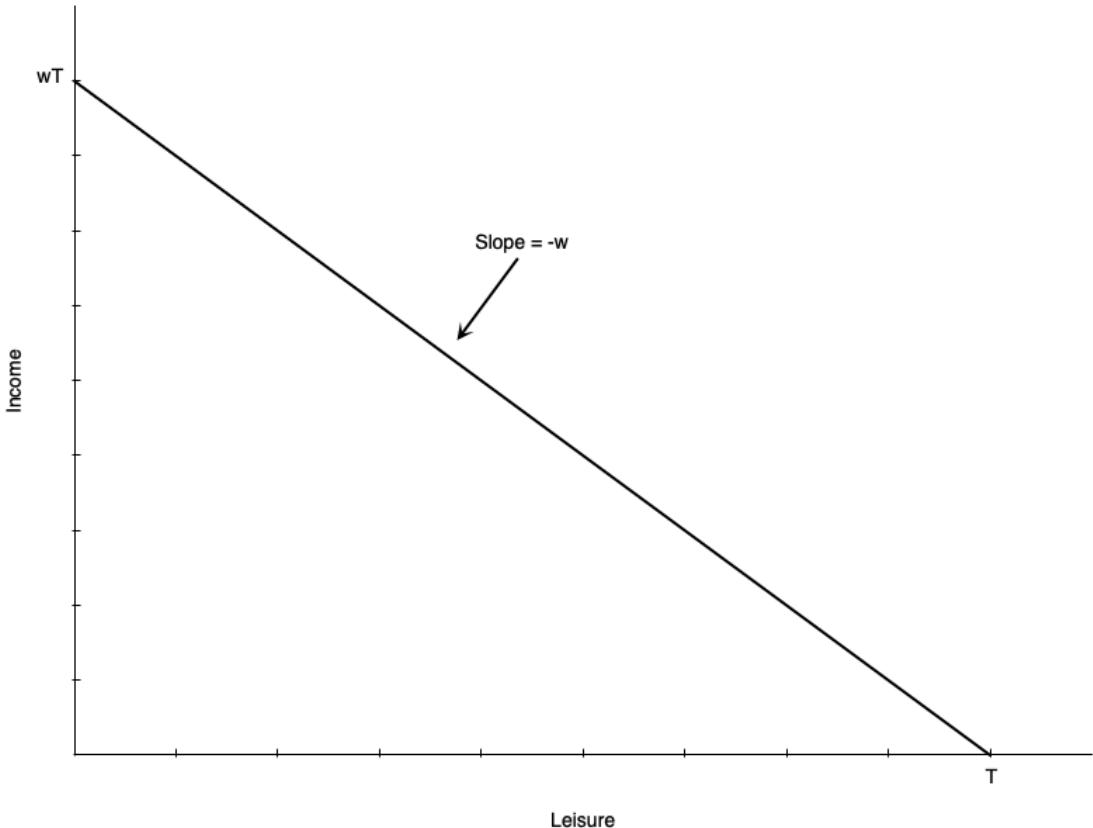
- Utility increases with curves further from the origin
  - $U_2 > U_1 > U_0$

# Constraints

- Individuals do not choose income and leisure bundles on preference alone
- They are constrained by
  - The wage rate
  - Total number of hours available
- Budget constraint is also called
  - Potential income constraint
  - Full income constraint



# Constraints



- Graph shows a linear budget constraint
- There are  $T$  total hours to allocate to work or leisure
- Each hour worked gets wage of  $w$
- Person working  $T$  hours (no leisure) earns  $wT$  income
  - Called “full income”

# Constraints

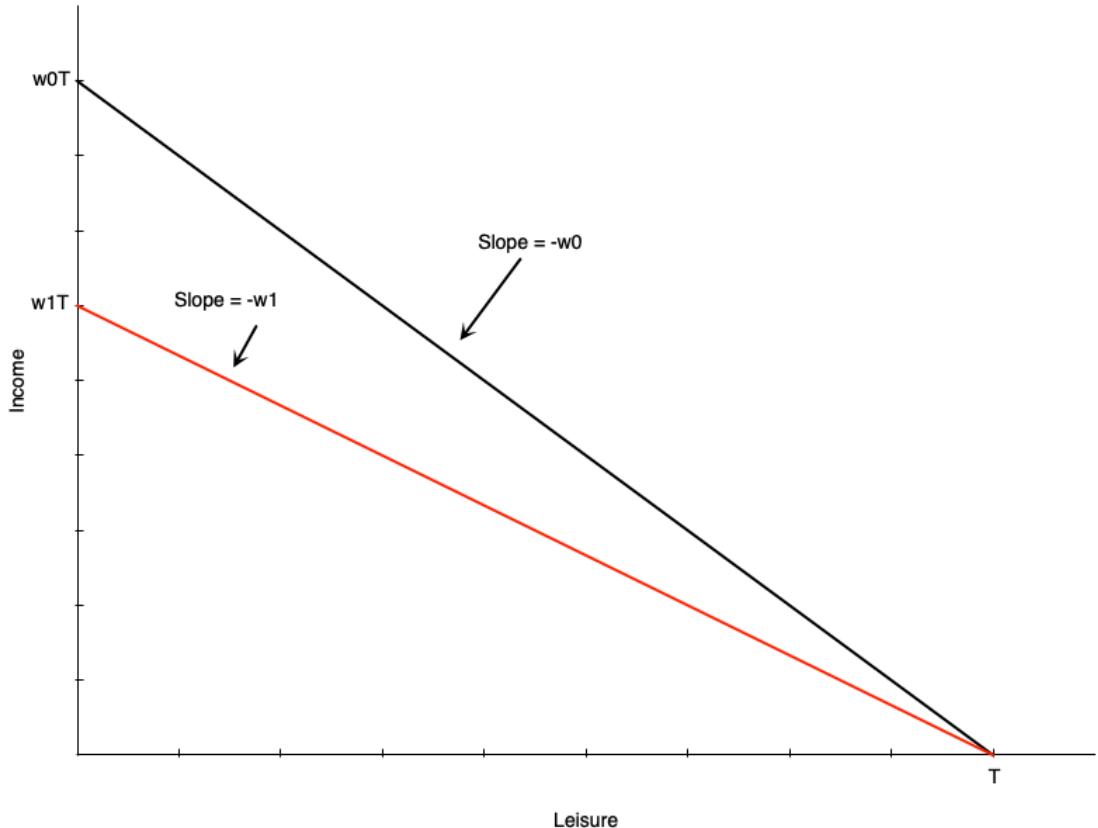
- Mathematically, the budget constraint is

