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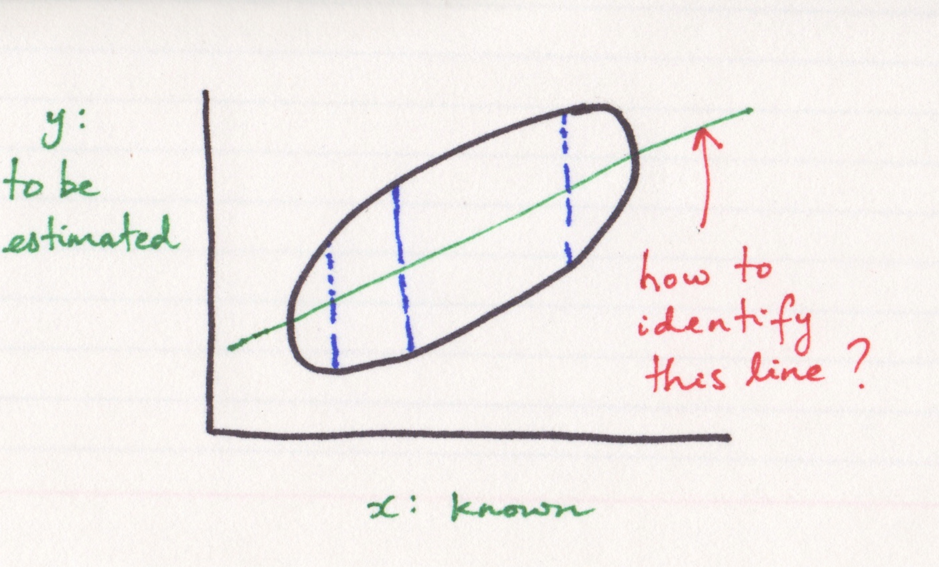

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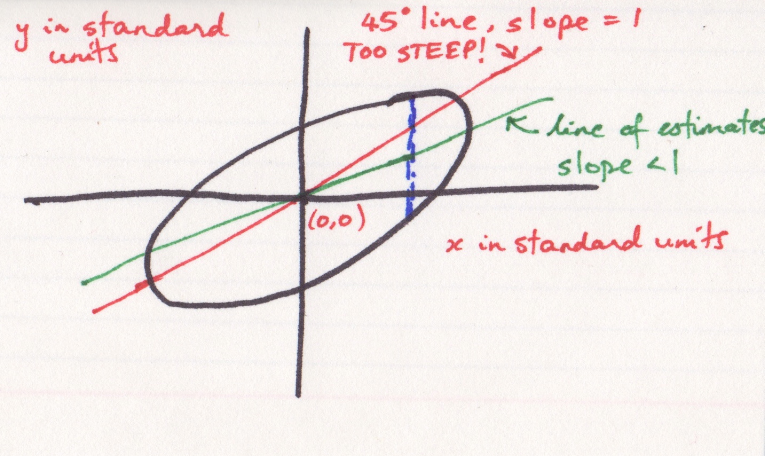

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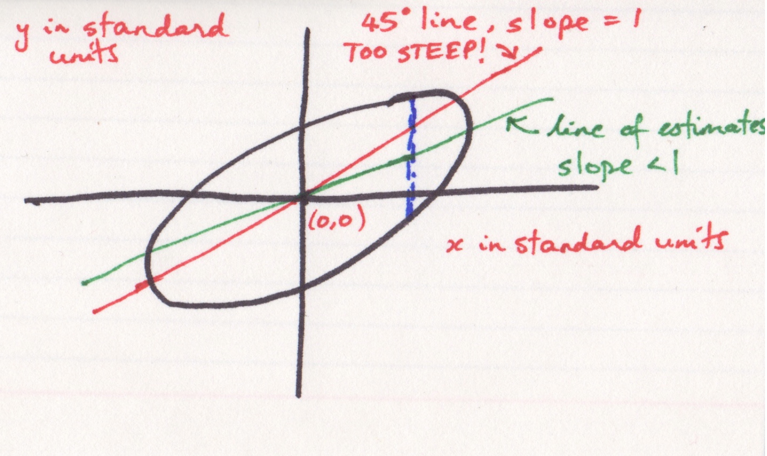


**The estimates are on the green line. The slope of the green line is $r$.**

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Equation of the regression line

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**Weights:** average 160 pounds, SD 20 pounds

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$=$ 80th percentile of standard normal curve

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**Answer: roughly 66th percentile on the final**

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**To find the regression estimate of $y$ based on a given $x$:**

- First find the given $x$ in standard units.
- Multiply the result by $r$. That is your estimate of $y$, but it's in standard units.
- Now convert your estimate from standard units to the units that are required.