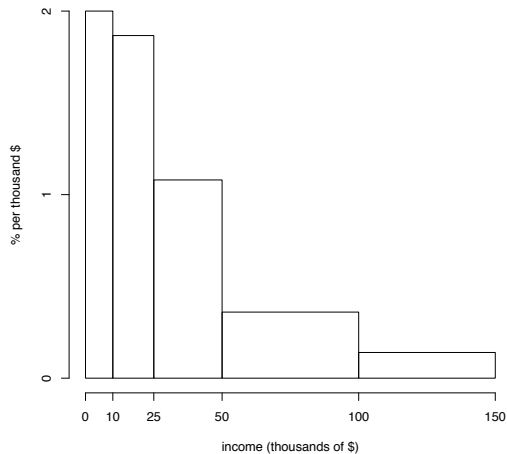


# Shapes of distributions

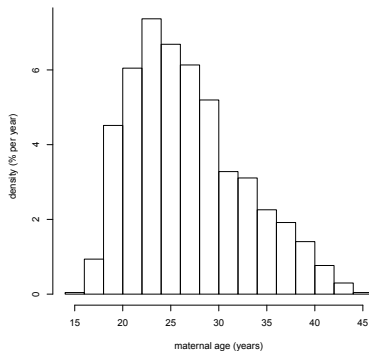
# Shapes of distributions

Annual income of U.S. adults in 2010



# A bell shaped distribution

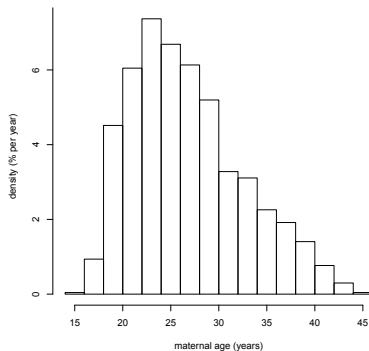
Ages of mothers who  
gave birth at a local  
hospital



# A bell shaped distribution

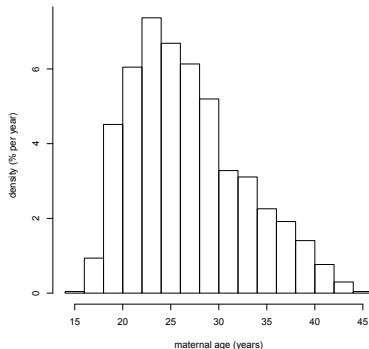
Ages of mothers who  
gave birth at a local  
hospital

Birthweights of their  
babies

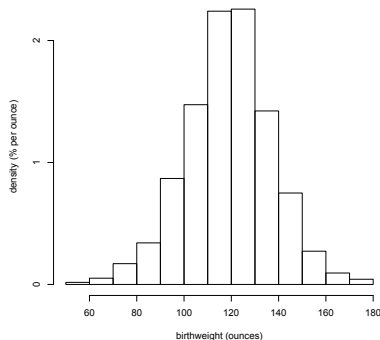


# A bell shaped distribution

Ages of mothers who gave birth at a local hospital

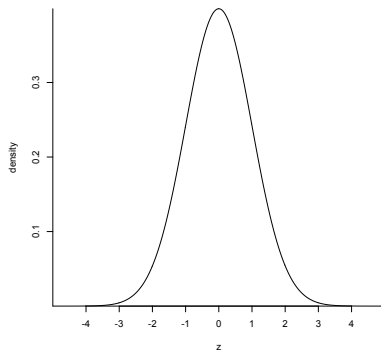


Birthweights of their babies

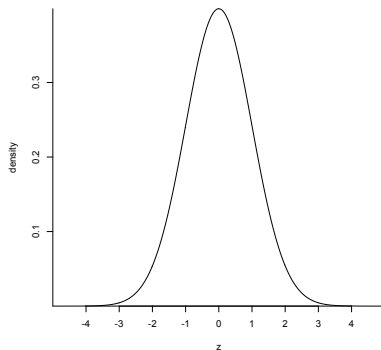


# The standard normal curve

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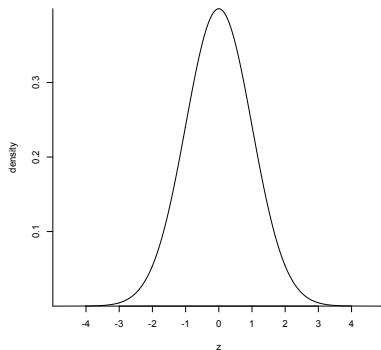


density at  $z$

$$= \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}z^2}, \quad -\infty < z < \infty$$



# The standard normal curve

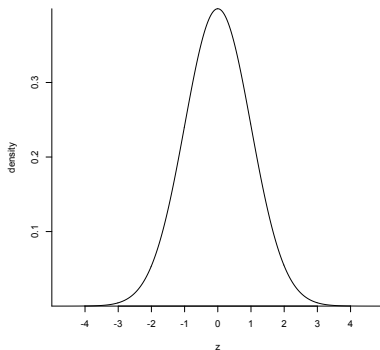


density at  $z$

$$= \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}z^2}, \quad -\infty < z < \infty$$

- total area = 1

# The standard normal curve

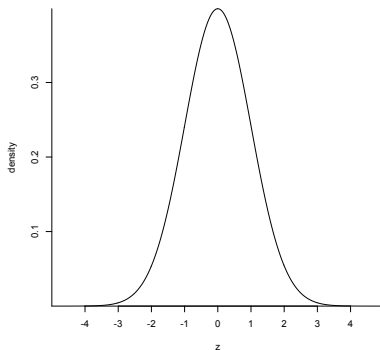


density at  $z$

$$= \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}z^2}, \quad -\infty < z < \infty$$

- total area = 1
- balance point:  $z = 0$

# The standard normal curve



density at  $z$

$$= \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}z^2}, \quad -\infty < z < \infty$$

- total area = 1
- balance point:  $z = 0$
- points of inflection:  
 $z = -1, z = 1$

# Useful to remember

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**Central areas:**

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- between  $z = -1$  and  $z = 1$ : about 68%

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## Tail areas:



# Useful to remember

## Central areas:

- between  $z = -1$  and  $z = 1$ : about 68%
- between  $z = -2$  and  $z = 2$ : about 95%

## Tail areas:

- to the left of  $-1$ : about 16%
- to the right of  $1$ : about 16%

# Useful to remember

## Central areas:

- between  $z = -1$  and  $z = 1$ : about 68%
- between  $z = -2$  and  $z = 2$ : about 95%

## Tail areas:

- to the left of  $-1$ : about 16%
- to the right of  $1$ : about 16%
- to the left of  $-2$ : about 2.5%
- to the right of  $2$ : about 2.5%

# Useful to remember

## Central areas:

- between  $z = -1$  and  $z = 1$ : about 68%
- between  $z = -2$  and  $z = 2$ : about 95%

## Tail areas:

- to the left of  $-1$ : about 16%
- to the right of  $1$ : about 16%
- to the left of  $-2$ : about 2.5%
- to the right of  $2$ : about 2.5%

## Percentiles:

# Useful to remember

## Central areas:

- between  $z = -1$  and  $z = 1$ : about 68%
- between  $z = -2$  and  $z = 2$ : about 95%

## Tail areas:

- to the left of  $-1$ : about 16%
- to the right of  $1$ : about 16%
- to the left of  $-2$ : about 2.5%
- to the right of  $2$ : about 2.5%

## Percentiles:

- 95th percentile:  $z = 1.65$ , roughly
- 5th percentile:  $z = -1.65$ , roughly