$$I = w(T - L)$$

- Income is equal to income from working ( $w(T - L)$ )
- The slope of the budget constraint is  $-w$ 
  - The opportunity cost of leisure is the wage rate
  - Each hour of leisure means one less hour worked, which means  $w$  less income
- Someone who works zero hours has  $T$  leisure hours and no income
- Someone who works  $T$  hours has zero leisure hours and  $wT$  income



# Constraints

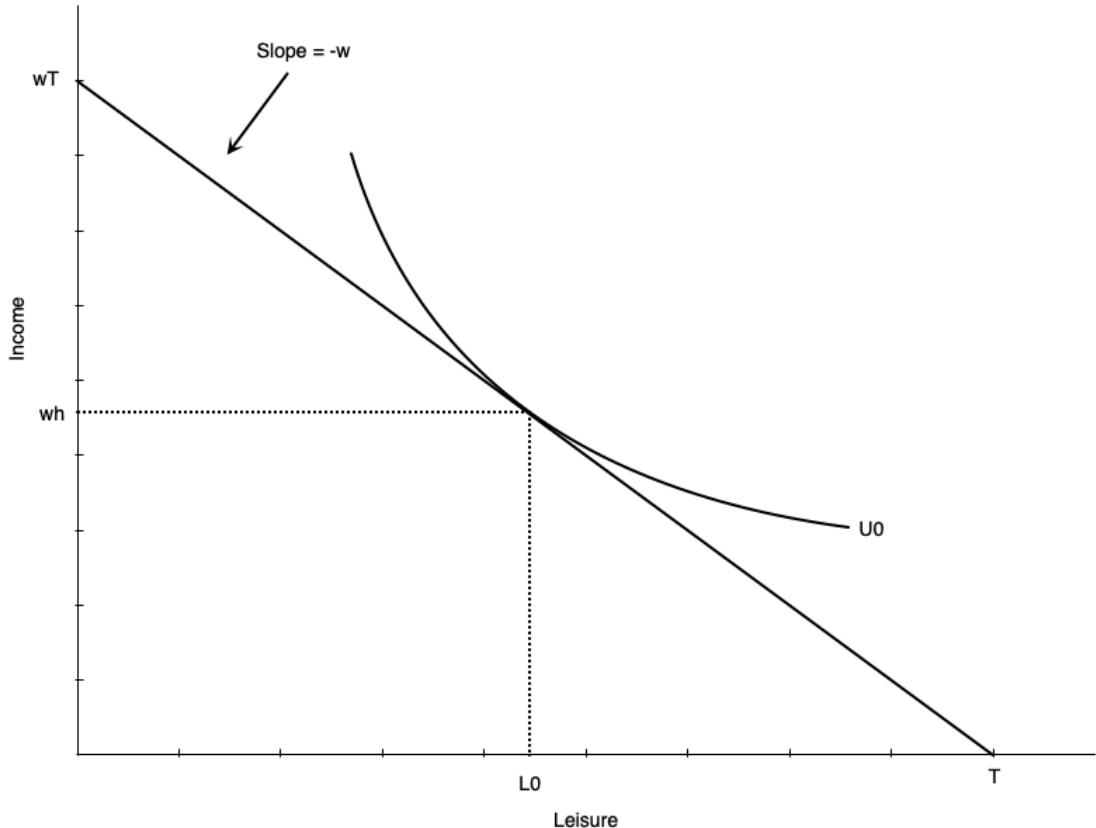


- Slope is the negative of the wage rate  $w$
- A lower wage means shallower slope
  - If  $w_1 < w_0$ , the budget line swivels down
  - They intersect at leisure =  $T$  because there are no work hours
- Lower wage also means full income is lower
  - Working all hours leads to less total labour earnings

