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If the distribution of heights is roughly normal, then for about 95% of the people, the estimate will be correct to within 6 inches.

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average: least squares estimate

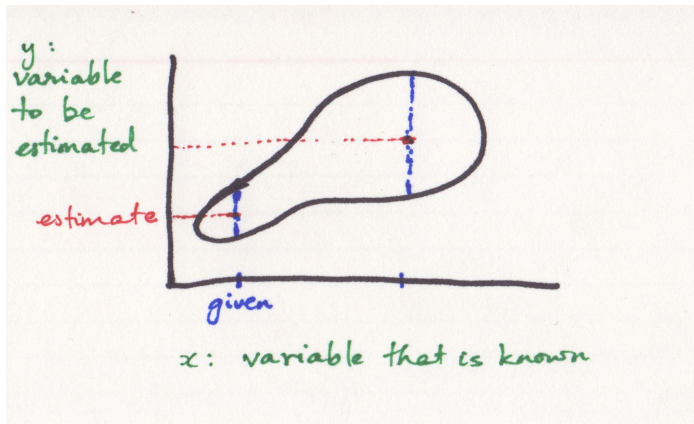
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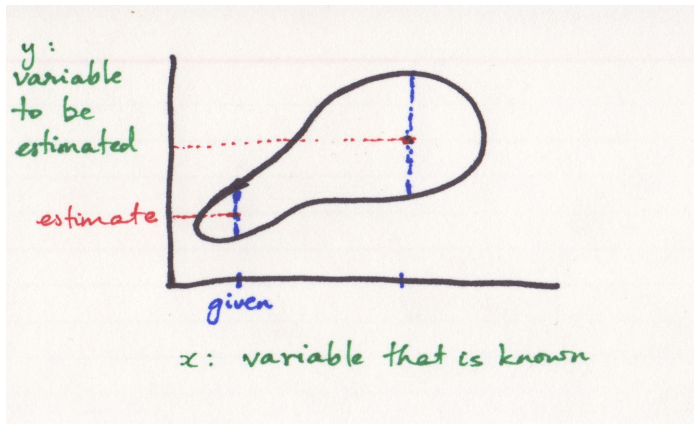
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Each estimate is at the center of a vertical strip.

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- **the distributions of both the variables are roughly normal**
- **the distribution of values in each vertical and horizontal strip is roughly normal**