

Physics Club: $F = ma$ Practice Test 2

Assume the acceleration due to gravity near the surface of the Earth $g = 10 \text{ m/s}^2$.

Correct answers will be awarded one point; incorrect answers will result in a deduction of 1/4 point. There is no penalty for leaving an answer blank.

You may use a scientific calculator. Its memory must be cleared of data and programs.

- Consider a dripping faucet, where the faucet is 15 cm above the sink. The time between drops is such that when one drop hits the sink, one is in the air, and another is about to drop. At what height above the sink will the drop in the air be right as a drop hits the sink?
 - Between 2 and 4 cm
 - Between 4 and 6 cm
 - Between 6 and 8 cm
 - Between 8 and 10 cm
 - Between 10 and 12 cm
- A cannonball is launched with initial velocity of magnitude v_0 over a horizontal surface. At what minimal angle θ_{\min} above the horizontal should the cannonball be launched so that it rises to a height H which is larger than one half of the horizontal distance R that it will travel when it returns to the ground?
 - $\theta_{\min} = 76^\circ$
 - $\theta_{\min} = 70^\circ$
 - $\theta_{\min} = 64^\circ$
 - $\theta_{\min} = 45^\circ$
 - There is no such angle θ_{\min} , as $R > 2H$ for all range problems.
- An equilateral triangle is sitting on an inclined plane. Friction is too high for it to slide under any circumstance, but if the plane is sloped enough it can “topple” down the hill. What angle incline is necessary for it to start toppling?
 - 30 degrees
 - 45 degrees
 - 60 degrees
 - It will topple at any angle more than zero
 - It can never topple if it cannot slide
- A particle at rest explodes into three particles of equal mass in the absence of external forces. Two particles emerge with velocities of the same magnitude v but form an angle of 60° . What is the speed of the third particle?

- (a) v
 - (b) $\sqrt{3}v$
 - (c) $2v$
 - (d) $2\sqrt{3}v$
 - (e) The third particle can have a range of different speeds.
5. A 12 kg block moving east at 3 m/s collides head on with a 6 kg block that is moving west at 2 m/s. The two blocks move together after the collision. What is the loss in kinetic energy in this collision?
- (a) 36 J
 - (b) 50 J
 - (c) 60 J
 - (d) 72 J
 - (e) 96 J

The following information is used for questions X and Y.

Two cannons are arranged vertically, with the lower cannon pointing upward (toward the upper cannon) and the upper cannon pointing downward (toward the lower cannon), 200 m above the lower cannon. Simultaneously, they both fire. The muzzle velocity of the lower cannon is 35 m/s and the muzzle velocity of the upper cannon is 55 m/s.

6. How long after the cannons fire do the projectiles collide?
- (a) 2.2 s
 - (b) 2.5 s
 - (c) 3.6 s
 - (d) 6.7 s
 - (e) 8.0 s
7. How far beneath the top cannon do the projectiles collide?
- (a) 31 m
 - (b) 67 m
 - (c) 110 m
 - (d) 150 m
 - (e) 170 m
8. A block of mass $m = 4.0$ kg is moving on a horizontal surface toward a massless spring with spring constant $k = 80.0$ N/m. The coefficient of kinetic friction between the block and the surface is $\mu_k = 0.50$. The block has speed of 2.0 m/s when it first comes into contact with the spring. How far will the spring be compressed?

- (a) 0.19 m
 - (b) 0.24 m
 - (c) 0.32 m
 - (d) 0.45 m
 - (e) 0.61 m
9. A uniform spherical planet has radius R and the acceleration due to gravity at its surface is g . What is the escape velocity of a particle from the planet's surface?
- (a) $\frac{1}{2}\sqrt{gR}$
 - (b) \sqrt{gR}
 - (c) $\sqrt{2gR}$
 - (d) $2\sqrt{gR}$
 - (e) The escape velocity cannot be expressed in terms of g and R alone.
10. Four objects are placed at rest at the top of an inclined plane and allowed to roll without slipping to the bottom in absence of rolling resistance and air resistance.
 Object A is a solid brass ball of diameter d .
 Object B is a solid brass ball of diameter $2d$.
 Object C is a hollow brass sphere of diameter d .
 Object D is a solid aluminum ball of diameter d . (Aluminum is less dense than brass.)
 The balls are placed so that their centers of mass all travel the same distance. In each case, the time of motion T is measured. Which of the following statements is correct?
- (a) $T_B > T_C > T_A = T_D$
 - (b) $T_A = T_B > T_C = T_D$
 - (c) $T_B > T_A = T_C = T_D$
 - (d) $T_A = T_B = T_C = T_D$
 - (e) $T_C > T_A = T_B = T_D$
11. As shown, Lily is using the rope through a fixed pulley to move a box with constant speed v . The kinetic friction coefficient between the box and the ground is $\mu < 1$; assume that the fixed pulley is massless and there is no friction between the rope and the fixed pulley. Then, while the box is moving, which of the following statements is correct?
- (a) The magnitude of the force on the rope is constant.
 - (b) The magnitude of friction between the ground and the box is increasing.
 - (c) The magnitude of the normal force of the ground on the box is decreasing.
 - (d) The pressure of the box on the ground is increasing.
 - (e) The pressure of the box on the ground is constant.