# Consumer Optimum

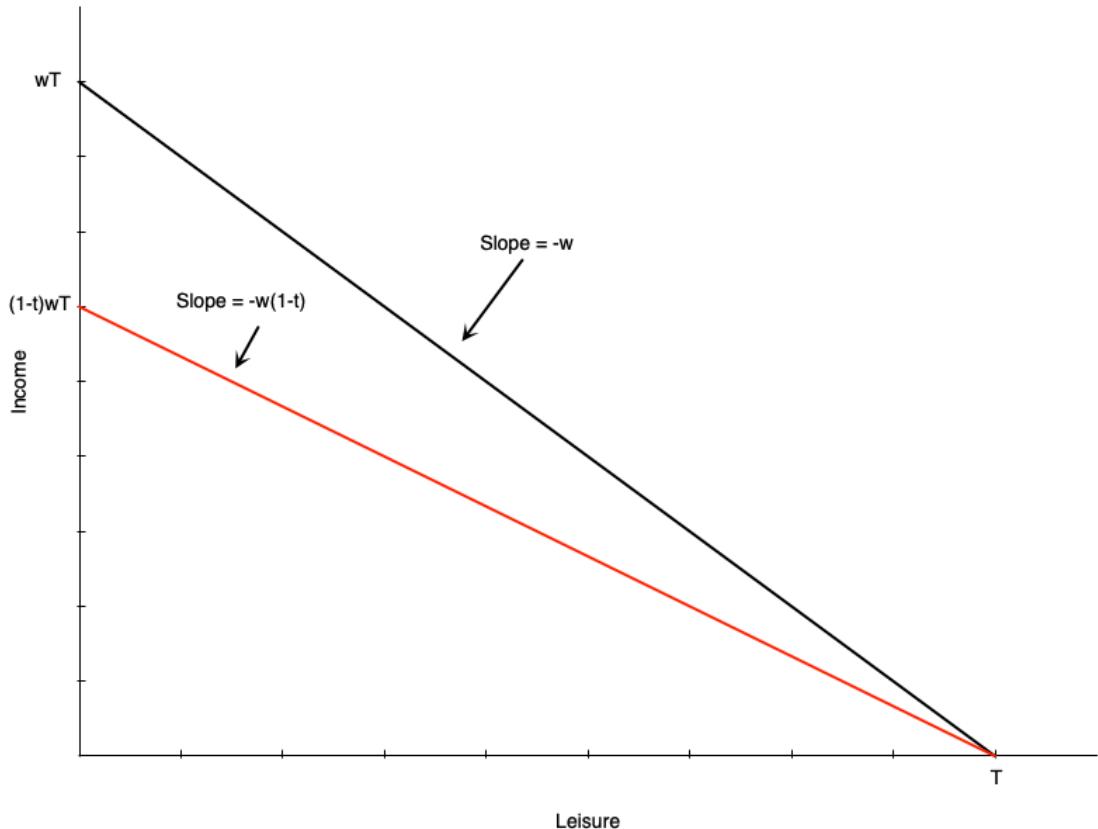
- Work hours are chosen using the combination of preferences and constraints
- The consumer optimum is the point that maximizes utility subject to the budget constraint
- The optimum occurs where the budget constraint is tangent to an indifference curve
- There are two possibilities for the optimum
  - Non-participation: optimum occurs at the end of the budget constraint (full leisure)
  - Participation: optimum occurs at an interior point (some leisure, some work)

# Consumer Optimum



- Graph shows an optimum with participation
- Optimum is where indifference curve is tangent to budget constraint
- At the optimum,  $MRS = \text{wage rate}$ 
  - Willingness to trade leisure for income ( $MRS$ ) equals ability to trade them (wage)
- Optimal work hours are  $h_0 = T - L_0$
- Optimal consumption is  $I_0 = W_0 h_0$

# Personal Income Tax

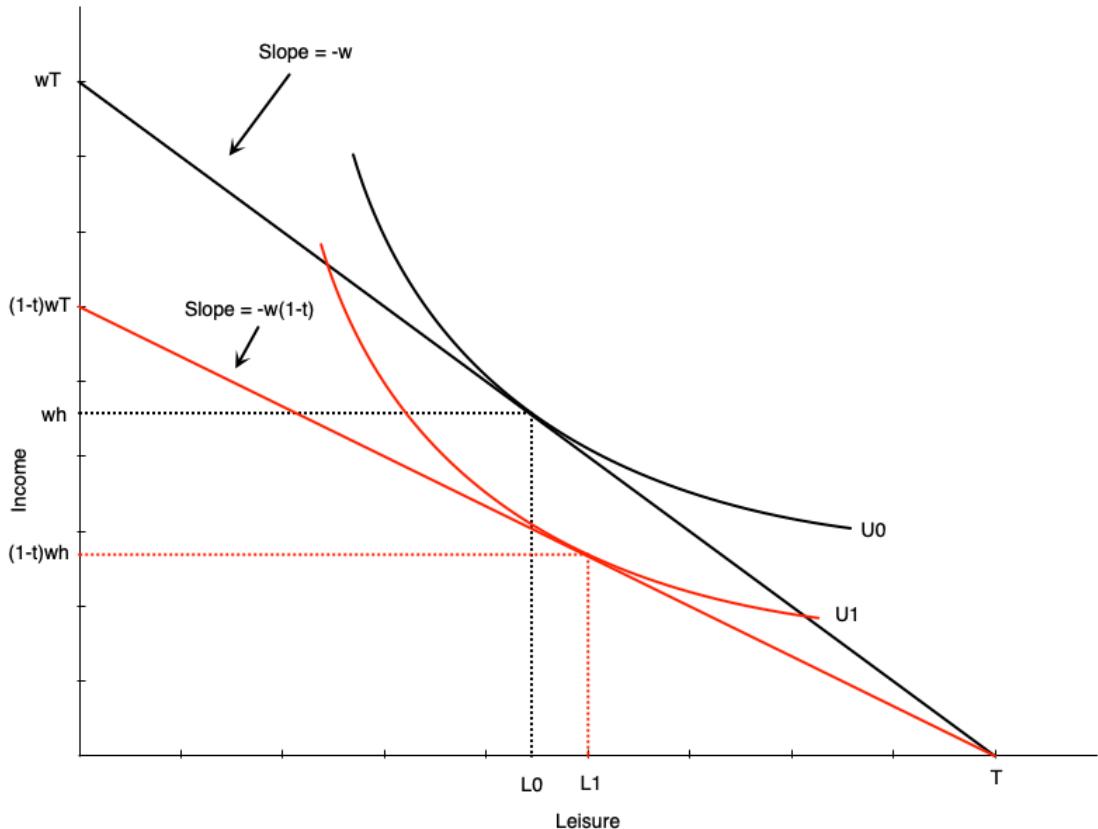


- The personal income tax affects the budget constraint
- Suppose a proportional income tax at rate  $t$  is introduced
  - The after-tax wage is now  $w(1 - t)$
  - Tax causes the budget constraint to pivot inward
    - Slope is now  $-w(1 - t)$
    - Full income is now  $w(1 - t)T$

