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# ShowFib.py
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"""
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while-loop investigations of the Fibonacci sequence and its relation to the golden ration = $(1+\sqrt{5})/2$.

Background:

Given a "current" Fibonacci number and its "predecessor", the "next" Fibonacci number is the sum of the current and the predecessor. Starting off with a 0 and 1 as the predecessor and the current Fibonacci number, we get

0,1,1,2,3,5,8,13,21,34, etc

We index the Fibonacci numbers by where they are in this sequence, e.g.,

0 is the zeroth Fibonacci number

13 is the seventh Fibonacci number

34 is the ninth Fibonacci number

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"""
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```
import math
```

```
#Problem 1. Print out Fibonacci numbers 1 through 15
```

```
# Initializations
```

```
k = 1
```

```
x = 0 # the past Fibonacci number
```

```
y = 1 # the current Fibonacci number
```

```
z = 1 # the next Fibonacci number
```

```
ratio = float(z)/float(y)
```

```
# y is the k-th Fibonacci number
```

```
print '\n k    kth Fib    kth Ratio '
```

```
print '-----'
```

```
while k<=15:
```

```
    print '%3d %10d    %14.12f'%(k,y,ratio)
```

```
    k += 1
```

```
    x = y    # Fib k-1
```

```
    y = z    # Fib k
```

```
    z = x+y  # Fib k+1
```

```
    ratio = float(z)/float(y)
```

```
#Problem 2. Print out Fibonacci numbers
```

```
# 1 through k where k is the first Fibonacci
```

```
# number whose ratio is < .000001
```

```
# Initializations
```

```
r = (1 + math.sqrt(5))/2
```

```
k = 1
```

```
x = 0 # the past Fibonacci number
```

```
y = 1 # the current Fibonacci number
```

```
z = 1 # the next Fibonacci number
```

```
# y is the k-th Fibonacci number
```

```
error = abs(float(z)/float(y)-r)
```

```
print '\n k    kth Fib    kth Ratio Error '
```

```
print '-----'
```

```
while error>=.000000001:
```

```
    print '%3d %10d    %14.12f'%(k,y,error)
```

```

k += 1
x = y    # Fib k-1
y = z    # Fib k
z = x+y  # Fib k+1
error = abs(float(z)/float(y)-r)
print '%3d %10d    %14.12f ' %(k,y,error)

```

#Problem 3. Print out the smallest Fibonacci
number bigger than 1000000

Initializations

```

k = 1
x = 0 # the past Fibonacci number
y = 1 # the current Fibonacci number
z = 1 # the next Fibonacci number
# y is the k-th Fibonacci number
while y<1000000:
    k += 1
    x = y    # Fib k-1
    y = z    # Fib k
    z = x+y  # Fib k+1
print '\nThe smallest Fibonacci number > million is Fib %1d = %1d' % (k,y)

```

#Problem 4. Print out the largest Fibonacci
number less than 1000000

Initializations

```

k = 1
x = 0 # the past Fibonacci number
y = 1 # the current Fibonacci number
z = 1 # the next Fibonacci number
# y is the k-th Fibonacci number
while z<1000000:
    k += 1
    x = y    # Fib k-1
    y = z    # Fib k
    z = x+y  # Fib k+1
print '\nThe largest Fibonacci number < million is Fib %1d = %1d' % (k,y)

```