12. A rigid hoop can rotate about the center. Two massless strings are attached to the hoop, one at A, the other at B. These strings are tied together at the center of the hoop at O, and a weight G is suspended from that point. The strings have a fixed length, regardless of the tension, and the weight G is only supported by the strings. Originally OA is horizontal and OB forms an angle $\theta_0 < 90^\circ$ with the horizontal as shown in the diagram.

Now, the outer hoop will start to slowly rotate 90° clockwise until OA will become vertical, while keeping the angle between the strings constant and keeping the object static. Which of the following statements about the tensions T_1 and T_2 in the two strings is correct?

- (a) T_1 always decreases.
 - (b) T_1 always increases.
 - (c) T_2 always decreases.
 - (d) T_2 always increases.
 - (e) T_2 first increases then decreases.
13. Shown below is a graph of the x component of force versus position for a 2.0 kg cart constrained to move in one dimension on the x axis. At $x = 0$ the cart has a velocity of -3.0 m/s (in the negative direction). Which of the following is closest to the maximum speed of the cart?
- (a) 5.1 m/s
 - (b) 4.2 m/s
 - (c) 4.0 m/s
 - (d) 3.0 m/s
 - (e) 2.5 m/s
14. A uniform cylinder of radius a originally has a weight of 80 N. After an off-axis cylinder hole at $2a/5$ was drilled through it, it weighs 54 N. The axes of the two cylinders are parallel and their centers are at the same height.

A force T is applied to the top of the cylinder horizontally. In order to keep the cylinder at rest, the magnitude of the force T is closest to

- (a) 3 N
- (b) 5 N
- (c) 10 N
- (d) 25 N
- (e) 35 N

15. A car of mass m has an engine that provides a constant power output P . Assuming no frictional loss of energy, what is the maximum constant speed v_{\max} that this car can drive up a long incline that makes an angle θ with the horizontal?

(a) $v_{\max} = \frac{1}{\sin \theta} \sqrt{\frac{2P}{mg}}$

(b) $v_{\max} = \frac{P^2 \sin \theta}{mg}$

(c) $v_{\max} = \frac{P}{mg \sin \theta}$

(d) There is no maximum constant speed.

(e) The maximum constant speed depends on the length of the incline.

16. Inside a cart that is accelerating horizontally at acceleration a , there is a block of mass M connected to two light springs of force constants k_1 and k_2 . The block can move without friction horizontally. Find the vibration frequency of the block.

(a) $\frac{1}{2\pi} \sqrt{\frac{k_1 + k_2}{M}} + a$

(b) $\frac{1}{2\pi} \sqrt{\frac{k_1 + k_2}{M}}$

(c) $\frac{1}{2\pi} \sqrt{\frac{k_1 k_2}{(k_1 + k_2)M}}$

(d) $\frac{1}{2\pi} \sqrt{\frac{k_1 k_2}{(k_1 + k_2)M}} + a$

(e) $\frac{1}{2\pi} \sqrt{\frac{|k_1 - k_2|}{M}}$

17. Shown below is a log-log plot for the data collected of amplitude and period of oscillation for a certain non-linear oscillator.

According to the data, the relationship between the period T and the amplitude A is best given by

(a) $T = 100A^3$

(b) $T = 1000A^2$

(c) $T = 1000A$

(d) $T = 2A + 3$

(e) The period is independent of the amplitude for oscillating systems.