# Personal Income Tax

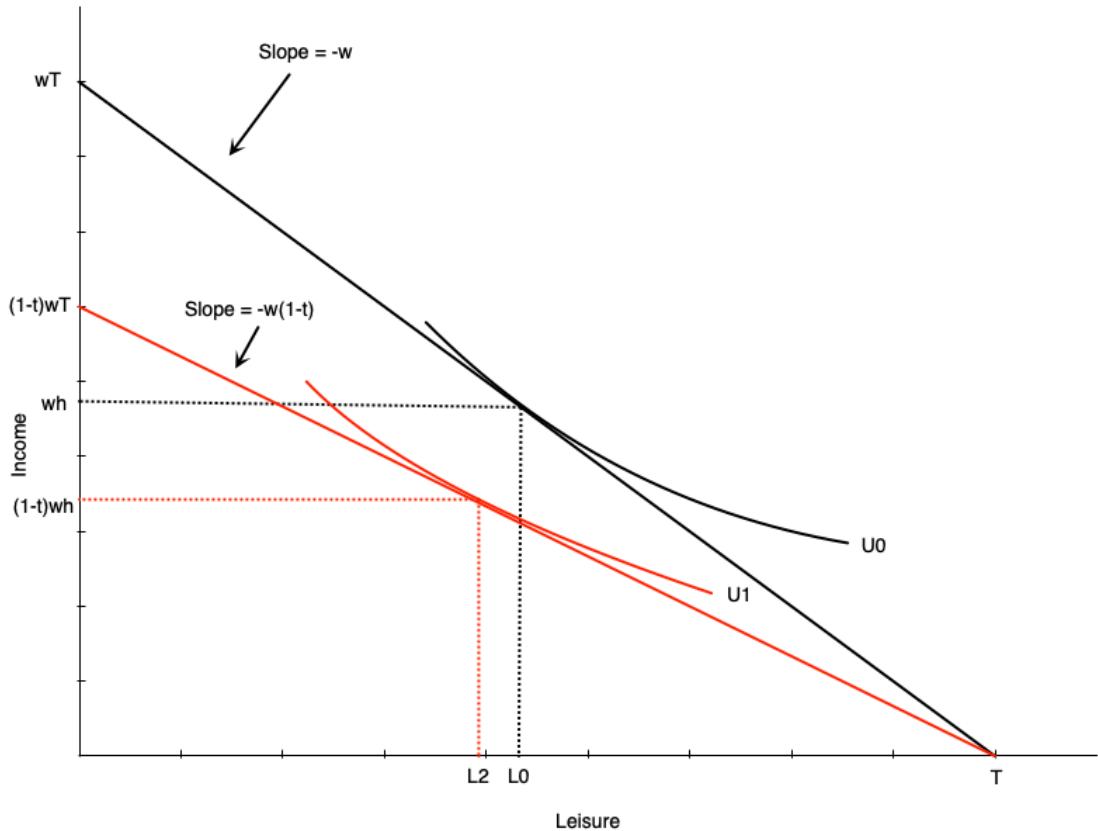
- When the budget constraint changes, so does the optimum
- Suppose there is a proportional income tax at rate  $t$
- There are two effects of the tax on labour supply
  - **Substitution effect:** leisure is relatively cheaper, so people want more leisure (work less)
  - **Income effect:** people are poorer, so they want less leisure (work more)
- The effect on labour supply is therefore ambiguous
  - If substitution effect > income effect, labour supply decreases
  - If income effect > substitution effect, labour supply increases

# Personal Income Tax



- Graph shows when substitution effect > income effect
  - Budget swivels down
  - Person optimizes at lower indifference curve
  - Leisure increases from  $L_0$  to  $L_1$
  - Work hours decrease from  $h_0$  to  $h_1$
- Happens when people are more willing to trade income for leisure

# Personal Income Tax



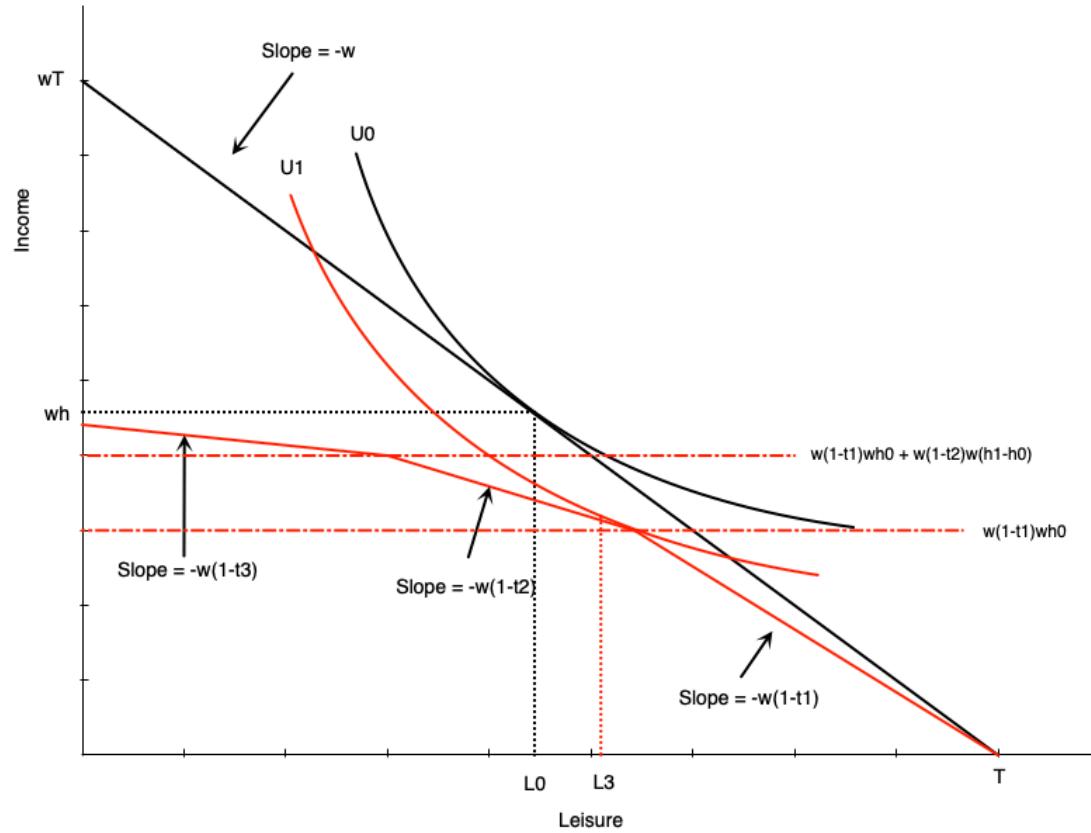
- Graph shows when income effect > substitution effect
  - Budget swivels down
  - Person optimizes at lower indifference curve
  - Leisure decreases from  $L_0$  to  $L_2$
  - Work hours increase from  $h_0$  to  $h_2$
- Happens when people are less willing to trade income for leisure

