

CPE1500 Boolean Algebra Reference Sheet

Axioms

	Axiom		Dual	Name
A1	$B = 0 \text{ if } B \neq 1$	A1'	$B = 1 \text{ if } B \neq 0$	Binary field
A2	$\bar{0} = 1$	A2'	$\bar{1} = 0$	NOT
A2	$0 \cdot 0 = 0$	A3'	$1 + 1 = 1$	AND/OR
A4	$1 \cdot 1 = 1$	A4'	$0 + 0 = 0$	AND/OR
A5	$0 \cdot 1 = 1 \cdot 0 = 0$	A5'	$1 + 0 = 0 + 1 = 1$	AND/OR

Theorems of One Variable

	Theorem		Dual	Name
T1	$B \cdot 1 = B$	T1'	$B + 0 = B$	Identity
T2	$B \cdot 0 = 0$	T2'	$B + 1 = 1$	Null Element
T3	$B \cdot B = B$	T3'	$B + B = B$	Idempotency
T4	$\bar{\bar{B}} = B$	T4'	same	Involution
T5	$B \cdot \bar{B} = 0$	T5'	$B + \bar{B} = 1$	Complements

Theorems of Multiple Variables

	Theorem		Dual	Name
T6	$B \cdot C = C \cdot B$	T6'	$B + C = C + B$	Commutativity
T7	$(B \cdot C) \cdot D = B \cdot (C \cdot D)$	T7'	$(B + C) + D = B + (C + D)$	Associativity
T8	$(B \cdot C) + (B \cdot D) = B \cdot (C + D)$	T8'	$(B + C) \cdot (B + D) = B + (C \cdot D)$	Distributivity
T9	$B \cdot (B + C) = B$	T9'	$B + (B \cdot C) = B$	Covering
T10	$(B \cdot C) + (B \cdot \bar{C}) = B$	T10'	$(B + C) \cdot (B + \bar{C}) = B$	Combining
T11	$(B \cdot C) + (\bar{B} \cdot D) + (C \cdot D)$ $= B \cdot C + \bar{B} \cdot D$	T11'	$(B + C) \cdot (\bar{B} + D) \cdot (C \cdot D)$ $= (B + C) \cdot (\bar{B} + D)$	Consensus
T12	$\overline{B_0 \cdot B_1 \cdot B_2 \dots} = (\bar{B}_0 + \bar{B}_1 + \bar{B}_2 \dots)$	T12'	$\overline{B_0 + B_1 + B_2 \dots} = (\bar{B}_0 \cdot \bar{B}_1 \cdot \bar{B}_2 \dots)$	De Morgan's Theorem