Name: ______
Date:

Algebra II Homework 29

Problem 1. Write the following functions in the form $f(x) = (x \pm h)^2 \pm k$ by completing the square. Describe how x^2 is shifted to obtain f(x). Graph f(x), label the vertex, label all axis intersections. An example of what I expect is given below.

(a)
$$f(x) = (x+1)^2 - 2$$
, x-intercepts: $\{-1 \pm \sqrt{2}\}$, y-intercept: -1 , vertex: $(-1, -2)$

(b)
$$f(x) = (x - \frac{7}{2})^2 - \frac{9}{4}$$
, x-intercepts: $\{2, 5\}$, y-intercept: 10, vertex: $(\frac{7}{2}, -\frac{9}{4})$

(c)
$$f(x) = (x + \frac{1}{2})^2 + \frac{3}{4}$$
, x-intercepts: $\{-\frac{1}{2} \pm i\frac{\sqrt{3}}{2}\}$, y-intercept: 1, vertex: $(-\frac{1}{2}, \frac{3}{4})$

(d)
$$f(x) = (x-4)^2 - 1$$
, x-intercepts: $\{3,5\}$, y-intercept: 15, vertex: $(4,-1)$

(e)
$$f(x) = (x + \frac{3}{2})^2 - \frac{9}{4}$$
, x-intercepts: $\{-3, 0\}$, y-intercept: 0, vertex: $(-\frac{3}{2}, -\frac{9}{4})$

(f)
$$f(x) = (x-2)^2 + 3$$
, x-intercepts: $\{2 \pm i\sqrt{3}\}$, y-intercept: 7, vertex: $(2,3)$

(g)
$$f(x) = (x + \frac{3}{4})^2 - \frac{5}{16}$$
, x-intercepts: $\left\{-\frac{3}{4} \pm \frac{\sqrt{5}}{4}\right\}$, y-intercept: $\frac{1}{4}$, vertex: $\left(-\frac{3}{4}, -\frac{5}{16}\right)$

(h)
$$f(x) = \left(x - \frac{1}{2}\right)^2 - \frac{5}{4}$$
, x-intercepts: $\left\{\frac{1}{2} \pm \frac{\sqrt{5}}{2}\right\}$, y-intercept: -1 , vertex: $\left(\frac{1}{2}, -\frac{5}{4}\right)$

(i)
$$f(x) = (x + \frac{3}{2})^2 - \frac{16}{9}$$
, x-intercepts: $\{-\frac{17}{6}, -\frac{1}{6}\}$, y-intercept: $\frac{17}{36}$, vertex: $(-\frac{3}{2}, -\frac{16}{9})$