# Personal Income Tax

- In reality taxes are not flat
  - Canada has a progressive income tax system
  - Higher income is taxed at higher rates
- This implies that the budget constraint becomes kinked
  - As income goes up, the tax rate increases
  - When the tax rate changes, the slope changes
- The basic principles are the same
  - Substitution and income effects still apply
  - Labour supply effect is still ambiguous



# Personal Income Tax



- Graph shows a proportional income tax with three brackets
- Tax rates are  $t_3 > t_2 > t_1$
- Slope changes at each kink
  - First kink happens with work hours  $h_0$
  - Second kink happens with work hours  $h_1$
- Graph shows increased leisure, but effect is ambiguous

# Evidence on Labour Supply

- The theory discusses effect of tax \*holding all else equal\*\*
- In statistical work, this is not easy to do
  - Many factors affect labour supply
  - Isolating the effect of taxes is difficult
- Studies show that
  - Elasticity of hours worked for working age men is between -0.2 and 0.2
  - For women is is between -0.2 and 0.5
- Means that a reduction in wage based on income tax has a small effect on work hours
- Effect on labour force participation is larger



# Caveats on Taxation and Labour Supply

# Individual vs Group Effects

- We simplified the discussion by analyzing one specific type of person
- But tax changes affect many types of people differently
- A change from a flat to progressive tax might
  - Increase the tax rate for some people
  - Decrease the tax rate for others
- The way they react will be different and for policy analysis we need to consider the group effects



# Human Capital

- Taxes can affect decisions about education and training
- We saw that taxes affect an individual's optimal labour supply at each wage
- If a tax increases the optimum hours at each wage, it would increase the desire to get education/training
  - This would make the worker more productive, and increase their wage
  - Could lead to further increases in supply
- The reverse would happen if tax decreases optimum hours at each wage



# Total Compensation

- Wages are not the only part of compensation
  - There are non-wage benefits like health insurance, retirement contributions, etc.
- If taxes rise, firms may switch to non-taxed forms of compensation
- The effect of the tax may be muted if firms can do this easily



# Expenditures

- Governments use tax revenues to fund public services
- That spending may itself affect labour supply
  - Spending on child care would increase supply
  - If spent on recreational facilities, parks, etc., may decrease supply
- Need to think about this from a general equilibrium lens



# Labour Supply and Tax Revenues

# Introduction

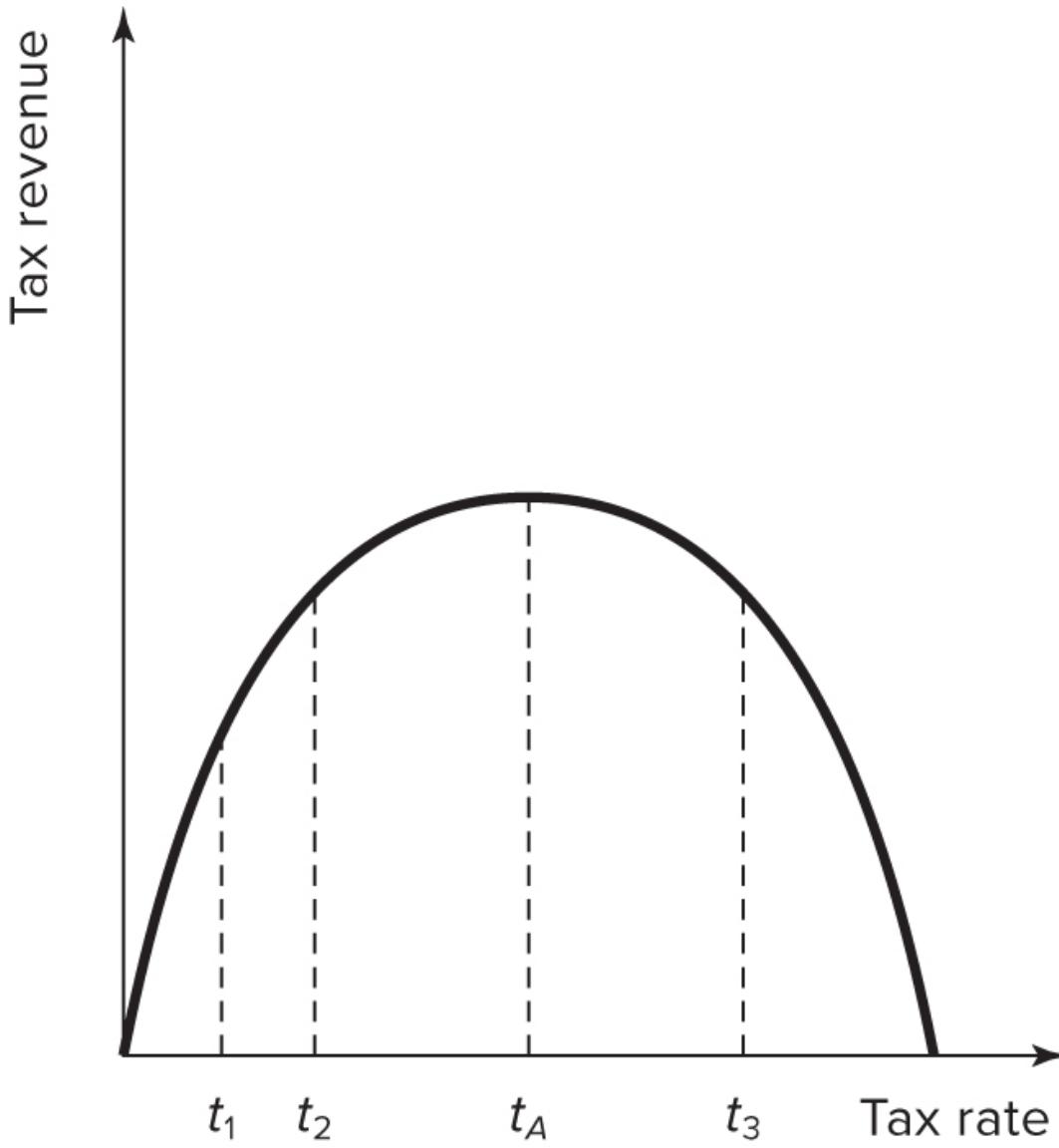
- As just noted, governments tax labour income to raise revenue
- The tax revenue collected from this exercise is the tax rate times the tax base
  - Tax base is the amount of income earned
  - Which in our model is  $w \times h$
- So the tax revenue is  $R = t \times w \times h$
- As we saw, if the substitution effect is larger than the income effect, higher tax rates reduce labour supply
- Means that as  $t$  increases,  $wh$  decreases