18. A mass hangs from the ceiling of a box by an ideal spring. With the box held fixed, the mass is given an initial velocity and oscillates with purely vertical motion. When the mass reaches the lowest point of its motion, the box is released and allowed to fall. To an observer inside the box, which of the following statements is true? Ignore air resistance.
- (a) The amplitude of the oscillation decreases.
 - (b) The period of the oscillation increases.
 - (c) The maximum speed reached by the mass increases.
 - (d) The height, measured from the bottom, at which the mass reaches its maximum speed decreases.
 - (e) The maximum height reached by the mass decreases.
19. A 1500 watt motor is used to pump water a vertical height of 2.0 meters out of a flooded basement through a cylindrical pipe. The water is ejected through the end of the pipe at a speed of 5.0 m/s. Ignoring friction and assuming that all of the energy of the motor goes to the water, which of the following is closest to the radius of the pipe? The density of water is 1000 kg/m^3 .
- (a) $1/3 \text{ cm}$
 - (b) 1 cm
 - (c) 5 cm
 - (d) 10 cm
 - (e) 30 cm
20. A container of water is sitting on a scale. Originally, the scale reads $M_1 = 45 \text{ kg}$. A block of wood is suspended from a second scale; originally the scale reads $M_2 = 12 \text{ kg}$. The density of wood is 0.60 g/cm^3 ; the density of the water is 1.00 g/cm^3 . The block of wood is lowered into the water until half of the block is beneath the surface. What is the resulting reading on the scales?
- (a) $M_1 = 55 \text{ kg}$ and $M_2 = 6 \text{ kg}$
 - (b) $M_1 = 55 \text{ kg}$ and $M_2 = 2 \text{ kg}$
 - (c) $M_1 = 45 \text{ kg}$ and $M_2 = 2 \text{ kg}$
 - (d) $M_1 = 45 \text{ kg}$ and $M_2 = 6 \text{ kg}$
 - (e) $M_1 = 45 \text{ kg}$ and $M_2 = 10 \text{ kg}$
21. A spring system is set up as follows: a platform with a weight of 10 N is on top of two identical springs, each with spring constant 75 N/m . On top of the platform is a third spring with spring constant 75 N/m . If a ball with a weight of 5.0 N is then fastened to the top of the third spring and then slowly lowered, by how much does the height of the spring system change?

- (a) 0.033 m
 - (b) 0.067 m
 - (c) 0.100 m
 - (d) 0.133 m
 - (e) 0.600 m
22. The softest audible sound has an intensity of $I_0 = 10^{-12} \text{ W/m}^2$. In terms of fundamental units of kilograms, meters, and seconds, this is equivalent to
- (a) $I_0 = 10^{-12} \text{ kg/s}$
 - (b) $I_0 = 10^{-12} \text{ kg}^2 \cdot \text{m/s}$
 - (c) $I_0 = 10^{-12} \text{ kg}^2 \cdot \text{m/s}^2$
 - (d) $I_0 = 10^{-12} \text{ kg} \cdot \text{m}^{-1} \cdot \text{s}^{-3}$
 - (e) $I_0 = 10^{-12} \text{ kg/s}^3$
23. Which of the following sets of equipment cannot be used to measure the local value of the acceleration due to gravity (g)?
- (a) A spring scale (which reads in force units) and a known mass
 - (b) A rod of known length, an unknown mass, and a stopwatch
 - (c) A launcher which launches projectiles at a known speed, a projectile of known mass, and meter stick.
 - (d) An inclined plane of known inclination, several carts of different known masses, and a stopwatch
 - (e) A motor with a known output power, a known mass, a piece of string of unknown length, and a stopwatch
24. Three point masses m are attached together by identical springs. When placed at rest on a horizontal surface the masses form a triangle with side length l . When the assembly is rotated about its center at angular velocity ω , the masses form a triangle with side length $2l$. What is the spring constant k of the springs?
- (a) $2m\omega^2$
 - (b) $\frac{2}{\sqrt{3}}m\omega^2$
 - (c) $\frac{2}{3}m\omega^2$
 - (d) $\frac{1}{\sqrt{3}}m\omega^2$
 - (e) $\frac{1}{3}m\omega^2$

25. Consider the two orbits around the Sun shown below. Orbit P is circular with radius R , orbit Q is elliptical such that the farthest point b is between $2R$ and $3R$, and the nearest point a is between $R/3$ and $R/2$. Consider the magnitudes of the velocity of the circular orbit v_c , the velocity of the comet in the elliptical orbit at the farther point v_b , and the velocity of the comet in the elliptical orbit at the nearest point v_a . Which of the following rankings is correct?

- (a) $v_b > v_c > 2v_a$
- (b) $2v_c > v_b > v_a$
- (c) $10v_b > v_a > v_c$
- (d) $v_c > v_a > 4v_b$
- (e) $2v_a > \sqrt{2}v_b > v_c$