# Laffer Curve

- The fact that higher tax rates may reduce labour supply has implications for tax revenue
- The relationship between tax rates and tax revenue is called the **Laffer Curve**
- The Laffer Curve shows that tax revenue is zero at both 0% and 100% tax rates
- Initially as tax rates rise, revenue rises
- But at some point, further increases in tax rates reduce revenue
  - Because the reduction in labour supply is large enough that the tax base shrinks significantly

# Laffer Curve



# Laffer Curve

- The Laffer Curve suggests there is an optimal tax rate when it comes to revenues
  - At the peak of the curve where additional increases in tax rates do not increase revenue
- Also suggests that when tax rates are too high, reducing them could increase revenue
- However, determining the optimal tax rate is difficult in practice
  - Depends on how responsive labour supply is to tax changes
  - Empirical estimates suggest we are not near the peak of the Laffer Curve for labour income taxes in Canada

# Saving



# Introduction

- In addition to labour supply, taxes affect saving
- Saving is important because it funds investment
  - Investment leads to capital accumulation
  - Capital accumulation leads to economic growth
- Taxes affect saving through reductions in the return
  - Interest earned through saving counts as income
  - That income is taxable
- In this section we will look at how taxes affect saving behaviour in a life-cycle model



# Life-Cycle Model

- The life-cycle model assumes individuals plan their consumption and saving over their lifetime
- To keep things simple, we consider two time periods
  - Present and future
- Individuals have preferences for consumption in both periods
  - Represented by indifference curves
- They also have a budget constraint based on their income in both periods
  - Says that the present value of consumption equals the present value of income



# Life-Cycle Model

- Algebraically, the budget constraint is

$$c_0 + \frac{c_1}{1+r} = I_0 + \frac{I_1}{1+r}$$

- Where
  - $c_0$  = consumption in present period
  - $c_1$  = consumption in future period
  - $I_0$  = income in present period
  - $I_1$  = income in future period
  - $r$  = real interest rate



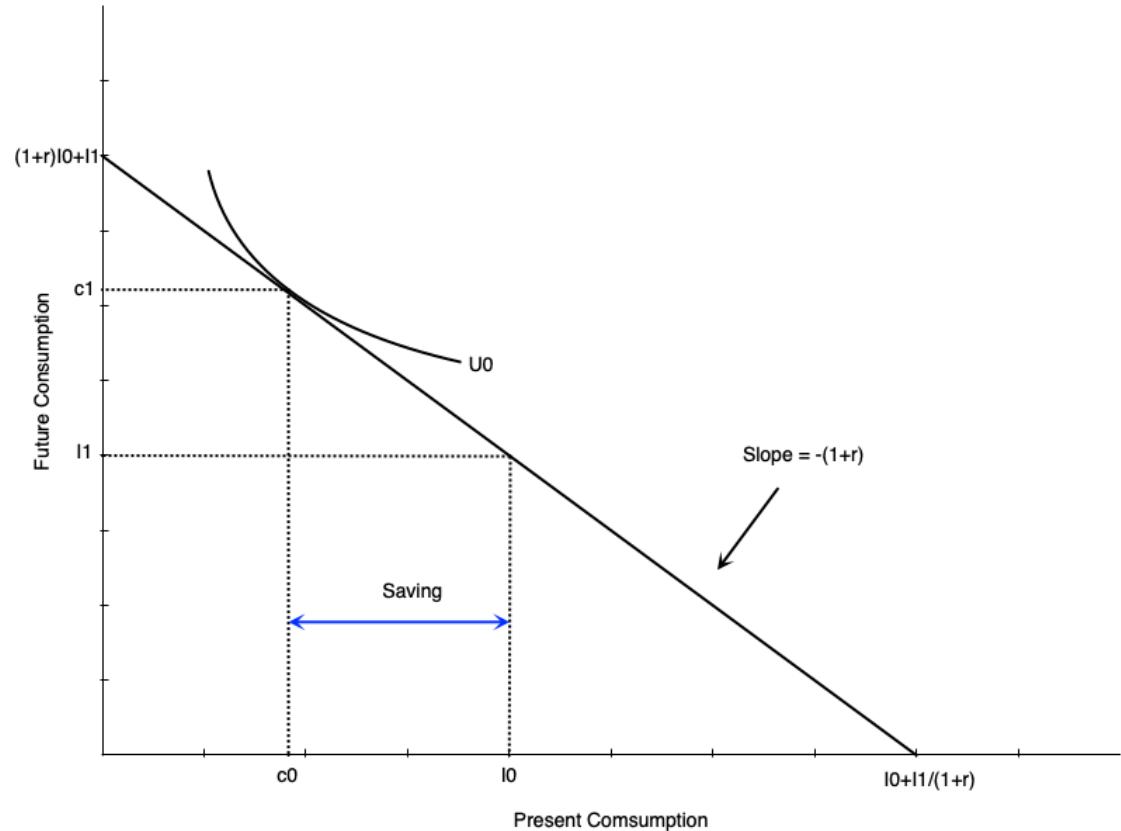
# Life-Cycle Model

- You can plot this on a graph with  $c_0$  on the x-axis and  $c_1$  on the y-axis
- Rearrange to get  $c_1$  on left side

$$c_1 = (1 + r)(I_0 - c_0) + I_1$$

- Slope of budget constraint is  $-(1 + r)$ 
  - Consuming a dollar today means giving up  $(1 + r)$  dollars tomorrow
- When a person consumes  $I_0$  today, they consume  $I_1$  tomorrow
  - The budget line passes through  $(I_0, I_1)$

# Life-Cycle Model



- Graph shows intertemporal budget constraint
- Slope is  $-(1 + r)$
- Optimal consumption occurs where budget constraint is tangent to indifference curve
- In this case, the person saves in period 0 to consume more in period 1
  - Saving is the difference between income and consumption in period 0

# Tax on Interest Income with Deductible Interest

- Now suppose there is a tax on interest income at rate  $t$
- A person who saves \$1 in period 0 receives interest  $r - rt$  in period 1
  - Because the interest earned is taxed they must pay  $rt$  on the interest
  - This lowers the return
- Means that foregoing \$1 in period 0 leads to consuming  $\$1 + r - rt = 1 + (1-t)r$  \$ in period 1
  - The after-tax interest rate is  $r(1 - t)$

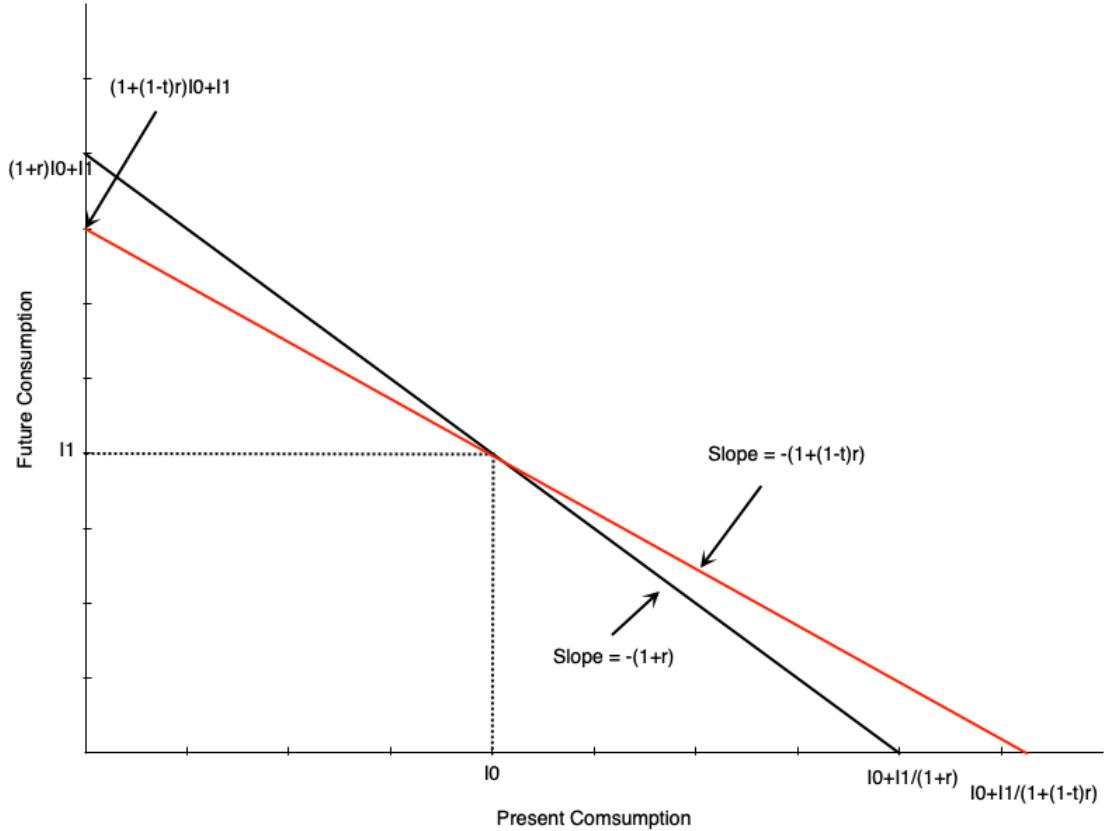


# Tax on Interest Income with Deductible Interest

- A person who borrows \$1 in period 0 will need to pay interest  $r - rt$  in period 1
  - They pay interest  $r$
  - But because it is *tax deductible* they save  $rt$  on taxes
  - Means that total interest paid is  $r - rt$
- Means that borrowing \$1 in period 0 leads to foregoing  $\$1 + r - rt = 1 + (1-t)r$  \$ of consumption in period 1
  - The after-tax interest rate is  $r(1 - t)$
- So whether saving or borrowing, the after-tax interest rate is the same



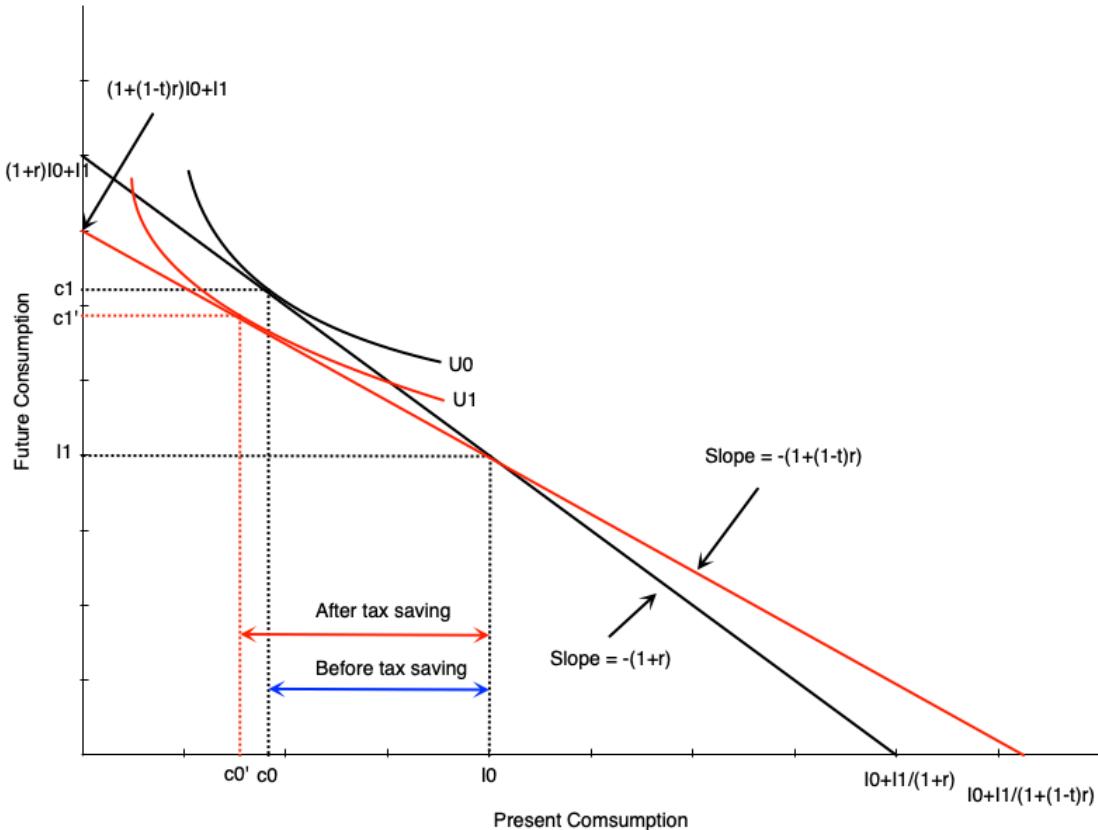
# Tax on Interest Income with Deductible Interest



- Graph shows effect of tax on interest income on optimum
- Tax rotates budget constraint around  $(I_0, I_1)$ 
  - Slope falls from  $-(1 + r)$  to  $-(1 + r(1 - t))$
  - Passes through  $(I_0, I_1)$  because no tax paid if no saving/borrowing
- Two effects of taxation
  - Substitution effect: opportunity cost of consumption today is lower, so consume more today (save less)
  - Income effect: lower real income, so consume less in both periods (save more)
- Total effect is ambiguous

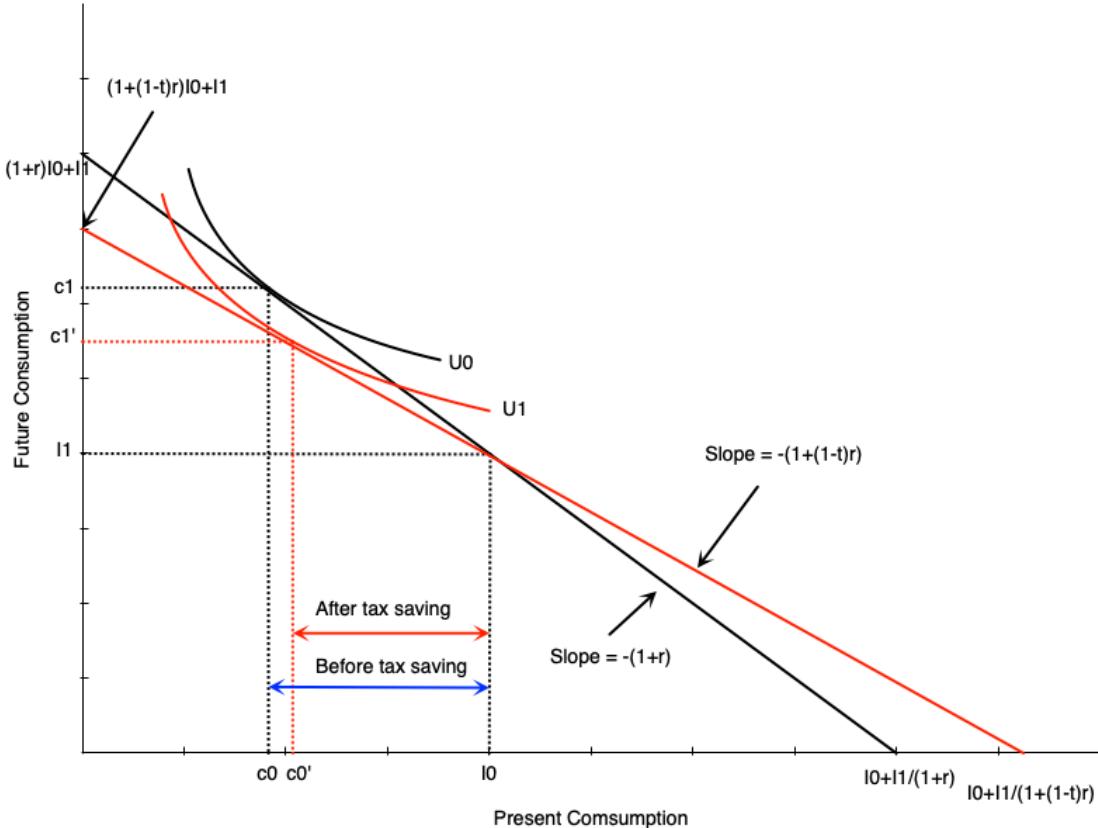
# Tax on Interest Income with Deductible Interest

- Graph shows case when saving increases
  - Income effect > substitution effect
- Saving increases today
- But consumption in both periods falls



# Tax on Interest Income with Deductible Interest

- Graph shows case when saving decreases
  - Substitution effect > income effect
- Saving falls today
- Consumption increases today, but falls in the future



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